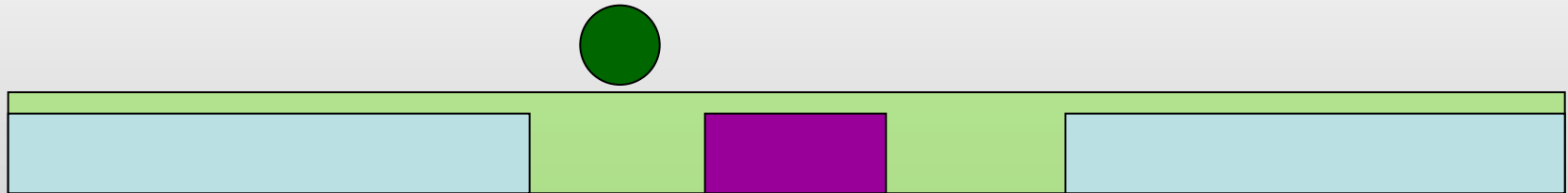


Circuit QED with electrons on helium:



What's the sound of one electron clapping?



David Schuster
Yale (soon to be at U. of Chicago)

Yale:
Andreas Fragner
Rob Schoelkopf

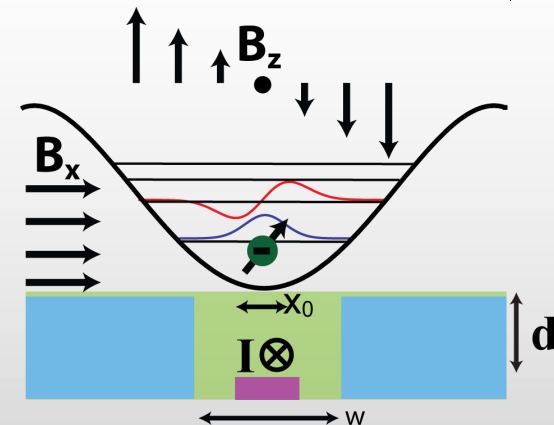
Princeton:
Steve Lyon

Michigan State:
Mark Dykman

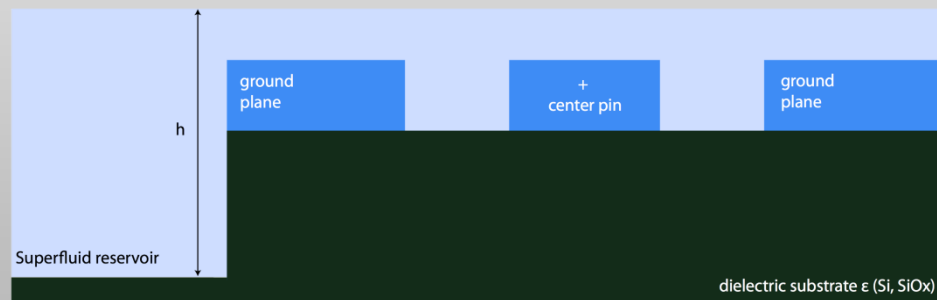
Useful cryogenics discussions: Mike Lea / David Rees

Outline

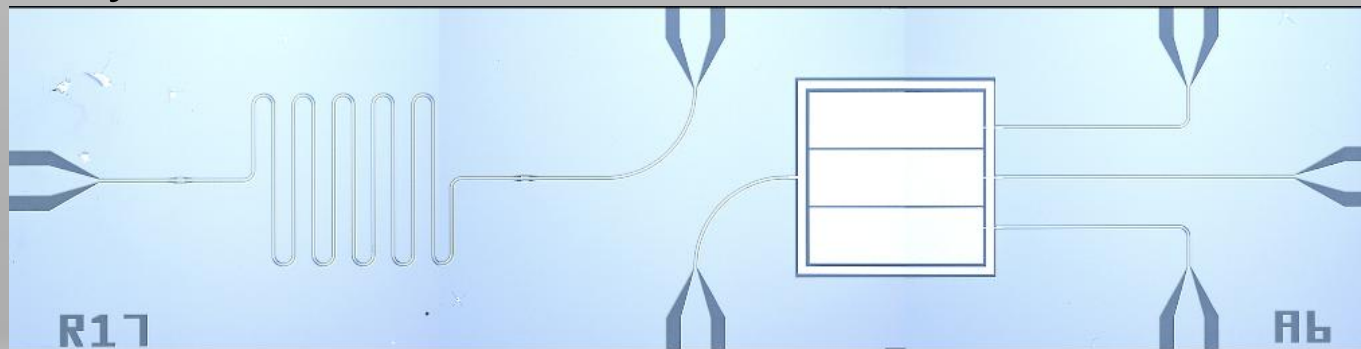
- Circuit QED with electrons on helium



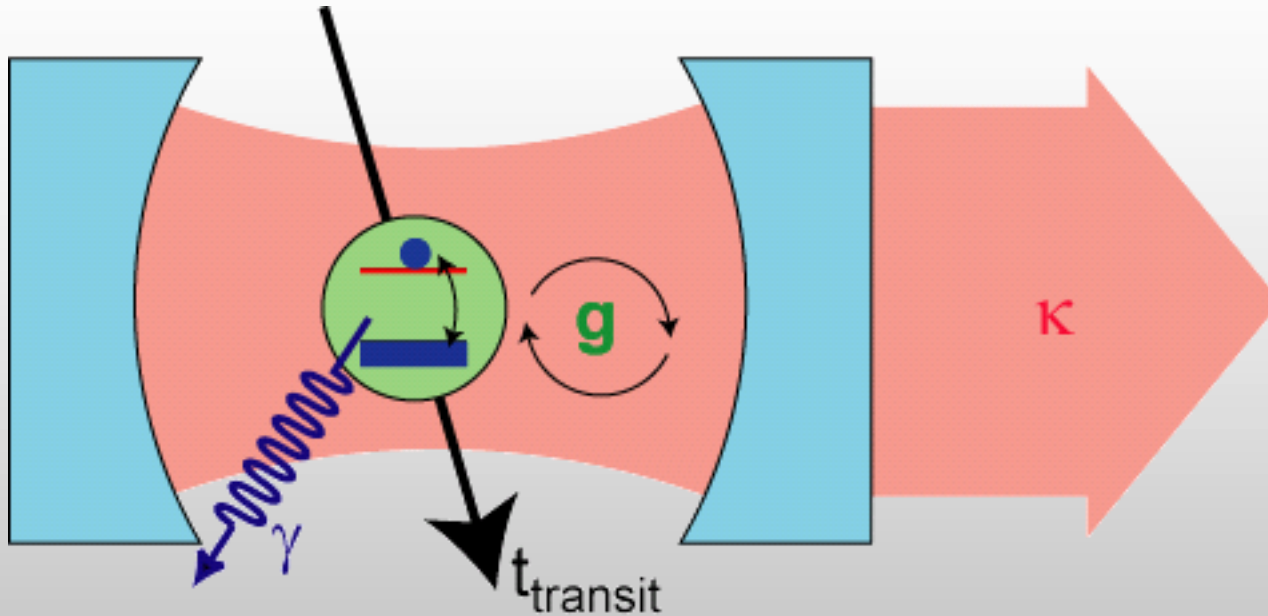
- Super-sensitive level meter



- Some preliminary measurements



Cavity Quantum Electrodynamics (CQED)



