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An Updated Comprehensive Kinetic Model of Hydrogen Combustion

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Abstract

A comprehensively tested H_2/O_2 chemical kinetic mechanism based on Mueller et al. [1] and recently published kinetic and thermodynamic information is presented. The revised mechanism is validated against a wide range of experimental conditions, including those found in shock tubes, flow reactors, and laminar premixed flame. Excellent agreement of the model predictions with the experimental observations demonstrates the mechanism is comprehensive and has good predictive capabilities for different experimental systems, including new results published subsequent to the work of Mueller et al. [1], particularly high pressure laminar flame speed and shock tube ignition results. The reaction $\text{H}+\text{OH}+\text{M}$ is found to be primarily significant only to laminar flame speed propagation predictions at high pressure. All experimental hydrogen flame speed observations can be adequately fit using any of the several transport coefficient estimates presently available in the literature for the hydrogen oxygen system simply by adjusting the rate parameters for this reaction within their present uncertainties.

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Introduction

The H_2/O_2 reaction mechanism plays a prominent role in fundamental chemical kinetics research as well as in the applied fields of fire safety, energy conversion and propulsion. Not only is hydrogen an important fuel for these applications, but the elementary kinetics involving H , O , OH , HO_2 , and H_2O_2 determine the composition of the radical pool in hydrocarbon reaction systems. The reaction system and associated mechanistic representations have been used extensively by several research groups including ours in various experiments to derive elementary reaction rate information, for example, by perturbations of kinetics using added species. The kinetics of the H_2/O_2 system and its behavior over a range of experiments conducted in a variable pressure flow reactor (VPFR) were recently discussed by Mueller et al. [1]. The initial mechanism development relied heavily on the earlier work of Yetter et al. [2] on the moist carbon monoxide oxidation system, which was comprehensively studied. The mechanism presented in [1] was extensively studied at flow reactor conditions, but it was not tested against or modified as a result of comparisons with experimental data derived in other types of experiments and in other parameter ranges. Indeed, the authors noted several issues that deserved further attention in applying the mechanism more generally. In the strictest sense, the published mechanism was therefore not “comprehensive”, a term originally applied by Westbrook and Dryer [3,4] to describe a mechanism developed by comparison against a number of different sources of kinetic data. These sources frequently include laminar flame speed measurements [5-8], shock tube ignition delay studies [9-14], and other sources such as static and stirred reactors. New flame speed experimental results using $\text{H}_2/\text{O}_2/\text{He}$ mixtures at pressures ranging from 1 to 20 atm appear to be poorly predicted by the Mueller et al. mechanism [7], while predictions of similar experiments using H_2/O_2 mixtures in argon, helium and nitrogen at 1 to 3 atm pressure are quite reasonable [8]. Recently, Curran and coworkers [15] have made wide-ranging comparisons with various experimental data and they have in addition noted that the mechanism in [1] substantially over-predicts shock tube ignition delay data reported by Skinner et al. [11].

Since the publication of [1], there have been several important elementary kinetic publications further addressing two of the most important reactions involving the hydrogen radical, i.e., the branching reaction [16],



and the competitive reaction [17-20],



While some of the results presented in [19] were known at the time of our earlier consideration of (R2) [21], reference 19 contributes new insights to the magnitudes of and mechanism responsible for the apparent third body efficiencies of various species in (R2), particularly H_2O . In addition, the enthalpy of formation of OH has recently been conclusively revised [22].

In the present study, we update the mechanism of [1] based upon the new thermodynamic data and rate coefficients, and compare the updated mechanism against a wide array of experimental data including the original VPFR data, shock tube ignition delay data, and the new flame speed results to yield a “comprehensive” hydrogen oxygen mechanism.

We wish to emphasize, however, that the term “comprehensive” carries no inference as to whether a mechanism is “complete”, “unique”, and will never require further revisions. Additional experimental systems observations that increase the constraints which define the acceptability of predictive comparisons and/or improvements in uncertainties of elementary kinetic information (rate data, thermochemistry) can both inspire the need to revise a previously developed comprehensive mechanism. Thus, even “comprehensive” mechanisms should be reviewed in a timely manner as new information becomes available. This is a perplexing, but extremely important issue in light of the hierarchical nature of hydrocarbon kinetics and its dependence on H_2/O_2 kinetics. Revisions of mechanisms are likely to be necessary in perpetuity, given the nature of the field. Moreover, even the most complete mechanistic description to be envisioned will most likely never be “unique” in terms of the associated elementary reaction rate and thermochemical parameters.

Updated H₂/O₂ Chemical Kinetics

The updated detailed H₂/O₂ reaction mechanism consists of 19 reversible elementary reactions and thermochemical data listed in Table I and II, respectively. Reverse rate constants are computed from the forward rate constants and the equilibrium constants. The third-body efficiency of helium is assumed to be the same as that of argon, except for reaction 9 in Table I. In the present work, the following parameters of mechanism presented in Mueller et al. [1] are revised:

1. *The Enthalpy of Formation of OH.* Recently, Ruscic et al. [22] studied the heat of formation of OH radical both experimentally and theoretically, and the recommended value of 8.91 kcal/mol at 298 K is in excellent agreement with the recent experimental result of 8.92 kcal/mol [23]. The heat of formation value presented by Ruscic et al. [22] is used in the current mechanism.

2. *The Rate Constant of (R1).* We performed a sensitivity analysis of the original mechanism for a VPFR case at 3.4 atm [1], for a premixed laminar flame speed at 10 atm [7], and for an ignition delay case under Skinner et al.'s [11] shock tube conditions. The normalized sensitivity coefficient of a reaction is defined as $\frac{\partial \ln Y}{\partial \ln k}$,

$\frac{\partial \ln s}{\partial \ln k}$, and $\frac{\partial \ln \tau}{\partial \ln k}$ for the disappearance of a species Y in a flow reactor, for the laminar flame speed, and for ignition delay time, respectively, where k is the rate constant, Y the mass fraction of a species (H₂ in this study), s the laminar flame speed, and τ the ignition delay time. The most sensitive reactions found are shown in Figure 1 along with their sensitivity coefficients as defined above.

As is well known through the literature and also shown in Figure 1, the H₂/O₂ system is very sensitive to the key chain branching reaction (R1) and the important chain termination reaction (R2). Mueller et al. [1] used the rate constant expression of Pirraglia et al. [24] for the reaction (R1) and noted that while the expression over-predicts the recent high temperature data above 1700 K [25-27], it more properly predicts the rate at low temperatures. The recent analysis of Hessler [16] excluded consideration of certain sets of available elementary rate data [27] based upon a defined uncertainty envelope. The resulting rate constant correlation predicts not only the data in [24-26], but also more

closely predicts appropriate rates at low temperatures within close proximity to those predicted by the expression in [24]. In the present mechanism, the rate constant of reaction (R1) is updated to that in Hessler [16]. Figure 2 compares the predictions of the rate constant of reaction (R1) available in literature. Yu et al. [28] analyzed the shock tube experimental data of [25] and [29], and used an H₂/O₂ mechanism to derive the rate constant of reaction (R1) over 1336-3370K. As shown in Figure 2, over this temperature range, the prediction of Hessler [16] is close to those of [25] and [28] (within 15%). The reasons driving us to choose the correlation of Hessler [16] over others will become clear below.

3. *The Low-Pressure-Limit Rate Constant of (R2).* The Troe formulation [30] is applied for reaction (R2) with the high-pressure-limit rate constant used in [1], and the low-pressure-limit results, k_0 , reported in [19]. Michael et al. [19] calculated k_0 with M representing N₂, Ar, He, H₂, H₂O, and O₂, and verified calculated values against experimental data. We fitted the data that were presented in the paper for each third body condition to capture both the rate constant and bath gas temperature dependences. The calculated fits in Arrhenius form for a bath gas of N₂ or Ar are as follows (in units of cm⁶mol⁻²s⁻¹):

$$k_0^{\text{N}_2} = 6.37 \times 10^{20} T^{-1.72} \exp(-264 / T),$$

$$k_0^{\text{Ar}} = 9.04 \times 10^{19} T^{-1.50} \exp(-248 / T).$$

The third-body efficiency of He, H₂, O₂, and H₂O are taken as the average value over the temperature range of 300-3000 K. The fall-off range of (R2) is described by taking the broadening factor F_c as 0.8 for N₂, and 0.5 for Ar. This implementation represents a compromise formulation that responds to: (1) the limitations of CHEMKIN-II format, especially, an inability to implement temperature-dependent collision efficiencies in fall-off reactions, and (2) the lack of fundamental understanding of the mixing rules for the fall-off reactions with bath gases having different broadening factors. As a consequence, the fall-off kinetics of (R2) is expressed in two groups, for N₂ and Ar/He as the bath gas, respectively.

The predictions of k_0 of (R2) reported in some recent publications are shown in Figure 3. As can be seen, the result of Michael et al. [19] is in very good agreement with that of [18]. Figure 4 shows the temperature and pressure dependence of the rate constant

of (R2) predicted by the present mechanism and by Troe [17]. We see that these two predictions agree reasonably well (within 20%) with each other over 300-3000 K and from low to high pressure range.