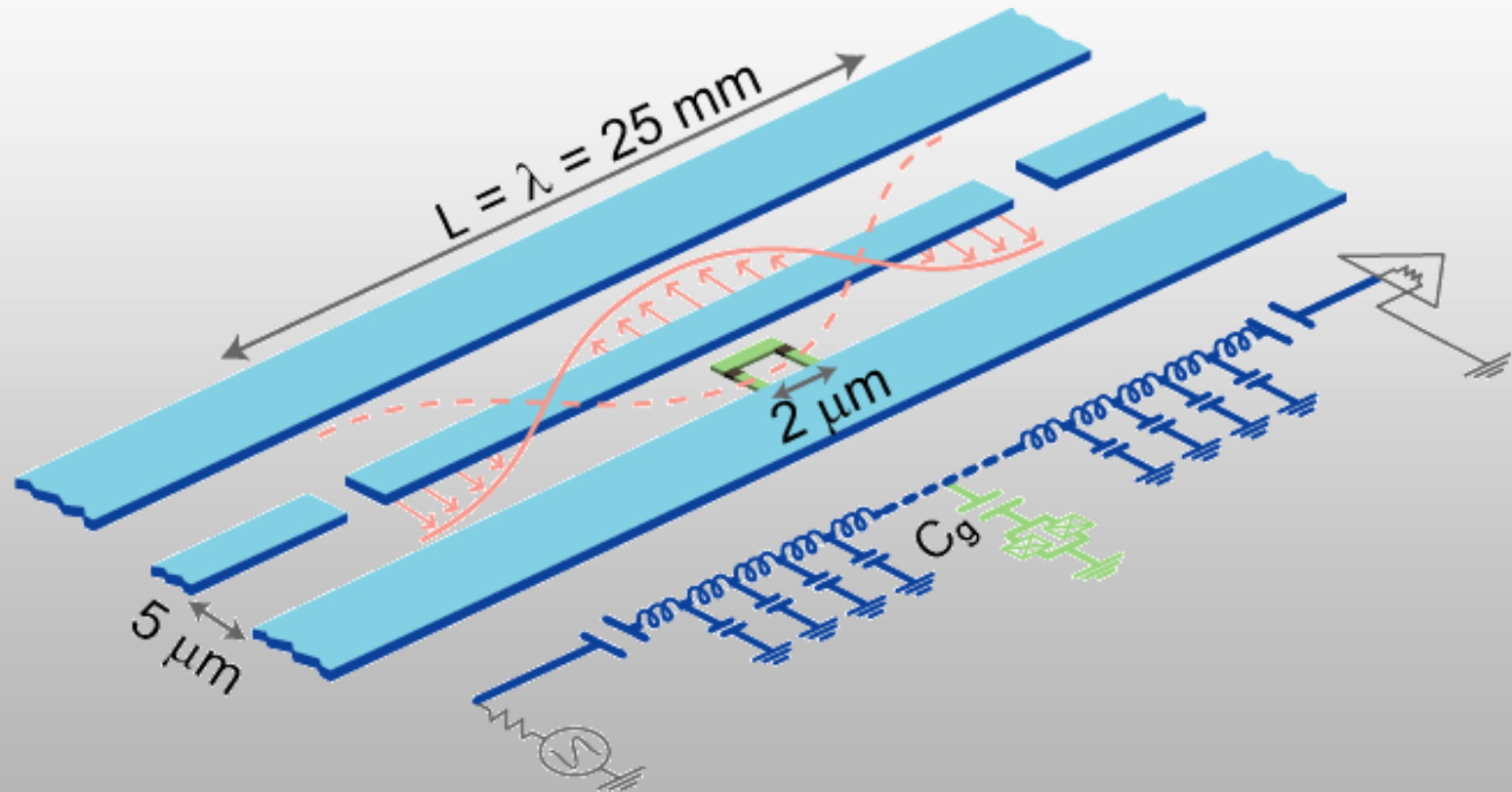
Jaynes-Cummings Hamiltonian

$$H = \hbar\omega_r \left(a^\dagger a + \frac{1}{2} \right) + \frac{\hbar\omega_a}{2} \sigma^z + \hbar g (a^\dagger \sigma^- + a \sigma^+) + H_\kappa + H_\gamma$$

strong coupling limit ($g = dE_0/\hbar > \gamma, \kappa, 1/t_{\text{transit}}$)

D. Walls, G. Milburn, Quantum Optics (Springer-Verlag, Berlin, 1994)

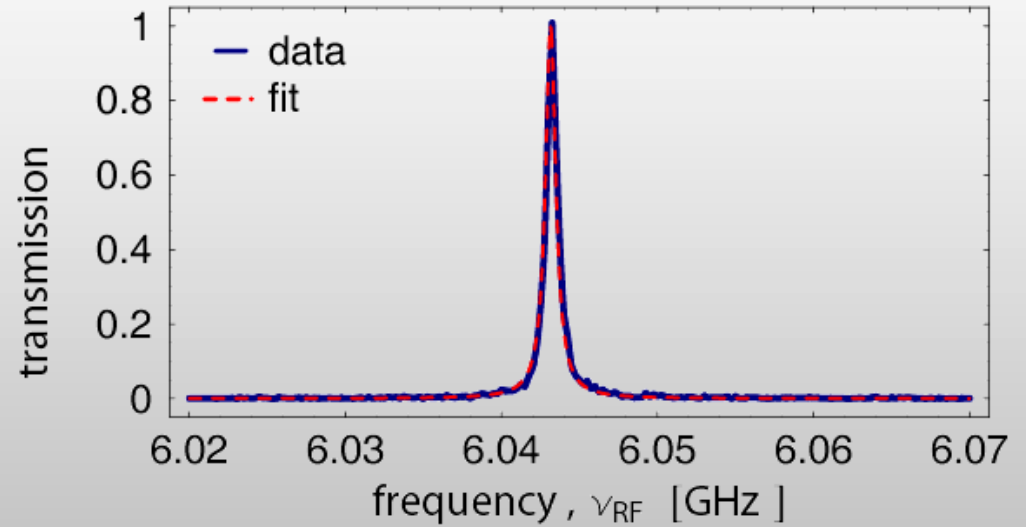
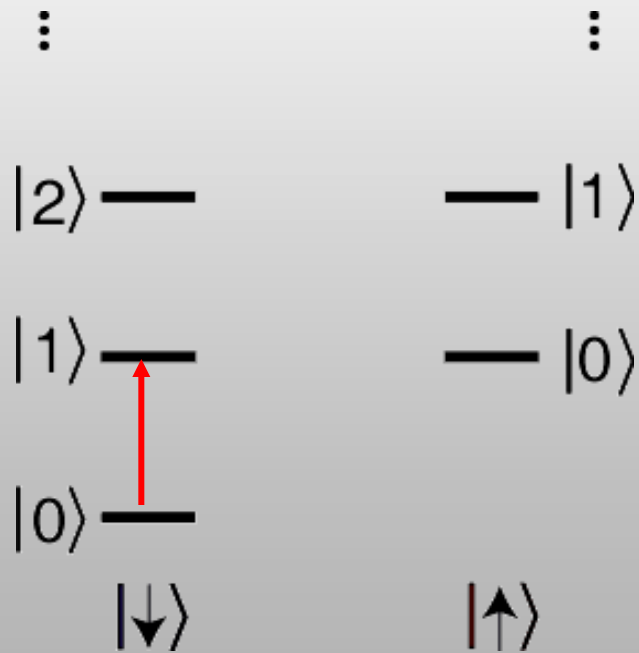
Circuit Quantum Electrodynamics



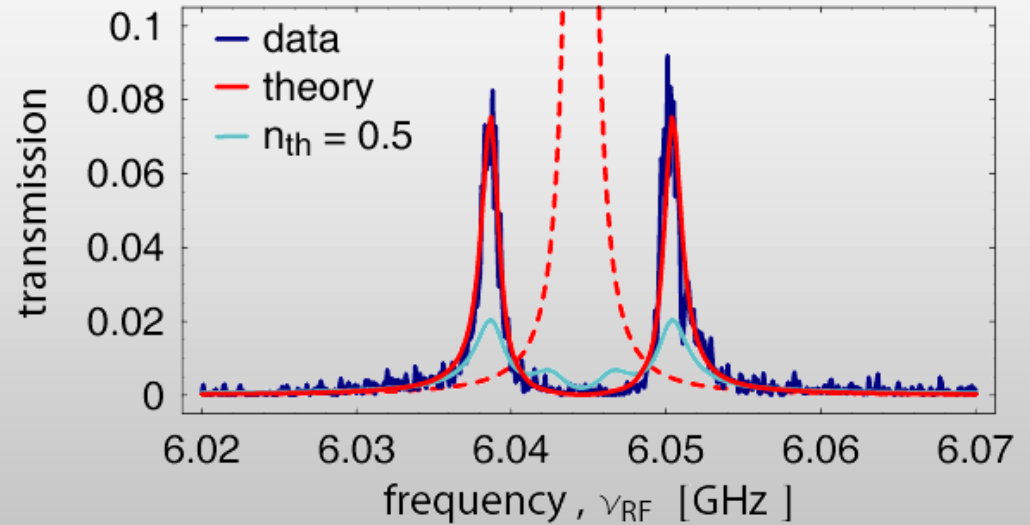
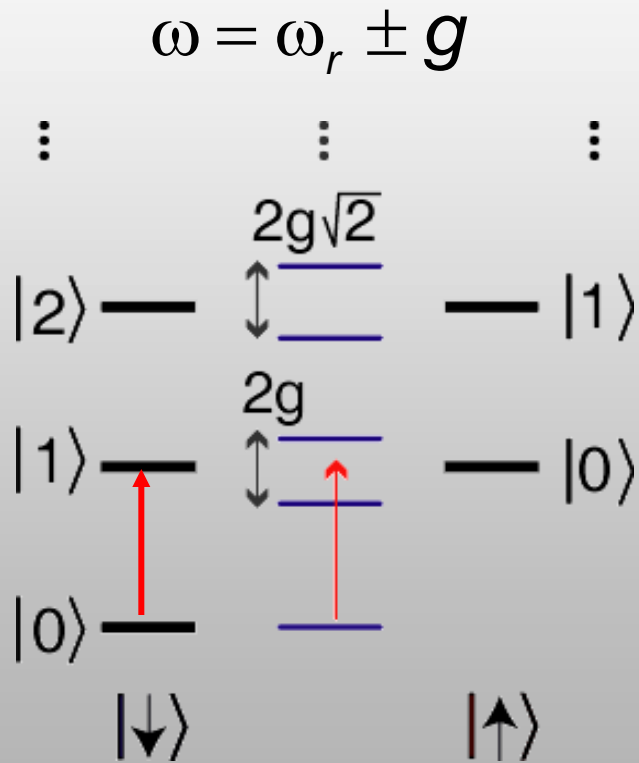
elements