Figure 5 shows the branching ratio, i.e. (R2)/(R1), at 0.1, 1, and 10 atm with the current revisions and from [1]. There is very good agreement (within 2%) at the conditions (800-900 K) where the value of k_0 used in [1] was experimentally derived [31]. At temperature higher than 2000 K, the difference between the two predictions becomes larger (~30%), but (R2) is of no significance at these conditions relative to (R1). Achieving agreement of this ratio at 800-900 K is very important to this update, as not only is this a temperature region most sensitive to the ratio, but our earlier work [31] defined this ratio experimentally with a very small uncertainty. As mentioned in the Mueller et al. [21], the use of data for reaction (R1) from other sources did not result in the appropriate ratio when combined with their independent measurement of (R2) in this temperature range. The uncertainty in this experimental determination was recently reviewed and further reduced by additional analyses [32]. On the other hand, the determined value of (R2) agrees very well with the extrapolation of the measurements obtained by Michael et al. [19] to flow reactor temperatures.

4. *The Rate Constant of $H + OH + M = H_2O + M$, (R3).* The sensitivity analysis in Figure 1 also indicates that the laminar flame speed case is sensitive to (R3), while flow reactor and shock tube ignition delay predictions are essentially insensitive to this reaction at all conditions. In order to improve flame predictions, we modified the A factor of the rate constant of (R3) to $3.8 \times 10^{22} \text{ cm}^6 \text{ mol}^{-2} \text{ s}^{-1}$ (from 2.2×10^{22} [1]). Curran coworkers [15] also suggest modification of this reaction to improve flame speed predictions. Figure 6 shows a review of the rate constant reported in the literature for (R3) [33-39]. Obviously, the rate constant results span more than an order of magnitude, with the value chosen here being in the middle of the range. Because of the large uncertainty in this rate constant, laminar flame speed predictions using any particular set of diffusion coefficients recommended by various authors can be forced to predict the same flame speed simply by adjusting the value of this single rate constant.

Results and Discussion

The mechanism updated as described above was compared against a wide range of experimental data, including laminar flame speed, shock tube ignition delay time, and the species profiles in VPFR, shock tube, and burner-stabilized flame studies. The SENKIN code [40] was used to simulate experimental conditions in a shock tube and flow reactor. The PREMIX code [41] was used for flame calculations. We used the standard CHEMKIN transport package [42] with multicomponent formulation and Soret effects included. A minimum of 1000 grid points was imposed in the PREMIX calculation for a fully converged flame speed value. Representative test results are shown in Figures 7 – 18.

The comparisons in Figures 7 and 8 show that the predictions of the present mechanism are in excellent agreement with the laminar flame speed measurements for $\text{H}_2/\text{O}_2/\text{He}$ mixture at pressures ranging from 1 to 20 atm. The prediction of the laminar flame speed of H_2/O_2 system diluted by N_2 , Ar, or He at 1 atm is presented in Figure 9.

Predictions also compare very well with shock tube ignition delay data, as is demonstrated with representative cases in Figures 10 – 12. Figure 13 shows the reaction time when the OH mole fraction under shock tube conditions reaches a specific fraction of the equilibrium value. Figure 14 and 15 show the time history of the H and OH mole fraction in shock tube experiments. Clearly, the current mechanism agrees with the experimental measurements very well.

The original Mueller et al. mechanism was validated against 16 VPFR experiments [1]. Excellent agreement of the model predictions with the experimental measurement was demonstrated in reference 1. The current mechanism was verified against all of these VPFR cases, and agrees with the experiments as well as the predictions using the original mechanism. Representative results are shown in Figures 16 and 17. Time-shift is use

d to compare the model predictions with the experimental measurement by shifting the simulated values along the time axis to match the 50% fuel consumption point.

The comparison of model predictions with species profiles measured in burner-stabilized flame [43] is shown in Figure 18. The experimental flame temperature profile

was used in the PREMIX calculation. Clearly, the predictions of the present mechanism and Mueller et al. [1] are almost the same and yield reasonably good level of agreement with the experiments, typical for premixed flame modeling [53].

Conclusion

The detailed H_2/O_2 reaction mechanism of Mueller et al. [1] has been updated using recently published rate constants of the reaction (R1) and (R2), and the thermodynamic data of OH. An important constraint on combinations of (R1) and (R2) is provided by the ratio of these reactions in the temperature range 800-900 K. Above and below this temperature range, one or the other of these reactions becomes significantly less important, and determining their ratio at other temperatures is subject to higher uncertainties. Analyses also show that reaction (R3) is of significance to observations in the case of high pressure flames propagation. The present uncertainties in experimental determinations, third body effects, and theory are so large that within the bounded range, the rate can be varied such that high pressure laminar flame speed data can be modeled as satisfactorily by any proposed set of transport properties. Thus hydrogen-oxygen flame speed experiments cannot at present resolve whether sources of disparity are the modeling of transport properties, (R3), or experiment. Here, we modified the rate constant of reaction (R3) to achieve flame propagation model performance using the transport properties from the CHEMKIN transport package [42].

The present mechanism is compared against a wide range of experimental conditions (298-3000 K, 0.3-87 atm, $\phi = 0.25$ -5.0) found in laminar premixed flames, shock tubes, and flow reactors. Very good agreement of the model predictions with the experimental measurement demonstrates that the updated comprehensive mechanism has excellent predictive capabilities for different experimental systems. The current mechanism in an electronic form compatible with CHEMKIN II is available by e-mail request (fldryer@princeton.edu).

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Table I. Detailed H₂/O₂ Reaction Mechanism. Units are cm³-mol-sec-kcal-K, and $k = A T^n \exp(-E/RT)$.

		A	n	E	Reference	
<i>H₂/O₂ Chain Reactions</i>						
1.	H + O ₂ = O + OH	3.55×10^{15}	-0.41	16.6	Hessler [16]	
2.	O + H ₂ = H + OH	5.08×10^4	2.67	6.29	Sutherland et al. [44]	
3.	H ₂ + OH = H ₂ O + H	2.16×10^8	1.51	3.43	Michael et al. [45]	
4.	O + H ₂ O = OH + OH	2.97×10^6	2.02	13.4	Sutherland et al. [46]	
<i>H₂/O₂ Dissociation/Recombination Reactions</i>						
5.	H ₂ + M = H + H + M ^a	4.58×10^{19}	-1.40	104.38	Tsang et al. [47]	
	H ₂ + Ar = H + H + Ar	5.84×10^{18}	-1.10	104.38	Tsang et al. [47]	
	H ₂ + He = H + H + He	5.84×10^{18}	-1.10	104.38	See text	
6.	O + O + M = O ₂ + M ^a	6.16×10^{15}	-0.50	0.00	Tsang et al. [47]	
	O + O + Ar = O ₂ + Ar	1.89×10^{13}	0.00	-1.79	Tsang et al. [47]	
	O + O + He = O ₂ + He	1.89×10^{13}	0.00	-1.79	See text	
7.	O + H + M = OH + M ^a	4.71×10^{18}	-1.0	0.00	Tsang et al. [47]	
8.	H + OH + M = H ₂ O + M ^b	3.8×10^{22}	-2.00	0.00	See text	
<i>Formation and Consumption of HO₂</i>						
9.	H + O ₂ + M = HO ₂ + M ^c	k _O	6.37×10^{20}	-1.72	0.52	Michael et al. [19] (M = N ₂)
	H + O ₂ + M = HO ₂ + M ^d	k _O	9.04×10^{19}	-1.50	0.49	Michael et al. [19] (M = Ar or He)
		k _∞	1.48×10^{12}	0.60	0.00	Cobos et al. [48]
10.	HO ₂ + H = H ₂ + O ₂		1.66×10^{13}	0.00	0.82	Mueller et al. [1]
11.	HO ₂ + H = OH + OH		7.08×10^{13}	0.00	0.30	Mueller et al. [1]
12.	HO ₂ + O = OH + O ₂		3.25×10^{13}	0.00	0.00	Baulch et al. [34]
13.	HO ₂ + OH = H ₂ O + O ₂		2.89×10^{13}	0.00	-0.50	Baulch et al. [34]
<i>Formation and Consumption of H₂O₂</i>						
14.	HO ₂ + HO ₂ = H ₂ O ₂ + O ₂ ^e		4.20×10^{14}	0.00	11.98	Hippler et al. [49]
	HO ₂ + HO ₂ = H ₂ O ₂ + O ₂		1.30×10^{11}	0.00	-1.63	
15.	H ₂ O ₂ + M = OH + OH + M ^f	k _O	1.20×10^{17}	0.00	45.5	Warnatz [50]
		k _∞	2.95×10^{14}	0.00	48.4	Brouwer et al. [51]
16.	H ₂ O ₂ + H = H ₂ O + OH		2.41×10^{13}	0.00	3.97	Tsang et al. [47]
17.	H ₂ O ₂ + H = H ₂ + HO ₂		4.82×10^{13}	0.00	7.95	Tsang et al. [47]
18.	H ₂ O ₂ + O = OH + HO ₂		9.55×10^6	2.00	3.97	Tsang et al. [47]
19.	H ₂ O ₂ + OH = H ₂ O + HO ₂ ^e		1.00×10^{12}	0.00	0.00	Hippler et al. [52]
	H ₂ O ₂ + OH = H ₂ O + HO ₂		5.8×10^{14}	0.00	9.56	

^aEfficiency factors are: $\epsilon_{\text{H}_2\text{O}} = 12.0$, $\epsilon_{\text{H}_2} = 2.5$, $\epsilon_{\text{Ar}} = 0.75$, and $\epsilon_{\text{He}} = 0.75$. When a rate constant is declared specifically for Ar or He collision partner, the efficiency of Ar or He is set to zero when determining M for the same reaction.