- the cavity: a superconducting 1D transmission line resonator (large E_0)
- the artificial atom: a Cooper pair box (large d)

Strong coupling cavity QED!



Strong coupling cavity QED!



$$\omega / 2\pi = 6 \text{ GHz}$$

$$2g / 2\pi = 12 \text{ MHz}$$

$$\kappa / 2\pi \approx \gamma / 2\pi = 200 \text{ kHz}$$

$$C = \frac{g^2}{\kappa\gamma} = 3600$$

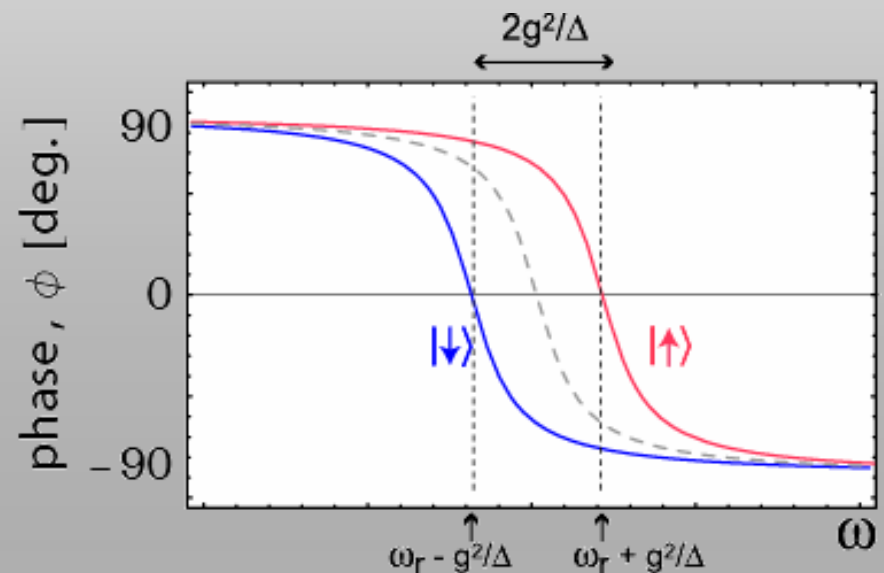
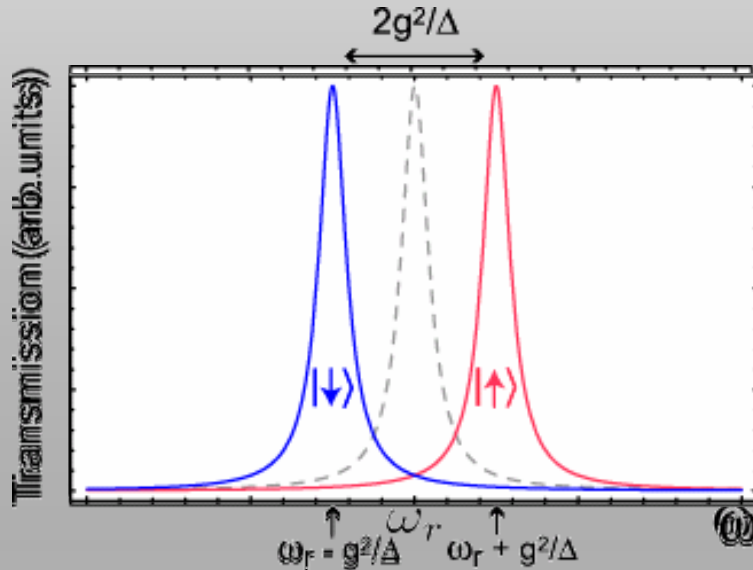
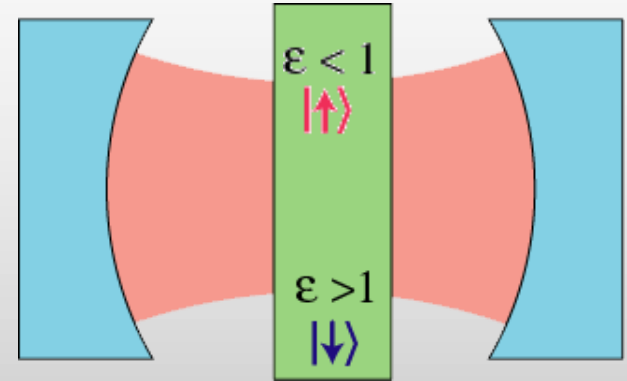
Non-Resonant Qubit Read-Out

approximate diagonalization for $|\Delta| = |\omega_a - \omega_r| \gg g$

$$H \approx \hbar \left(\omega_r + \frac{g^2}{\Delta} \sigma_z \right) a^\dagger a + \frac{1}{2} \hbar \left(\omega_a + \frac{g^2}{\Delta} \right) \sigma_z$$

//
cavity frequency shift
and qubit ac-Stark shift

//
Lamb shift



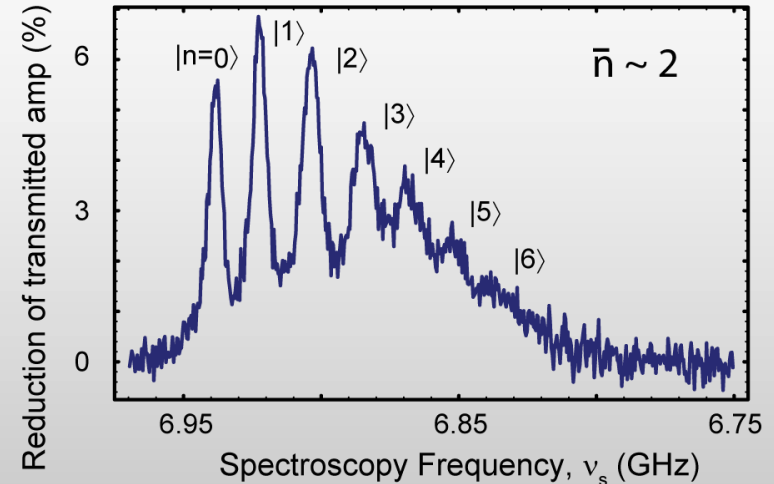
Circuits make good atoms/qubits

Photon number detection

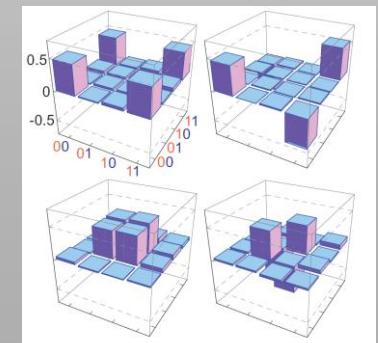
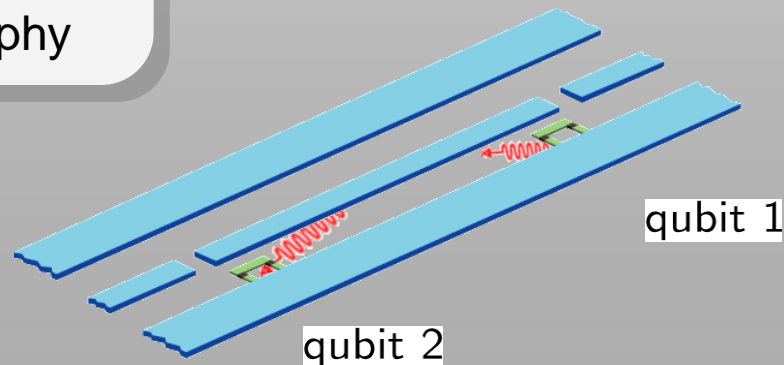
- ✧ QND detection of photons
- ✧ Qubit / photon gates
- ✧ Non-linear optics