^bEfficiency factors are: $\epsilon_{\text{H}_2\text{O}} = 12.0$, $\epsilon_{\text{H}_2} = 2.5$, $\epsilon_{\text{Ar}} = 0.38$, and $\epsilon_{\text{He}} = 0.38$.

^cWhen the main bath gas is N₂. Troe parameter is: $F_c = 0.8$. Efficiency factors are: $\epsilon_{\text{H}_2\text{O}} = 11.0$, $\epsilon_{\text{H}_2} = 2.0$, and $\epsilon_{\text{O}_2} = 0.78$.

^dWhen the main bath gas is Ar or He. Troe parameter is: $F_c = 0.5$. Efficiency factors are: $\varepsilon_{\text{H}_2\text{O}} = 16.0$, $\varepsilon_{\text{H}_2} = 3.0$, $\varepsilon_{\text{O}_2} = 1.1$, and $\varepsilon_{\text{He}} = 1.2$.

^eReactions 14 and 19 are expressed as the sum of the two rate expressions.

^fTroe parameter is: $F_c = 0.5$. Efficiency factors are: $\varepsilon_{\text{H}_2\text{O}} = 12.0$, $\varepsilon_{\text{H}_2} = 2.5$, $\varepsilon_{\text{Ar}} = 0.64$, and $\varepsilon_{\text{He}} = 0.64$.

Table II. $\Delta H_f(298.15)$, $S(298.15)$, and $C_p(T)$ for Species Considered in the H_2/O_2 Reaction Mechanism. Units Are cal/mol/K for S and C_p , and kcal/mol for ΔH_f .¹

Species	$\Delta H_f(298.15)$	$S(298.15)$	$C_p(300)$	$C_p(500)$	$C_p(800)$	$C_p(1000)$	$C_p(1500)$	$C_p(2000)$
H	52.10	27.39	4.97	4.97	4.97	4.97	4.97	4.97
O	59.56	38.47	5.23	5.08	5.02	5.00	4.98	4.98
OH	8.91	43.91	7.16	7.05	7.15	7.34	7.87	8.28
H ₂	0.0	31.21	6.90	7.00	7.07	7.21	7.73	8.18
O ₂	0.0	49.01	7.01	7.44	8.07	8.35	8.72	9.03
H ₂ O	-57.80	45.10	8.00	8.45	9.22	9.87	11.26	12.22
HO ₂	3.0	54.76	8.35	9.47	10.77	11.38	12.48	13.32
H ₂ O ₂	-32.53	55.66	10.42	12.35	14.29	15.21	16.85	17.88
N ₂	0.0	45.77	6.95	7.08	7.50	7.83	8.32	8.60
Ar	0.0	36.98	4.97	4.97	4.97	4.97	4.97	4.97
He	0.0	30.12	4.97	4.97	4.97	4.97	4.97	4.97

¹ After acceptance of the present work for publication, we became aware of a new evaluation of the standard heat of formation for HO₂ [54]. The new value is 2.88 +/- .15 kcal/mole (as opposed to 3.0 kcal/mole given in Table 2. While all of the results presented here were obtained with an old value, we have confirmed that using a new result [54] does not produce noticeable changes in model predictions. The new value is therefore recommended for future use of the present mechanism.

Figure Captions

- Figure 1. Sensitivity coefficient of reactions for a flow reactor [1], laminar flame speed [7], and shock tube ignition delay [11] case calculated by using the mechanism of Mueller et al. [1]. Initial conditions: $\text{H}_2 = 1.01\%$, $\text{O}_2 = 0.52\%$ with balance N_2 at 3.4 atm and 933 K [1]; $\text{H}_2 = 19.4\%$, $\text{O}_2 = 6.5\%$ with balance He at 10 atm and 298 K [7]; $\text{H}_2 = 8.0\%$, $\text{O}_2 = 2.0\%$ with balance Ar at 5 atm and 960 K [11]. The sensitivity coefficient for the flow reactor case is taken at the time when 50% H_2 has been consumed.
- Figure 2. Rate coefficient of reaction $\text{H} + \text{O}_2 \rightarrow \text{OH} + \text{O}$.
- Figure 3. Rate coefficient of reaction $\text{H} + \text{O}_2 + \text{M} \rightarrow \text{HO}_2 + \text{M}$ for $\text{M} = \text{N}_2$.
- Figure 4. Temperature and pressure dependence of the reaction rate of $\text{H} + \text{O}_2 (+ \text{M}) \rightarrow \text{HO}_2 (+ \text{M})$ for $\text{M} = \text{N}_2$. Solid lines represent the values used in the present mechanism, and dashed lines the recommendations of [17].
- Figure 5. Branching ratio of the reaction (R1) and (R2). Solid lines: the present model; dashed lines: Mueller et al. [1].
- Figure 6. Rate constant of $\text{H} + \text{OH} + \text{M} \rightarrow \text{H}_2\text{O} + \text{M}$ for $\text{M} = \text{Ar}$.
- Figure 7. Laminar flame mass burning rate at 1, 3, 5 atm for $\text{H}_2/\text{O}_2/\text{He}$ mixture ($\text{O}_2:\text{He} = 1:7$). Symbols: experimental data [7]; solid lines: the present model; dashed lines: Mueller et al. [1].
- Figure 8. Laminar flame mass burning rate at 10, 15, 20 atm for $\text{H}_2/\text{O}_2/\text{He}$ mixture ($\text{O}_2:\text{He} = 1:11.5$). Symbols: experimental data [7]; solid lines: the present model; dashed lines: Mueller et al. [1].
- Figure 9. Laminar flame speed at 1 atm for H_2/O_2 diluted with N_2 , Ar, or He. ($\text{O}_2:\text{N}_2 = \text{O}_2:\text{Ar} = \text{O}_2:\text{He} = 1:3.76$). Symbols: experimental data [5-8]; solid lines: the present model; dashed lines: Mueller et al. [1].
- Figure 10. Ignition delay time of $\text{H}_2/\text{O}_2/\text{N}_2$ mixture at 2 atm or 2.5 atm ($\text{H}_2 = 29.6\%$, $\text{O}_2 = 14.8\%$). Symbols: experimental data [9,10]; solid lines: the present model; dashed lines: Mueller et al. [1]. Ignition delay time is defined by a rapid increase in the pressure.

- Figure 11. Ignition delay of H₂/O₂/Ar mixtures in shock tubes. Initial conditions: H₂ = 8.0%, O₂ = 2.0% at 5 atm [11]; H₂ = 1.0%, O₂ = 2.0% at 1 atm [12]; H₂ = 2.0%, O₂ = 1.0% at 33, 57, 64, and 87 atm [13]. Symbols: experimental data [11-13]; solid lines: the present model; dashed lines: Mueller et al. [1]. Ignition delay time for the cases of [11] is defined by the maximum of OH concentration; for [12] - as the time when OH concentration reaches 1×10^{-6} mol/litter; and for [13] - by the maximum of $\frac{d[\text{OH}]}{dt}$.
- Figure 12. Ignition delay result of H₂/O₂/Ar mixture at 2 atm (H₂ = 6.7%, O₂ = 3.3%). Symbols: experimental data [14]; solid lines: the present model; dashed lines: Mueller et al. [1]. Ignition delay time is defined by a rapid rise of pressure.
- Figure 13. Reaction time in a shock tube when OH mole fraction reaches 0.25, 0.5, 0.75, and 0.99 times the equilibrium value, respectively. Initial conditions: H₂ = 5.0%, O₂ = 0.493% with balance Ar at 0.675 atm and 1980 K (for squares); H₂ = 1.10%, O₂ = 0.208% with balance Ar at 1.98 atm and 2898 K (for diamonds). Open symbols represent experimental data [25], and solid symbols the present mechanism.
- Figure 14. Time history of H mole fraction in a shock tube. Initial conditions: H₂ = 0.99%, O₂ = 0.10% with balance Ar at 0.79 atm and 1700 K. Dotted line: experimental data [25]; solid line: the present model; dashed line: Mueller et al. [1].
- Figure 15. Time history of OH mole fraction in a shock tube. Initial conditions: H₂ = 4002 ppm, O₂ = 3999 ppm with balance Ar at 1.075 atm and 2590 K. Dotted line: experimental data [23]; solid line: the present model; dashed line: Mueller et al. [1].
- Figure 16. Reaction profiles of H₂/O₂/N₂ mixture in a flow reactor. Initial conditions: H₂ = 0.50%, O₂ = 0.50% with balance N₂ at 0.3 atm and 880 K. Symbols: experimental data [1]; solid lines: the present model; dashed lines: Mueller et al. [1].