Coupled qubits

- ✧ Two qubit gates
- ✧ Quantum algorithms
- ✧ Process tomography

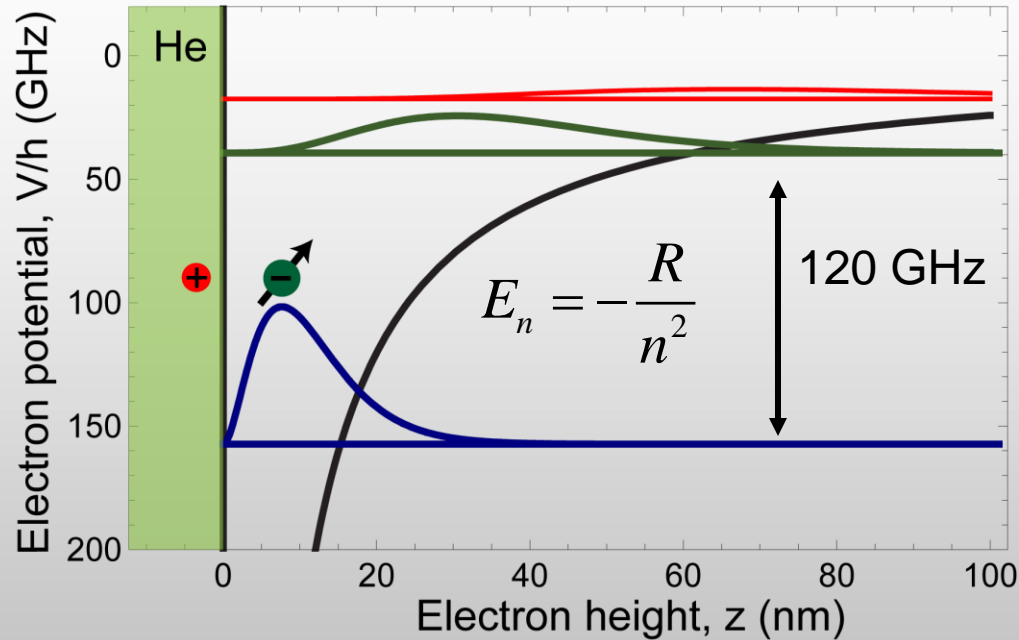


Schuster, Houck, et al., *Nature*, 2007



DiCarlo, Chow, et. al.,
Nature, 2009

Electrons on helium

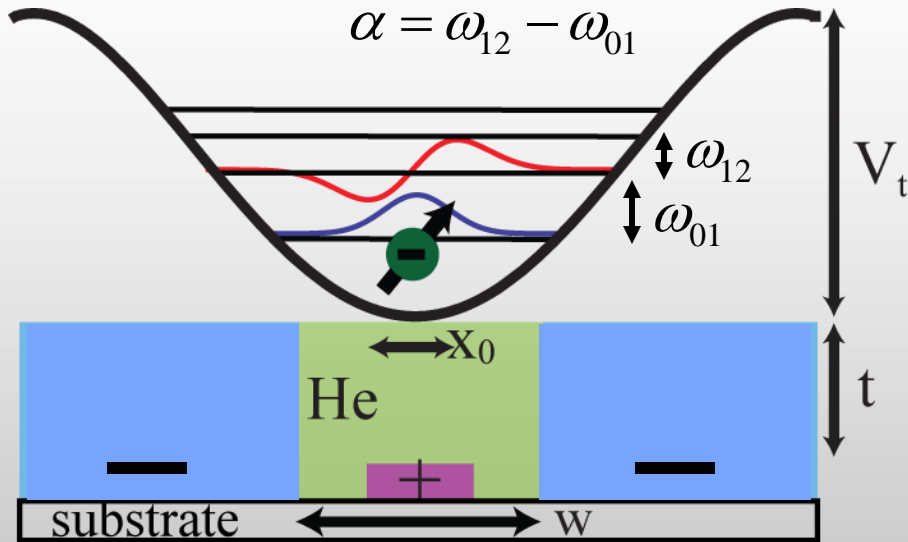


- ✧ Reduced H spectrum
- ✧ Potential well depth $\sim R = 8$ K
- ✧ “Bohr” radius 8 nm above surface

- ✧ Clean 2DEG (Mobility = 10^{10} cm²/Vs)
- ✧ Bare electron: $m_{\text{eff}} = 1.005 m_e$, $g = 2$
- ✧ <1 ppm ^3He nuclear spins
Bulk spin coherence time > 50 ms*

QC Proposal w/ vertical states: Dykman, Science 1999

An electron in an anharmonic potential



$$\frac{eV_t}{h} = 150 \text{ GHz}$$

$$w = 1 \mu\text{m}$$

$$t = 1 \mu\text{m}$$

$$\frac{\omega_{01}}{2\pi} \sim 10 \text{ GHz}$$

$$\frac{\alpha}{2\pi} \sim 100 \text{ MHz}$$

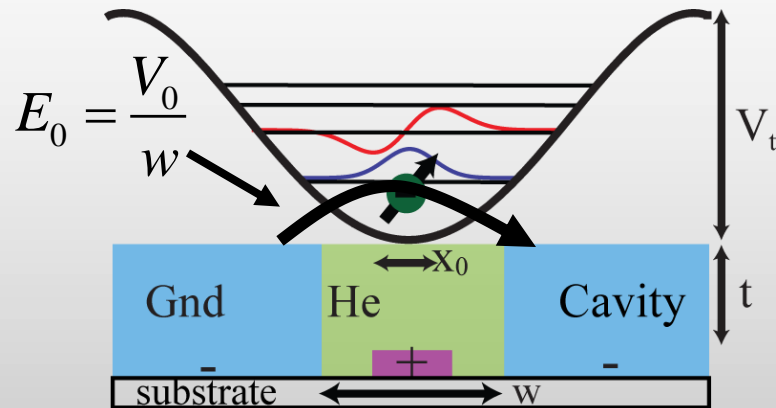
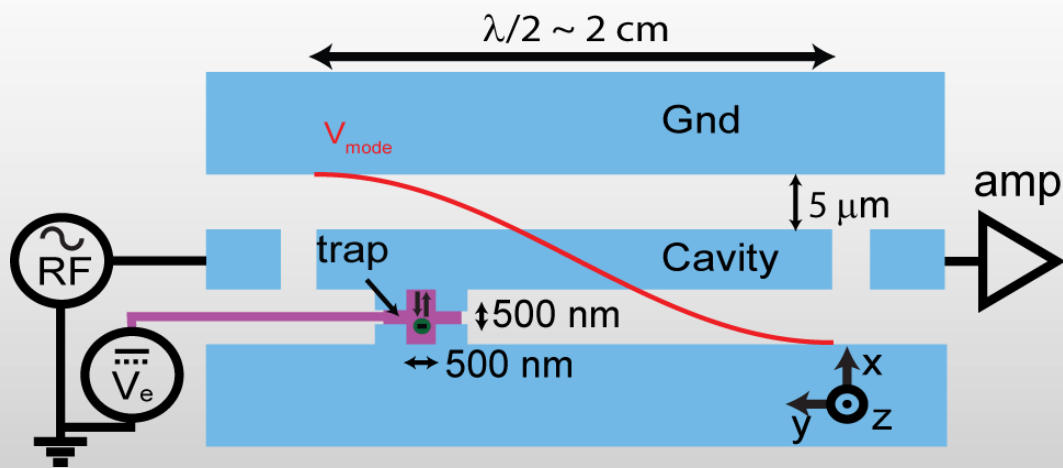
$$x_0 \sim 30 \text{ nm}$$

Big dipole moment!

$$\sim 1000D$$

- ✧ DC electrodes to define trap for **lateral** motion
- ✧ Nearly harmonic motion with transitions at \sim GHz
- ✧ Anharmonicity from small size of trap ($\sim 1 \mu\text{m}$)