Figure 17. Reaction profiles of $\text{H}_2/\text{O}_2/\text{N}_2$ mixture in a flow reactor. Initial conditions: $\text{H}_2 = 1.01\%$, $\text{O}_2 = 0.52\%$ with balance N_2 at 3.4 atm and 933 K. Symbols: experimental data [1]; solid lines: the present model; dashed lines: Mueller et al. [1].

Figure 18. Species profiles of $\text{H}_2/\text{O}_2/\text{Ar}$ mixture in burner-stabilized flame. Initial conditions: $\text{H}_2 = 39.7\%$, $\text{O}_2 = 10.3\%$ with balance Ar at 4.75 kPa. Symbols: experimental data [43]; solid lines: the present model; dashed lines: Mueller et al. [1].

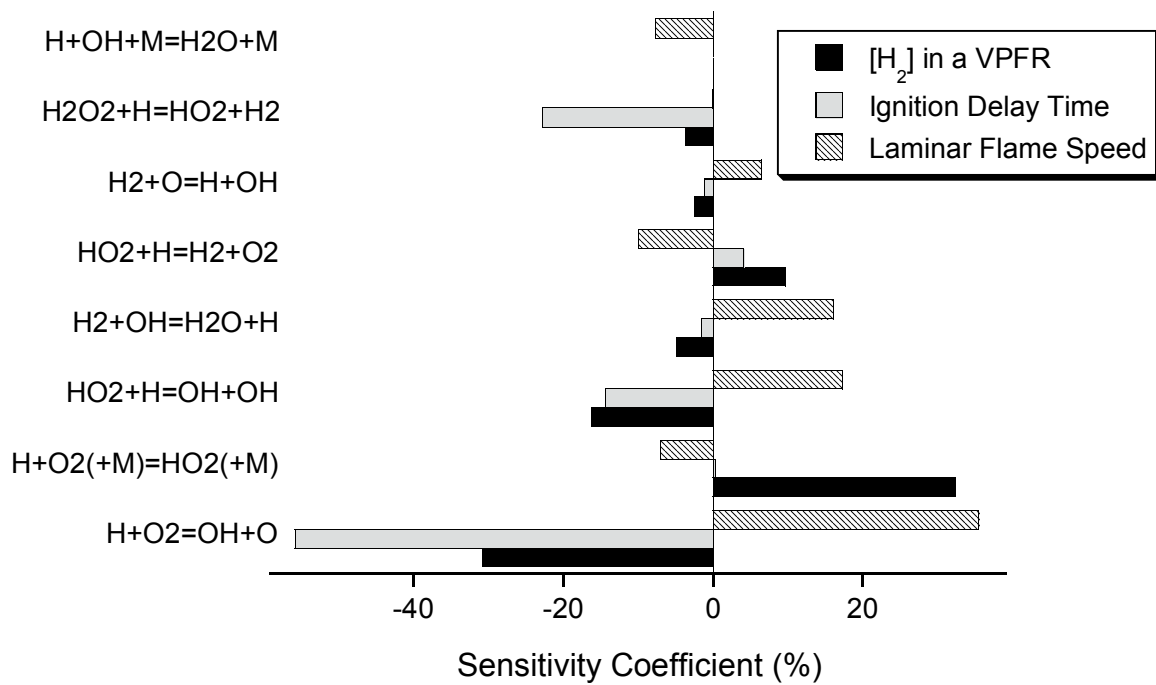


Figure 1.

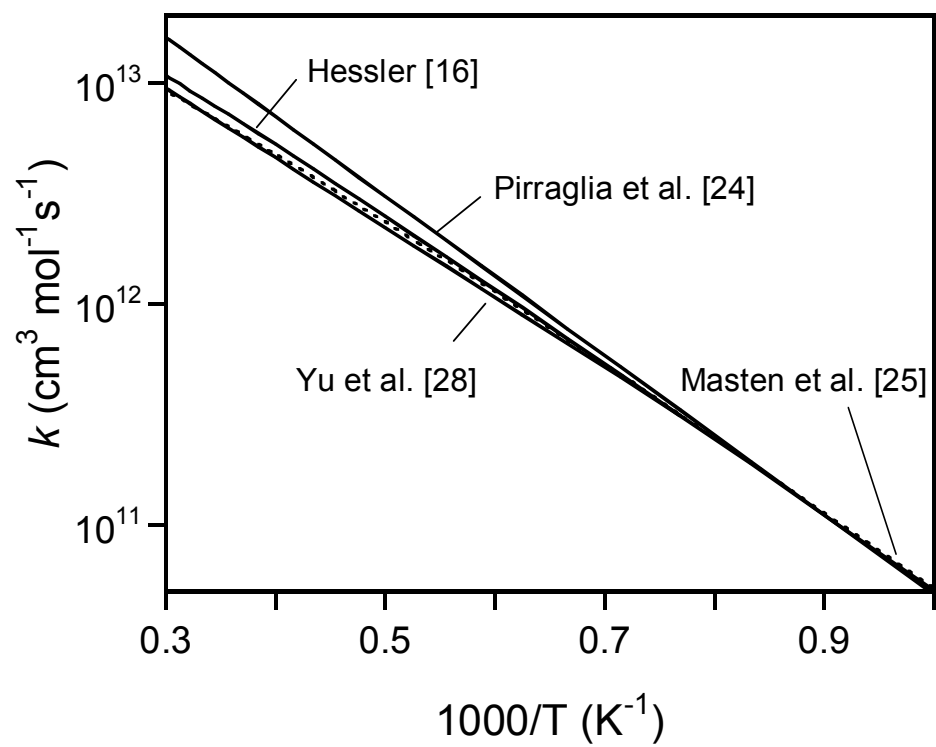


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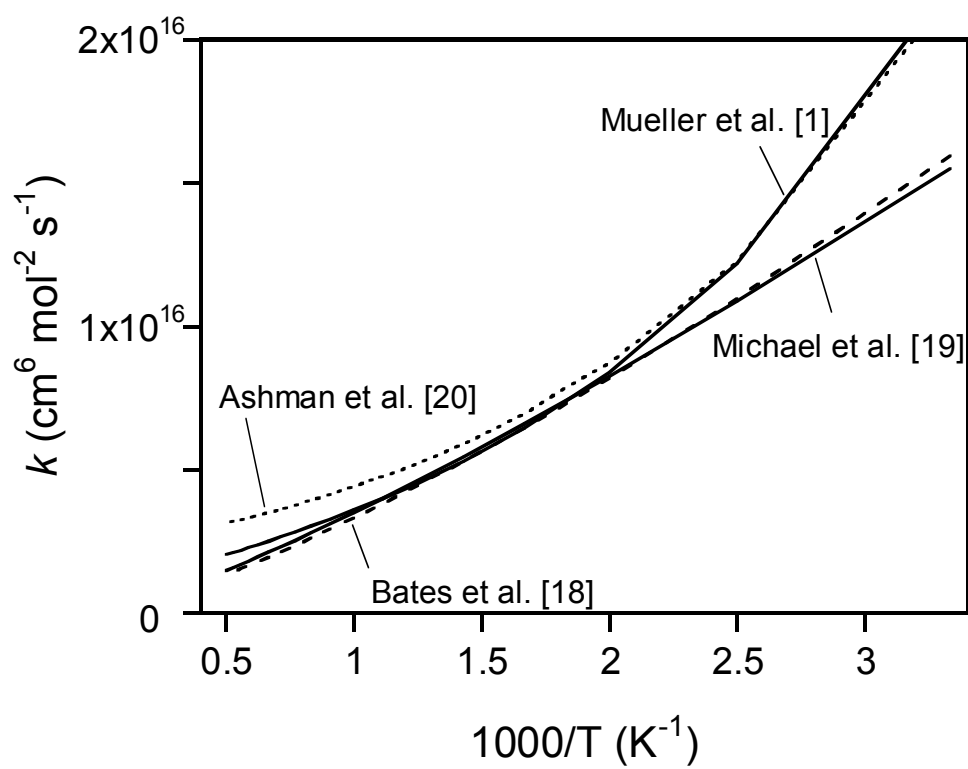


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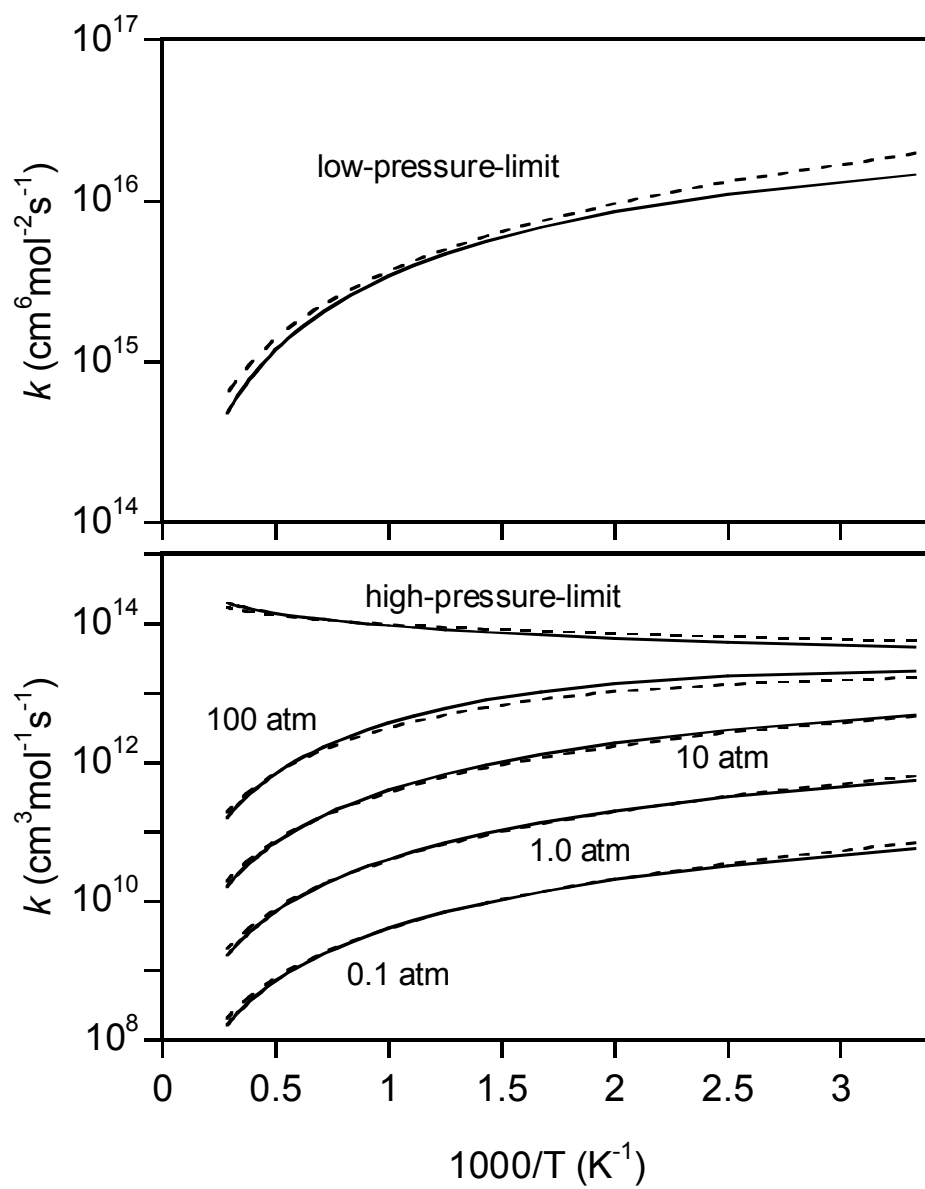


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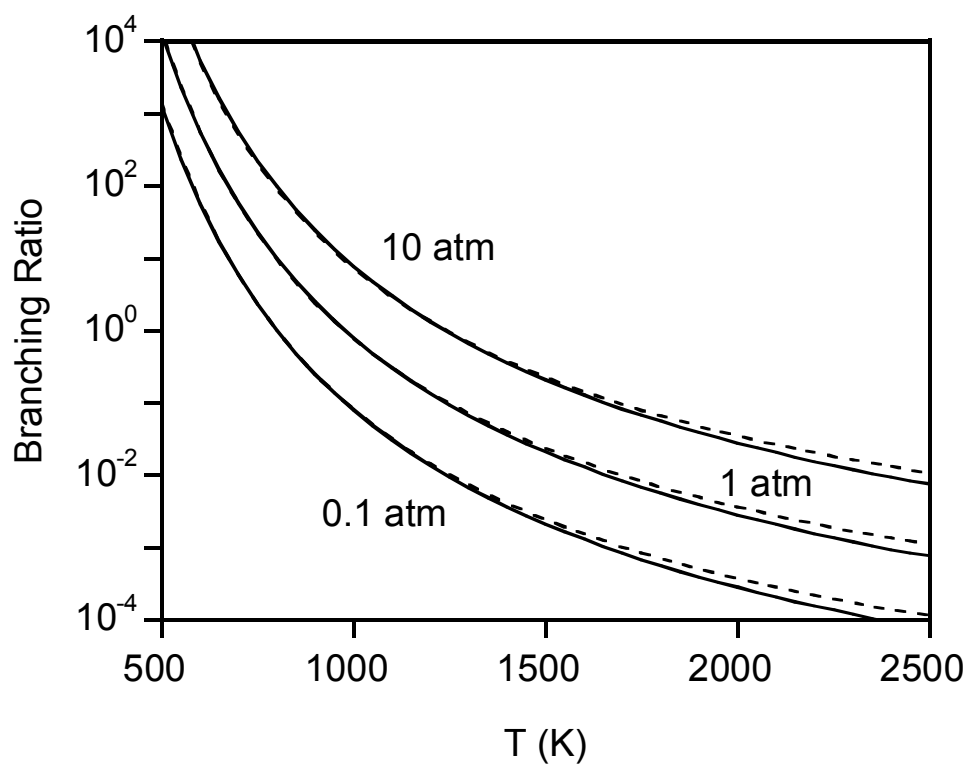


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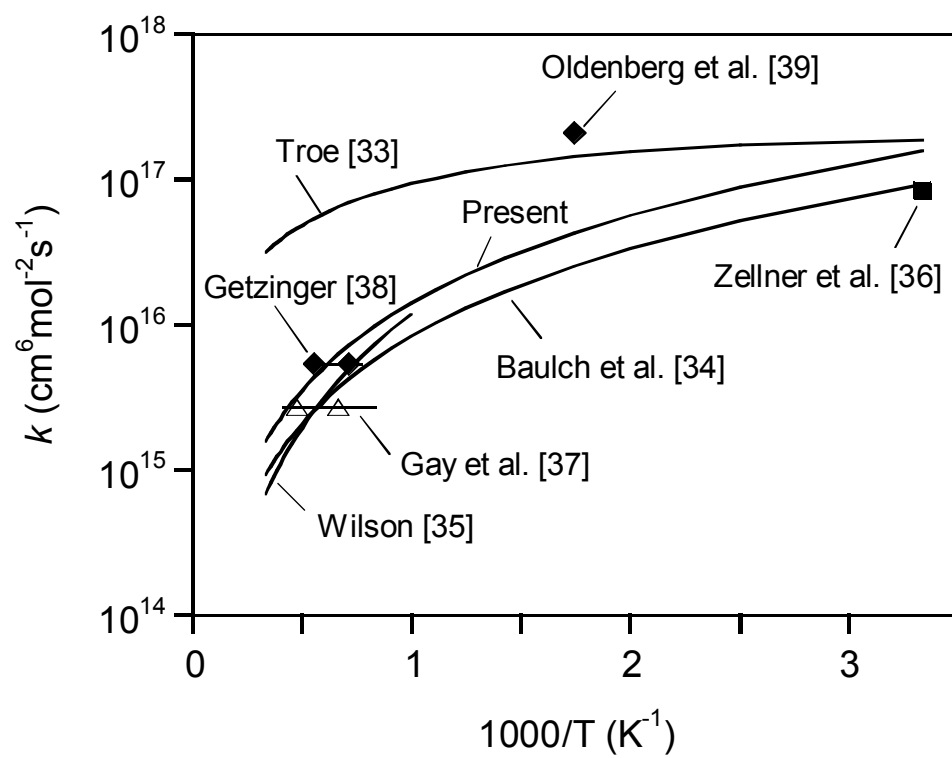


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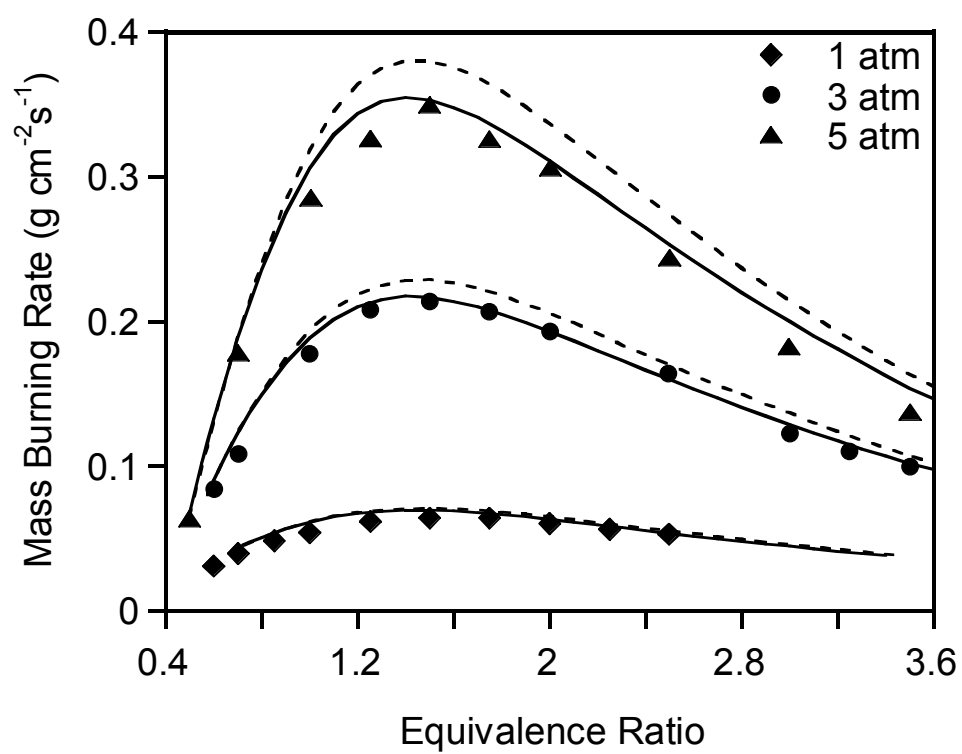