An electron in a cavity

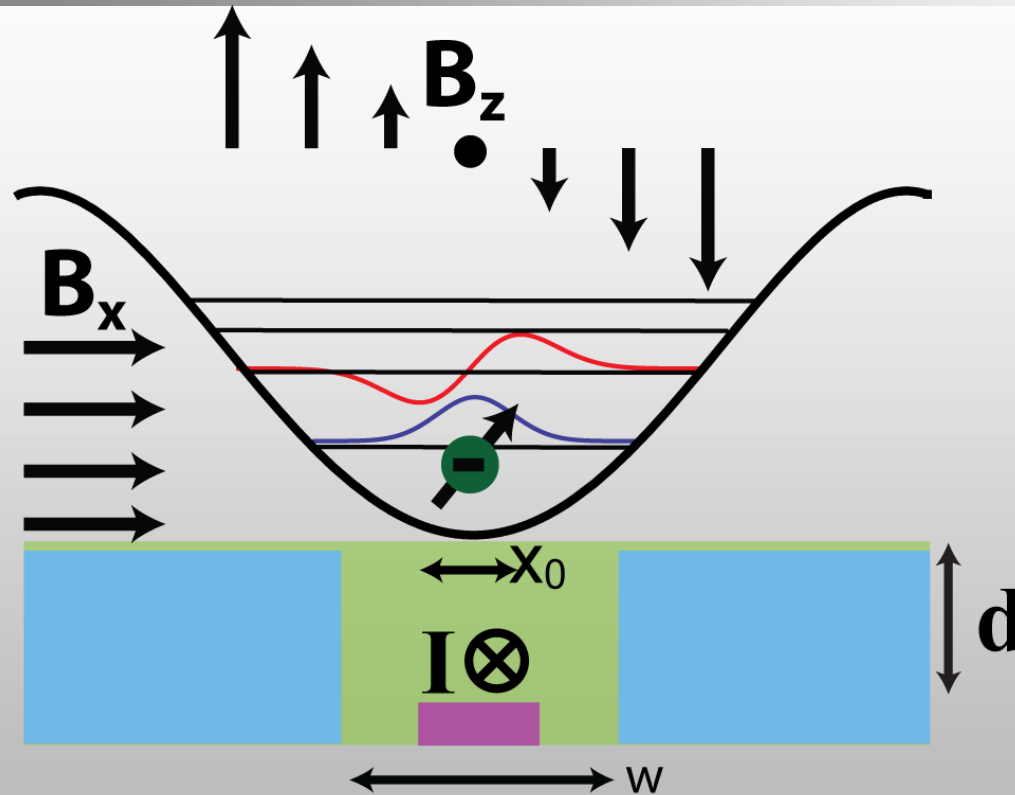


- ✧ Electron motion couples to cavity field
- ✧ Can achieve strong coupling limit of cavity QED
- ✧ Couple to other qubits through cavity bus

Cavity-electron coupling

$$\hbar g \sim e x_0 \frac{V_0}{w} \sim h \times 25 \text{MHz}$$

Accessing spin: Gradient method

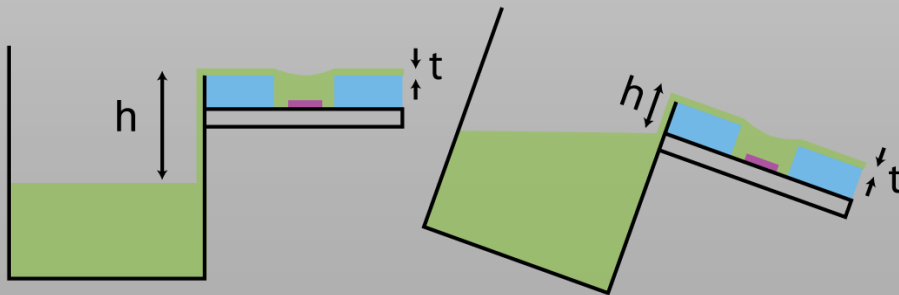
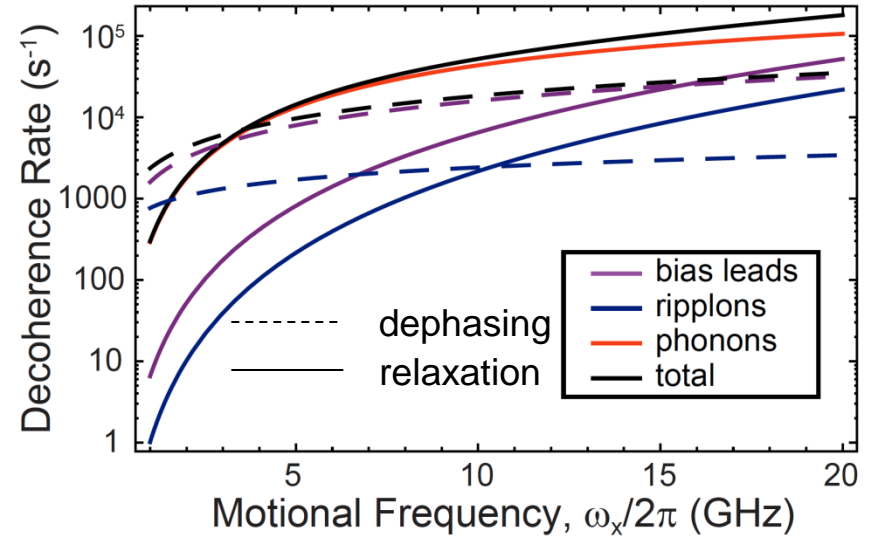


$$H_{sb} = -\mu_B \nabla \vec{B} \cdot \vec{S} \sim -\mu_B \Delta B_z \hat{\sigma}_x \hat{S}_x$$

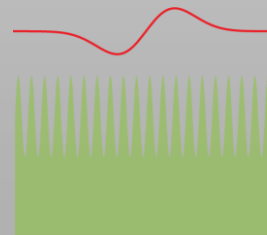
- ✧ Electrically tunable spin-motion coupling!
- ✧ With no flux focusing and current geometry: 100 kHz/mA

• Motional Decoherence

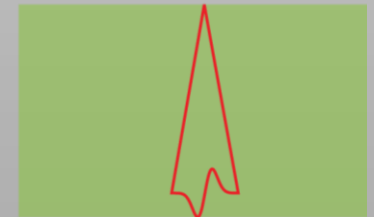
- ✧ Relaxation through bias electrodes
- ✧ Emission of (two) ripplons
- ✧ Emission of phonons



Classical helium fluctuations

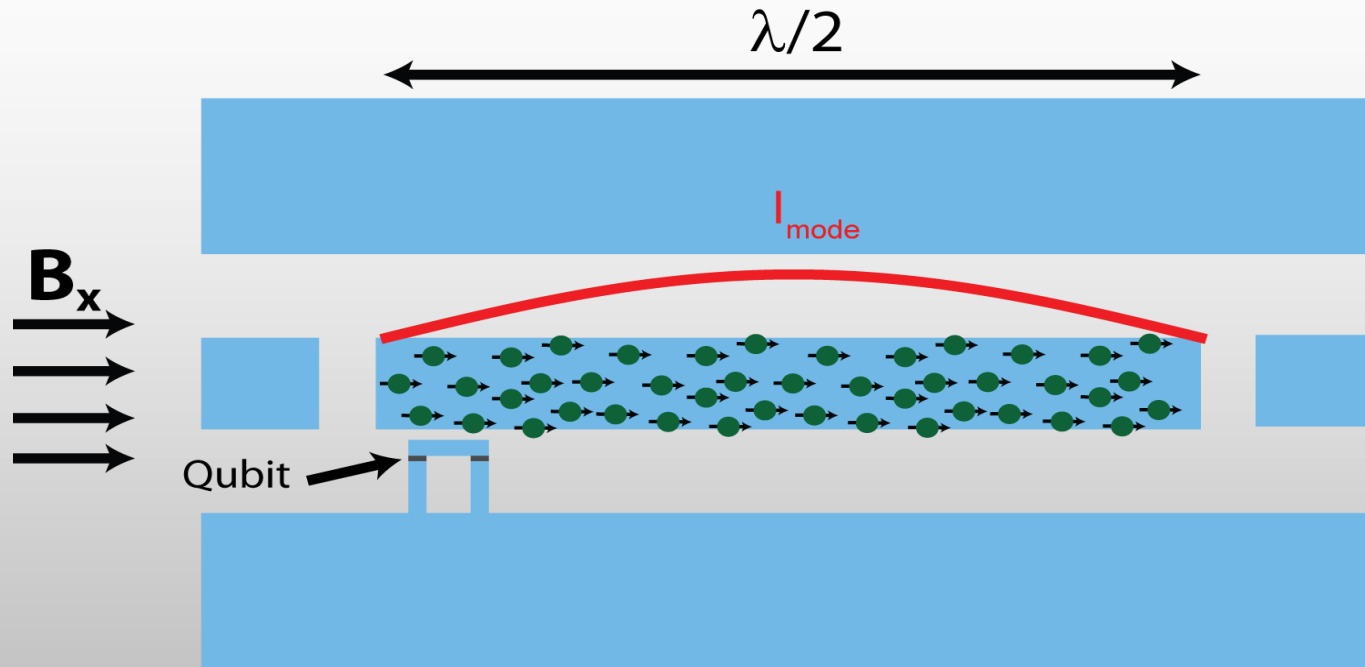


Ripplons



Phonons

eOnHe spin memory



- ✧ Put many electrons on top of the resonator.
- ✧ Spins coupled to resonator magnetic field.

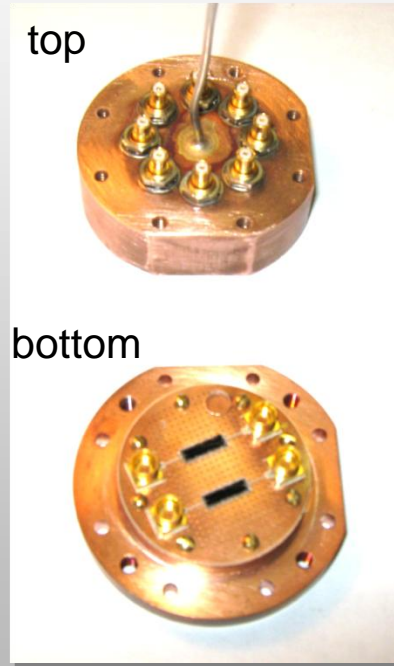
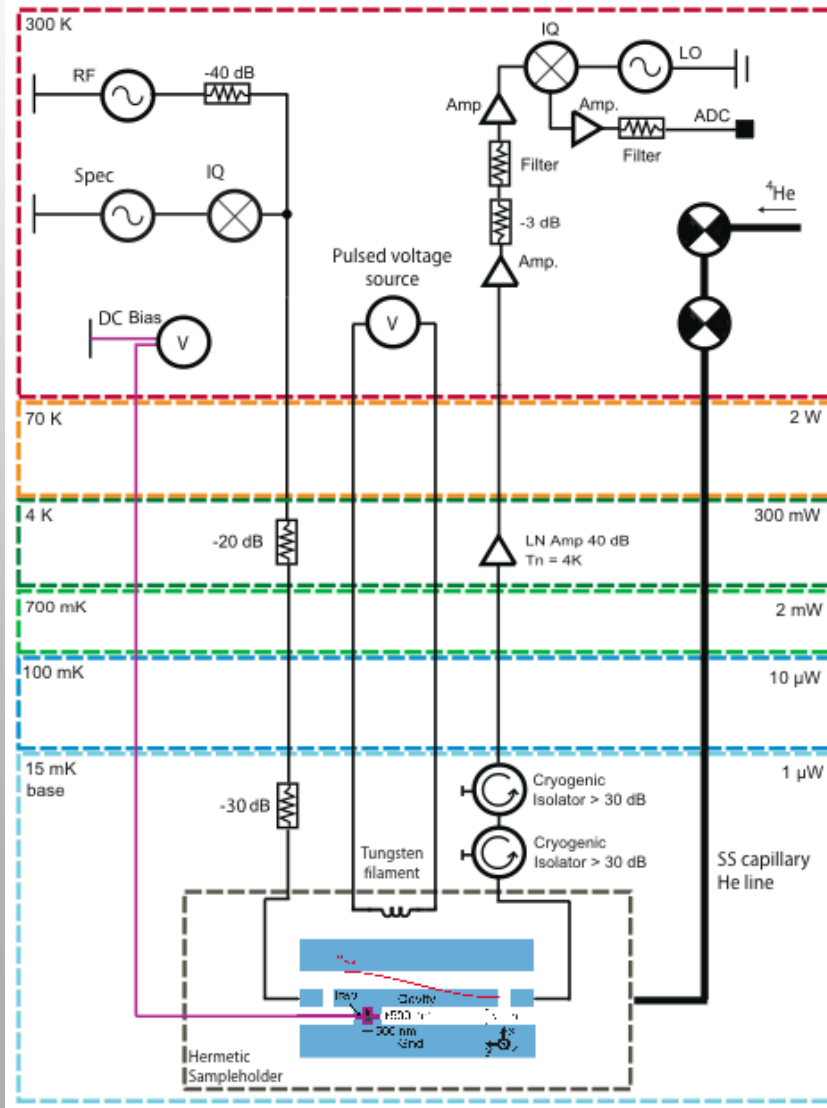
$$\frac{g}{2\pi} \sim 100\text{Hz} - 1\text{kHz}$$

$$\frac{g}{2\pi} \sqrt{M} \sim 10\text{kHz} - 100\text{kHz} \quad \text{with } \sim 10^4 \text{ spins}$$

Even basic ESR has never been done on eOnHe 2DEG!

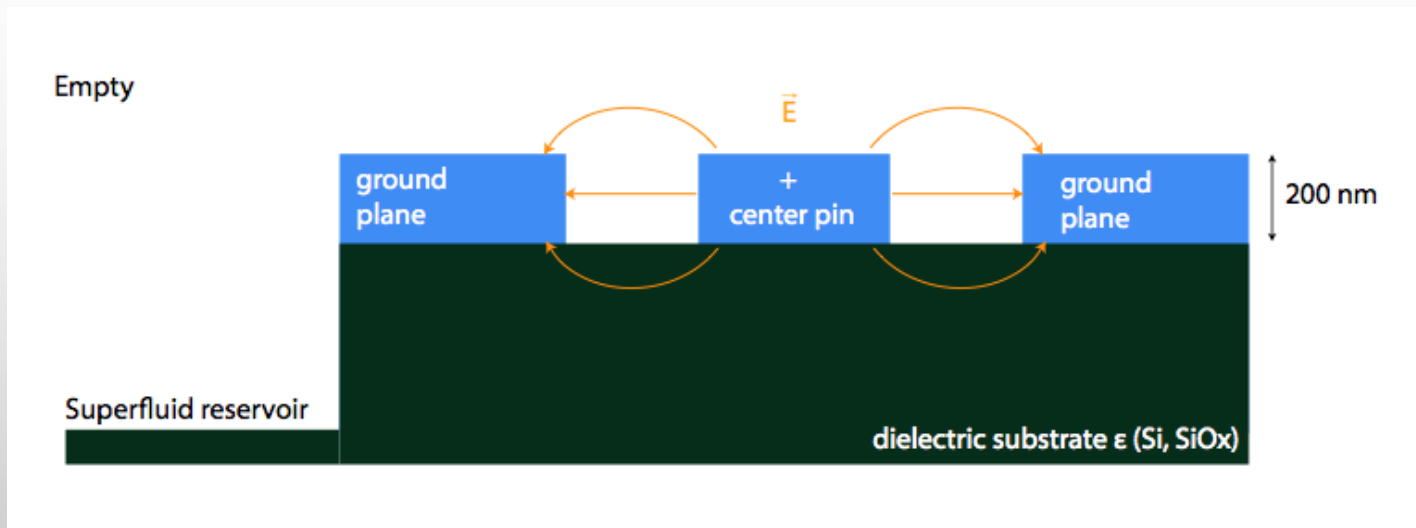
Experimental Setup

• Pulse-tube cooled dilution refrigerator

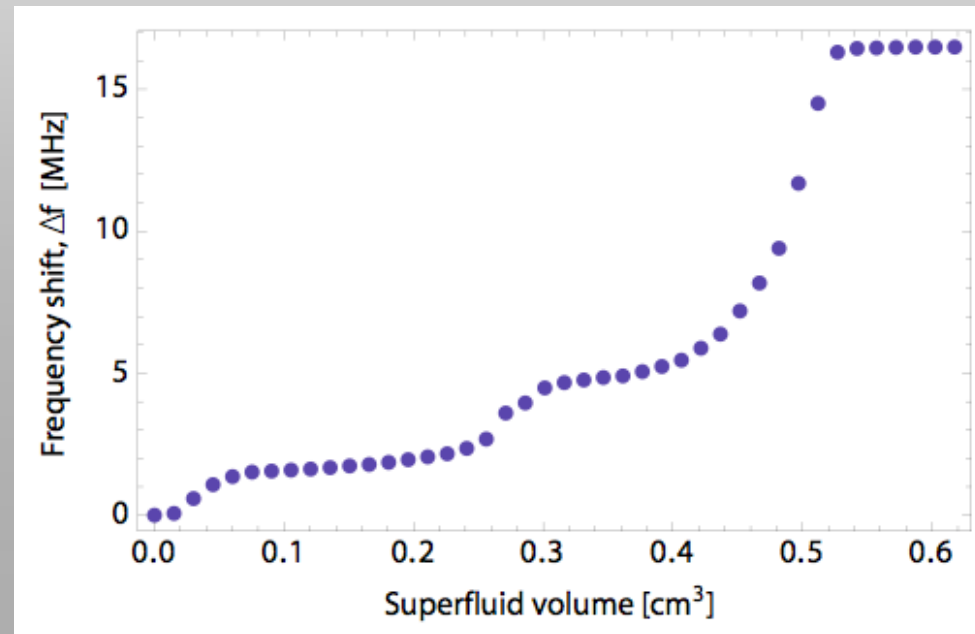


- hermetic sample holder with Indium sealing & stainless steel capillary
- no superfluid leaks down to 10mK