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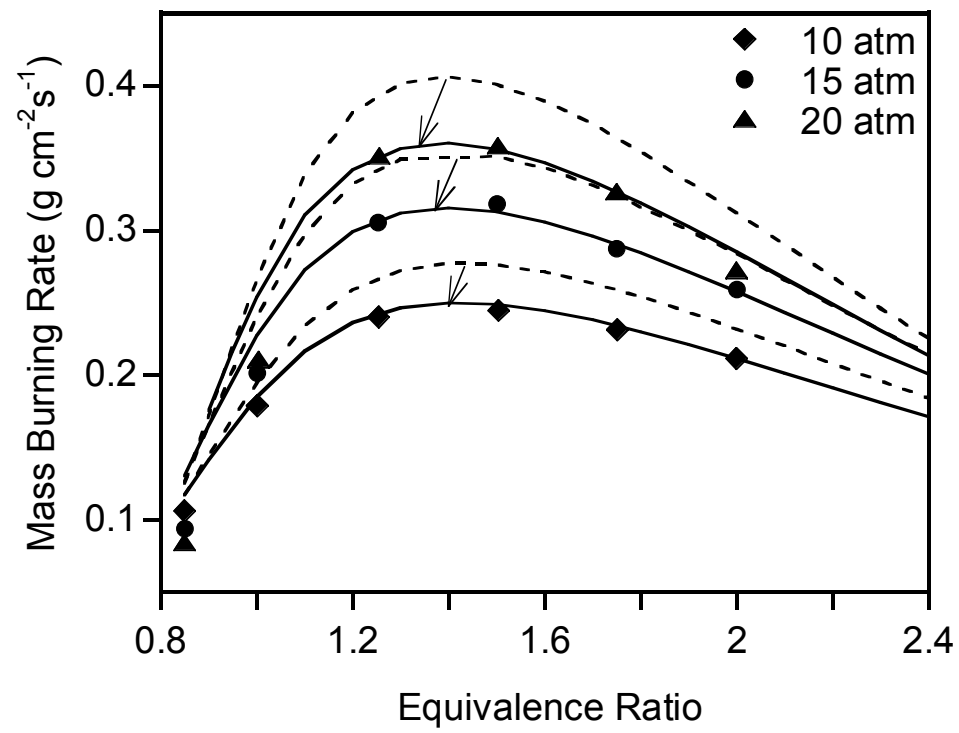


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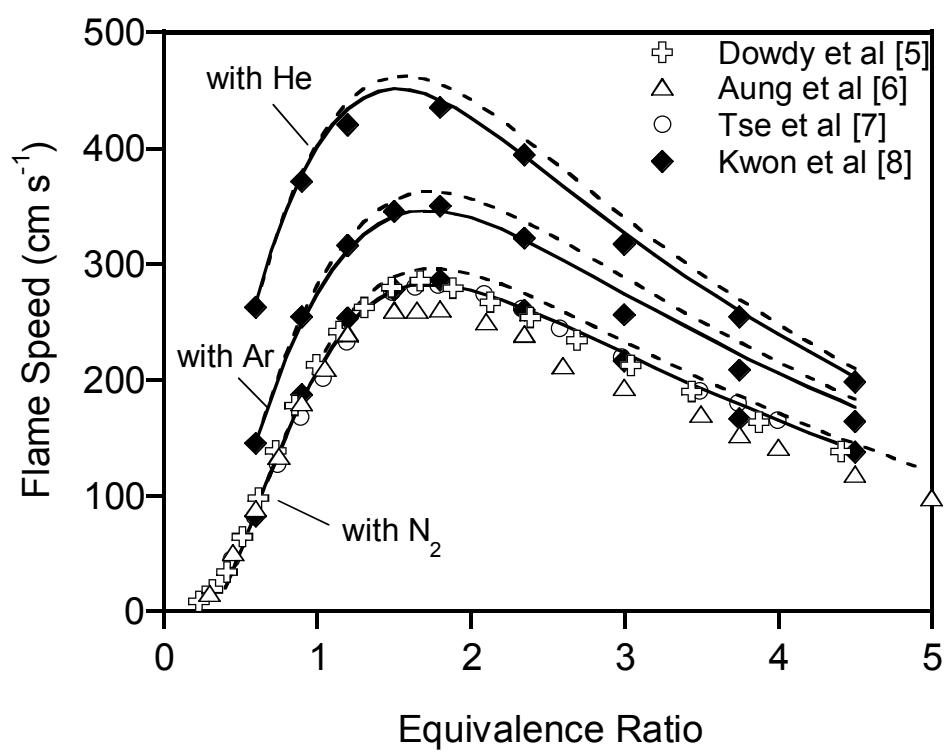


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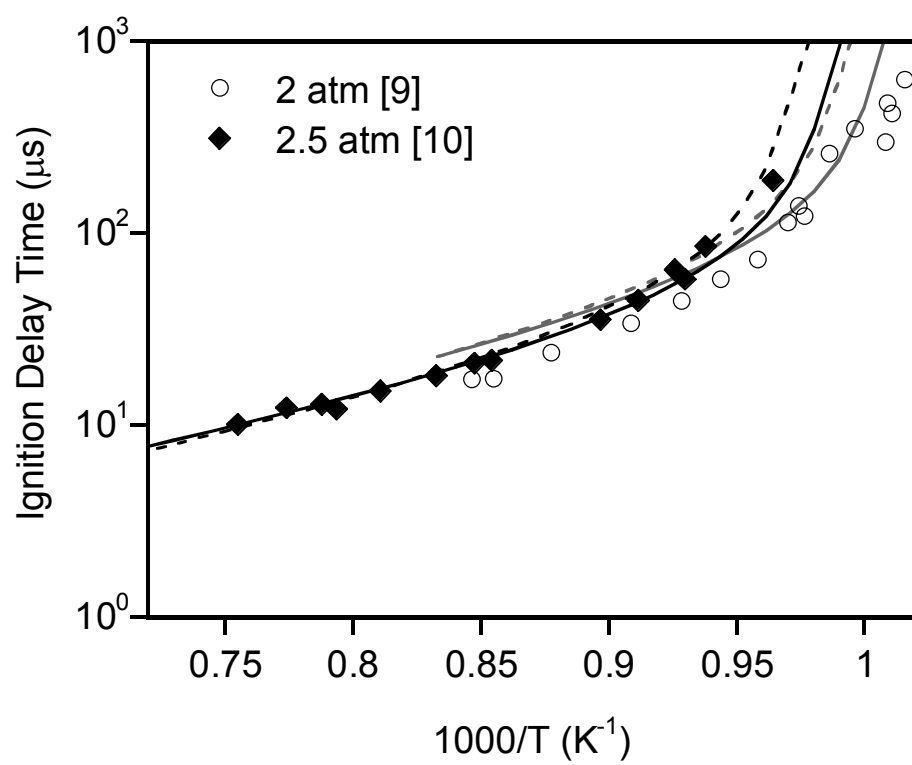


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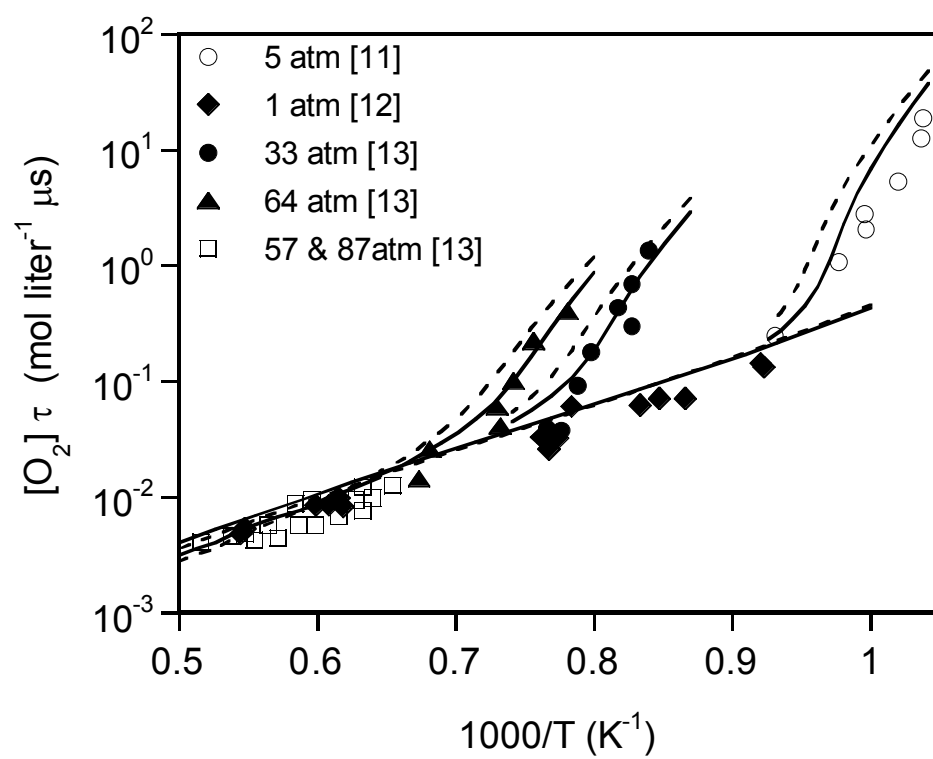


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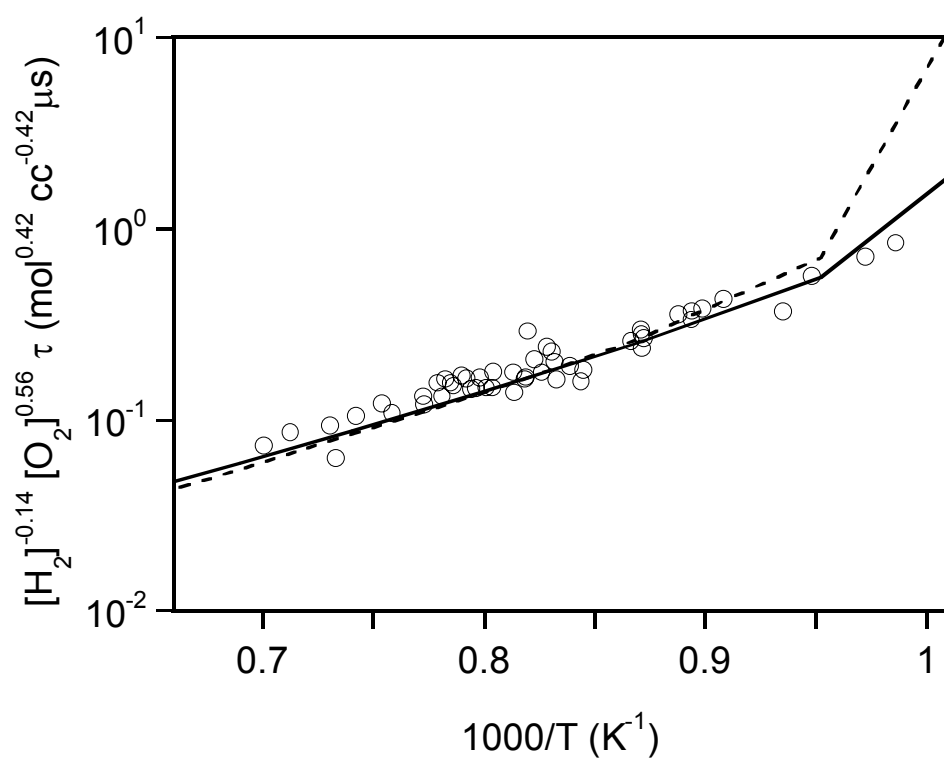


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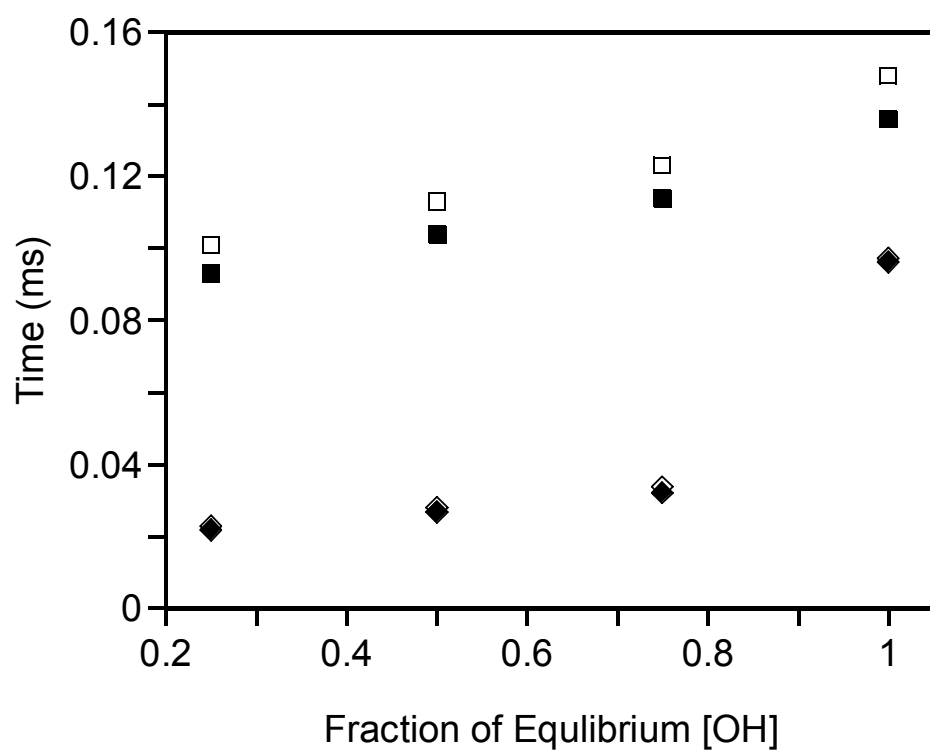


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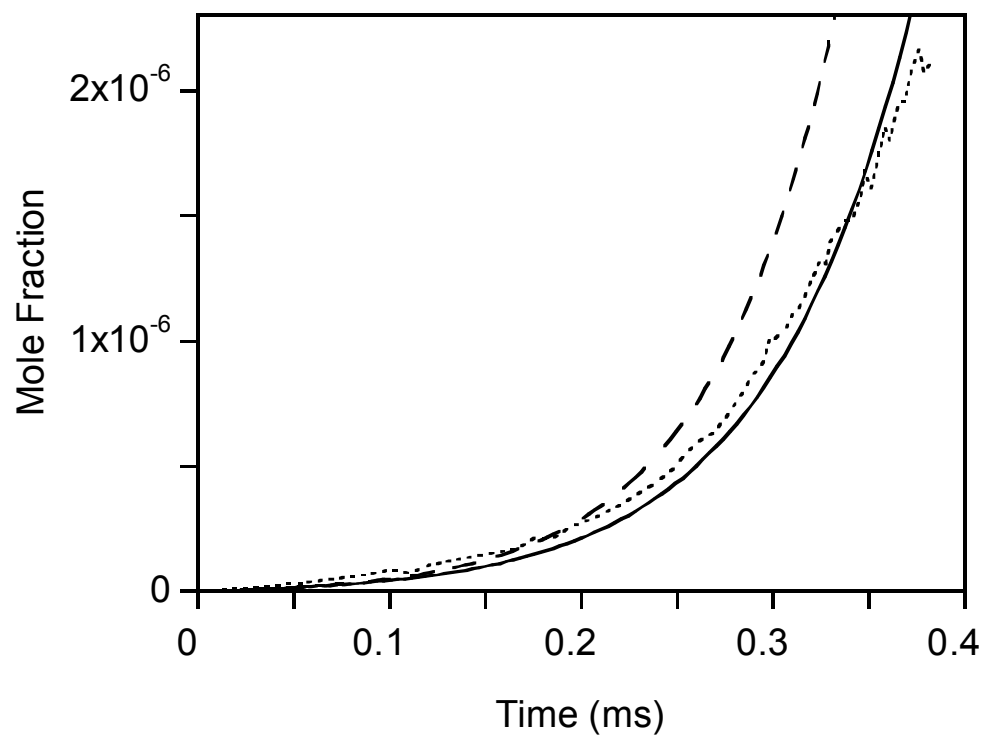


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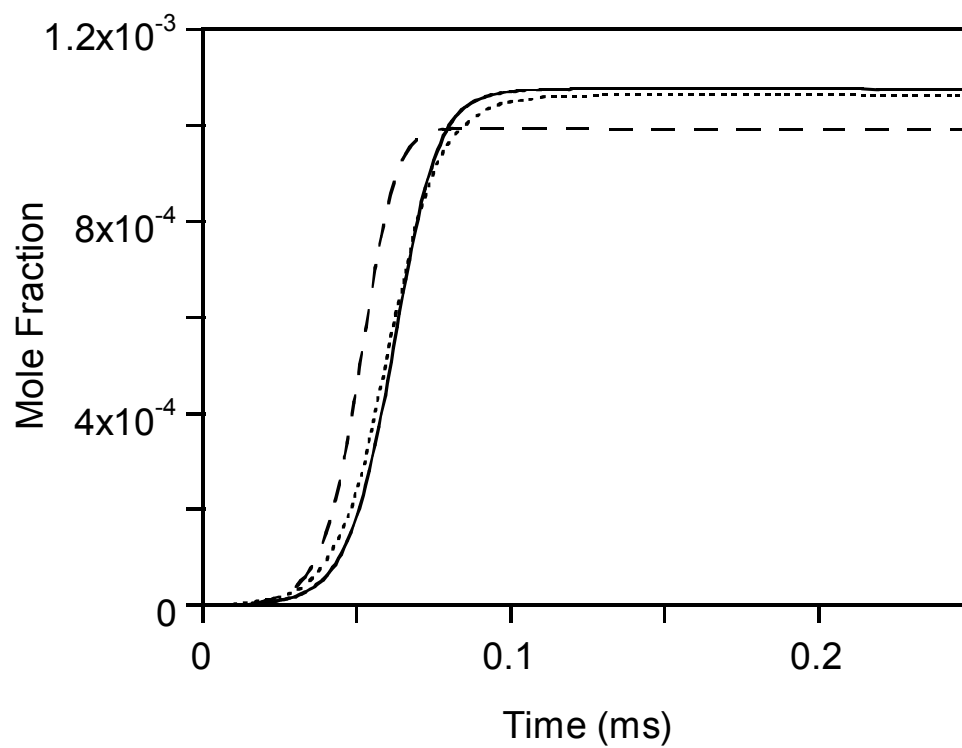