Superconducting Cavities as liquid He-Meters



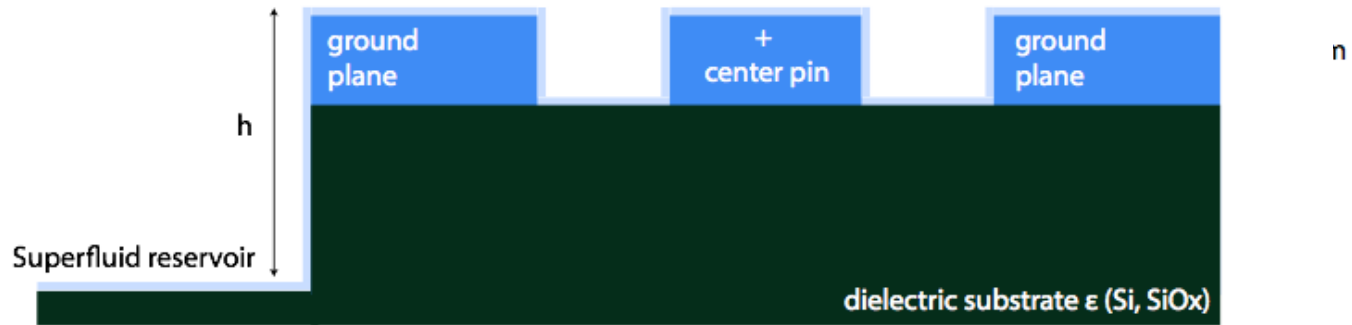
Experiment



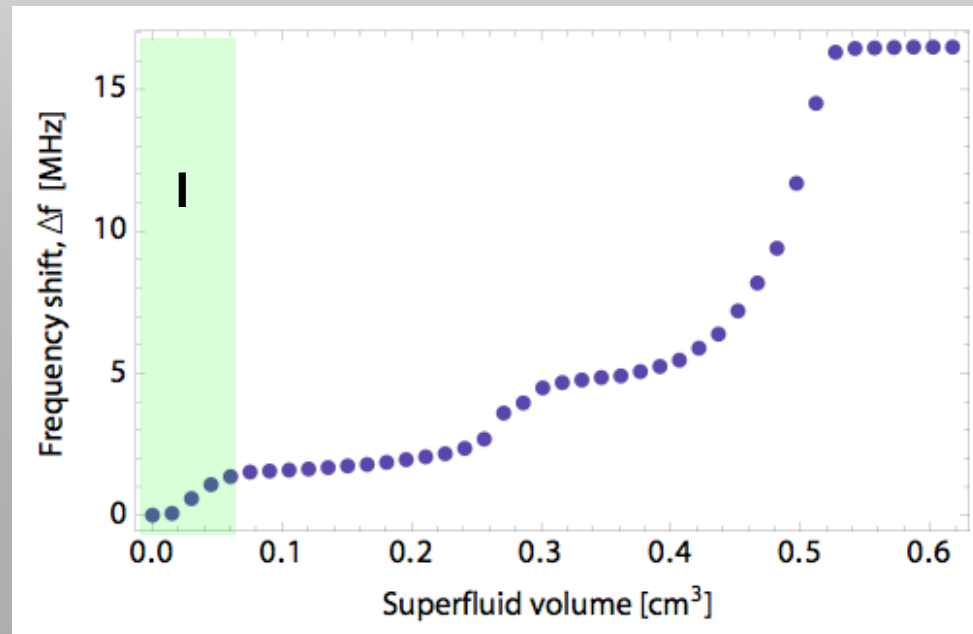
Superconducting Cavities as liquid He-Meters



I. Unsaturated van-der-Waals film $d \sim 30$ nm



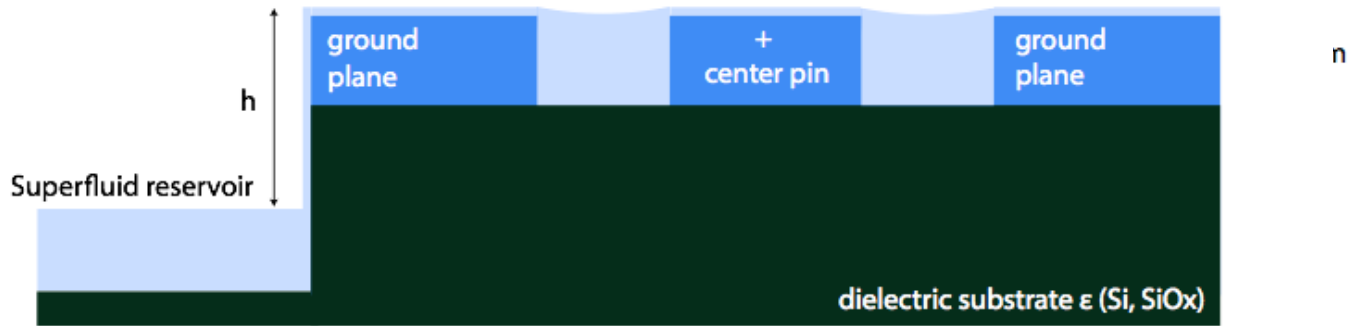
Experiment



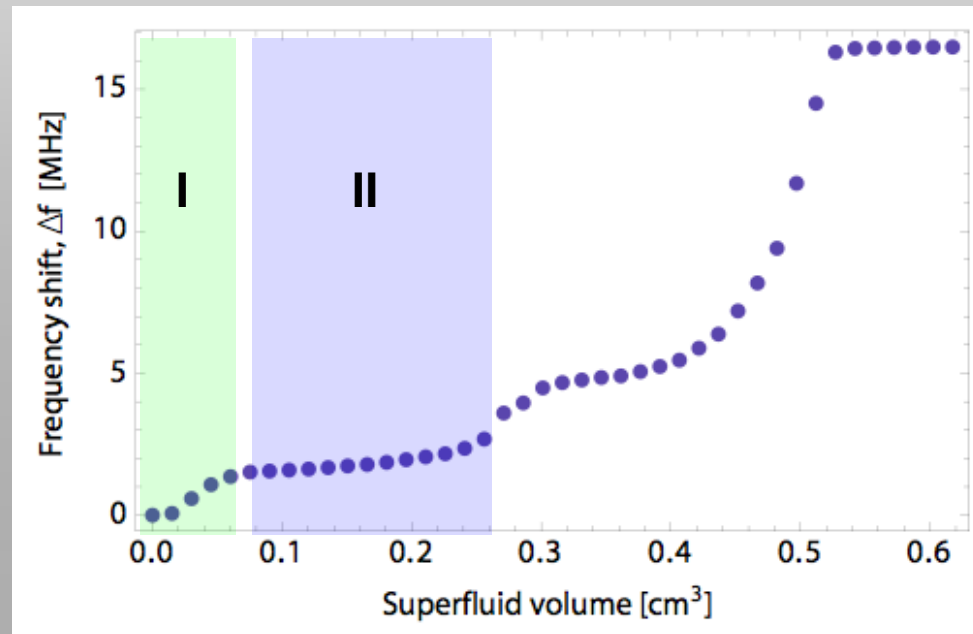
Superconducting Cavities as liquid He-Meters