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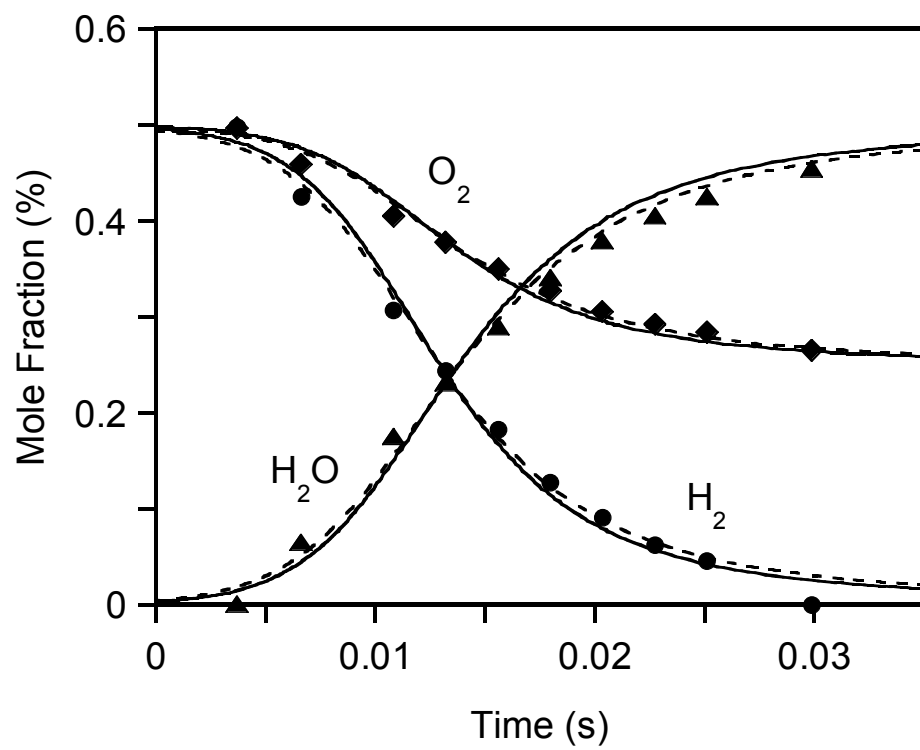


Figure 16.

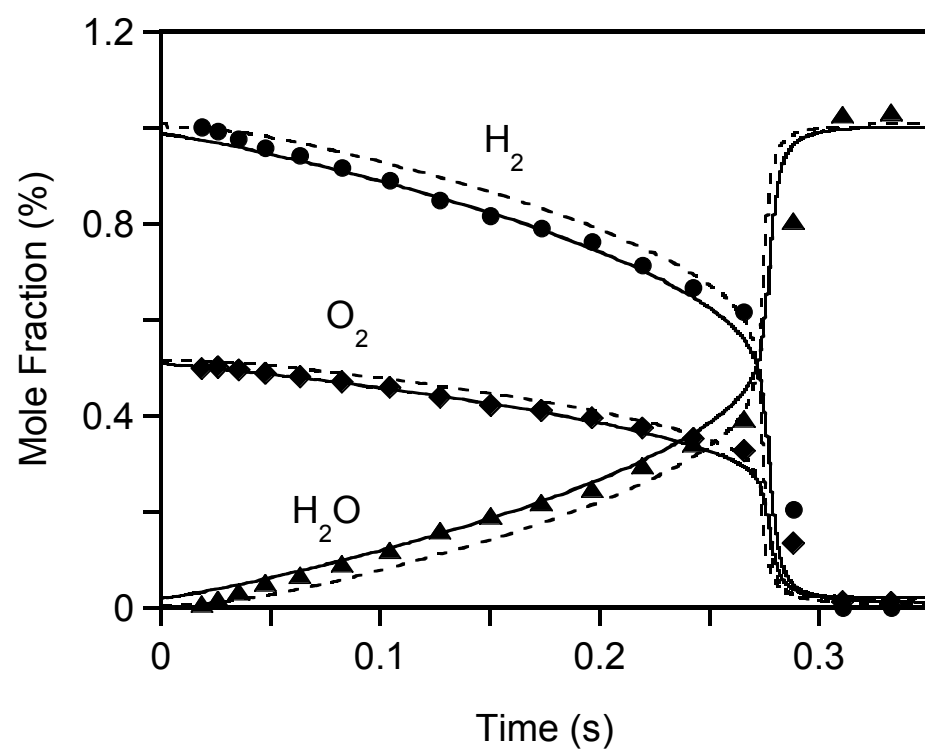


Figure 17.

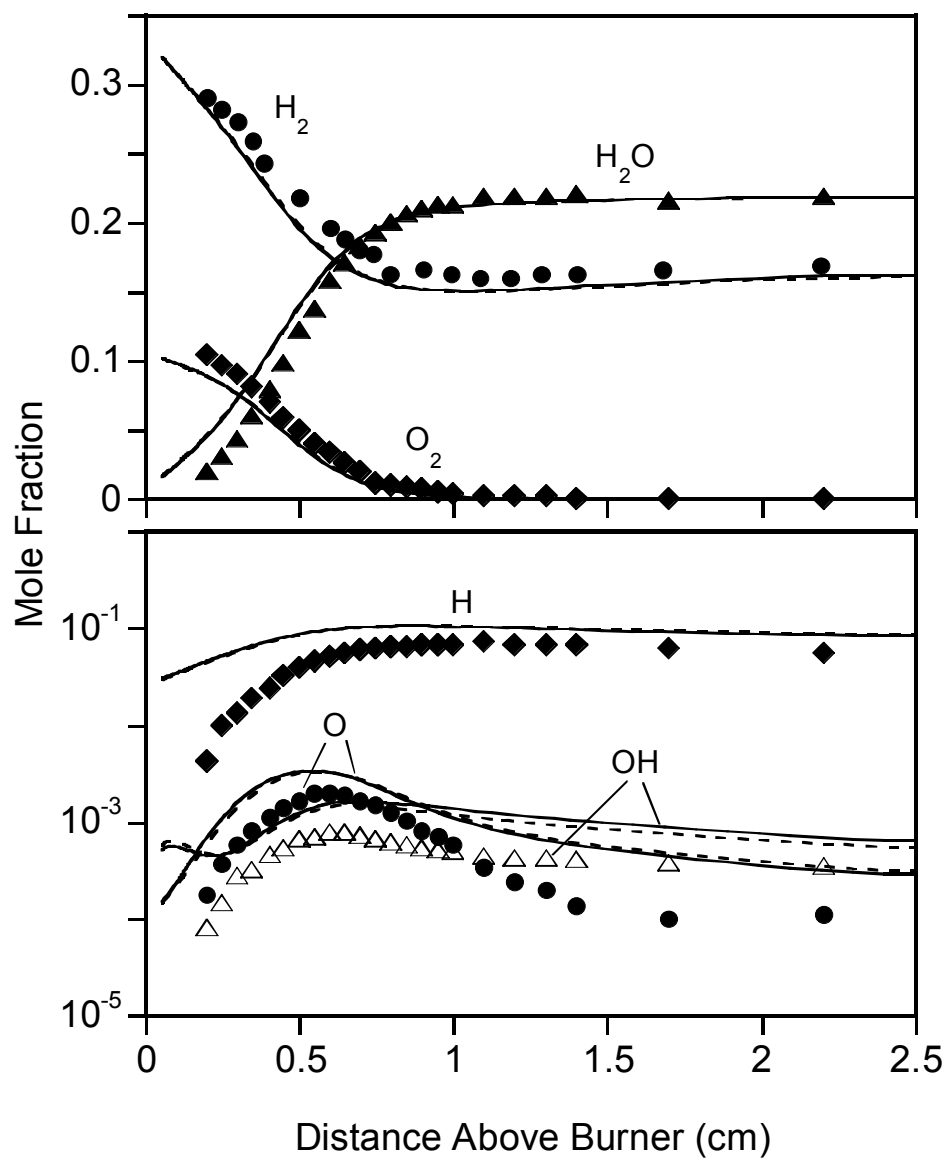


Figure 18.