II. Stable capillary action: gaps filled



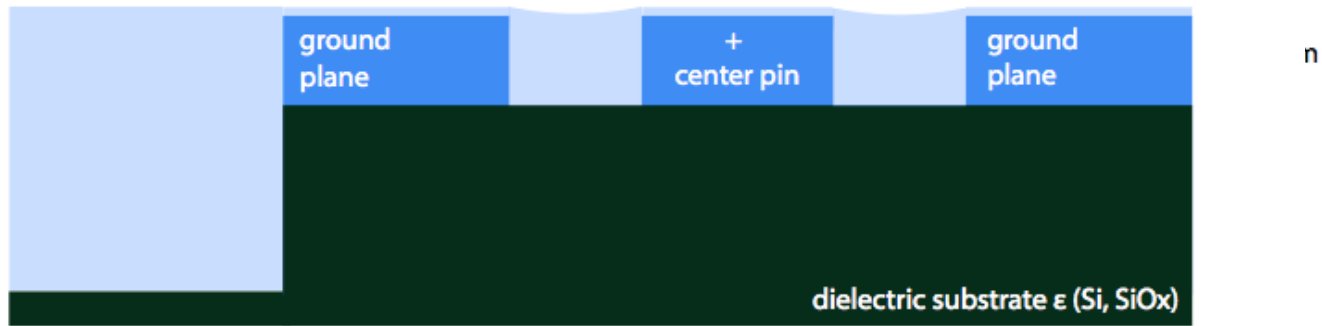
Experiment



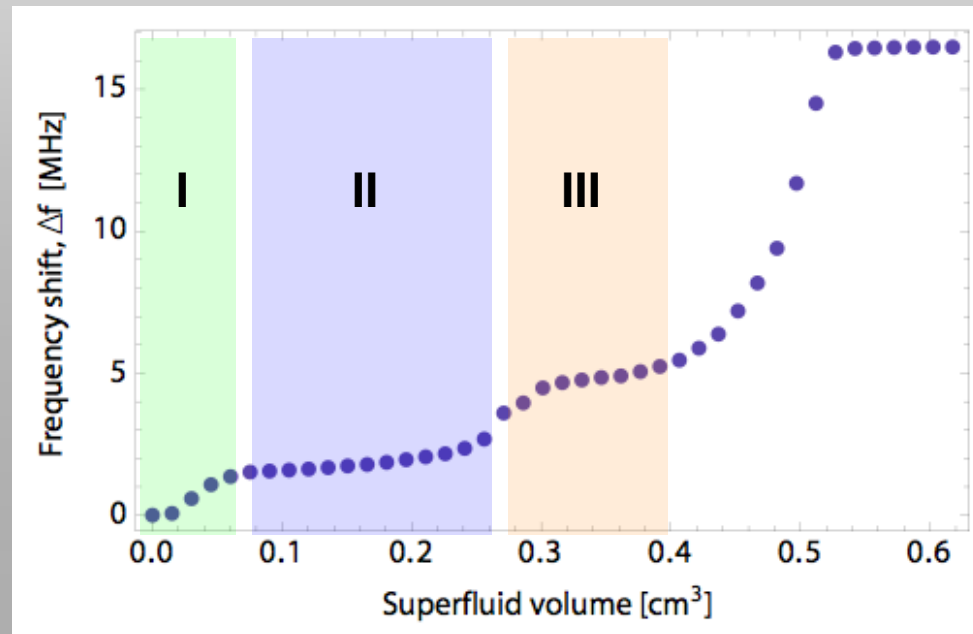
Superconducting Cavities as liquid He-Meters



III. Unstable capillary action



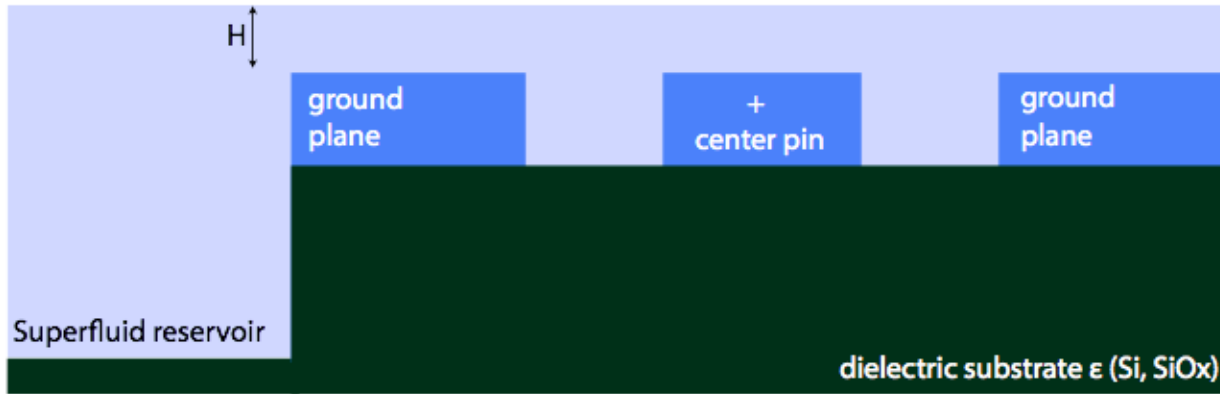
Experiment



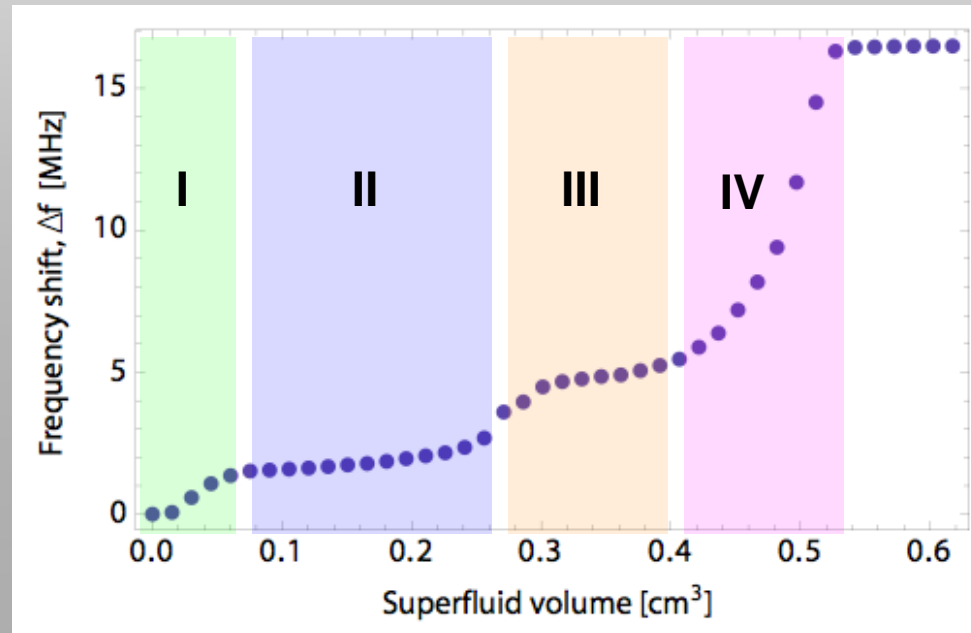
Superconducting Cavities as liquid He-Meters



IV. Linear Filling



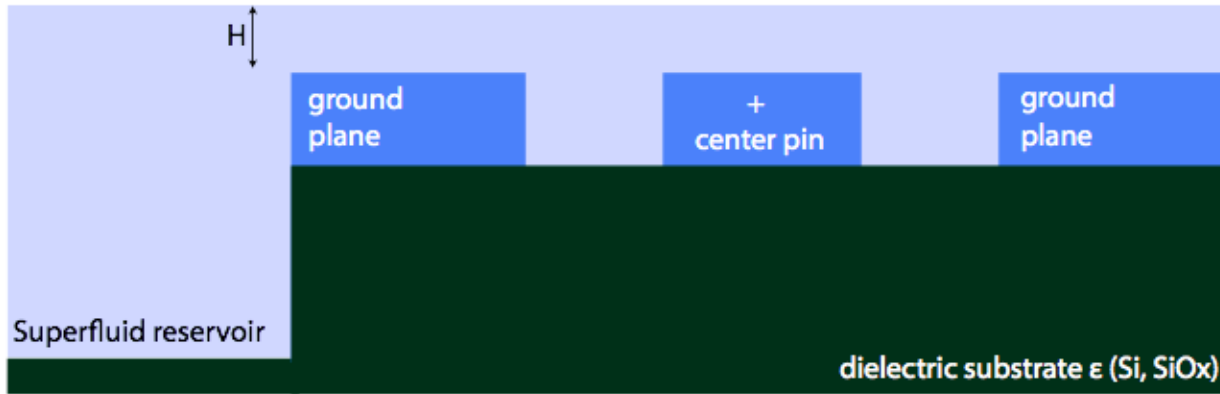
Experiment



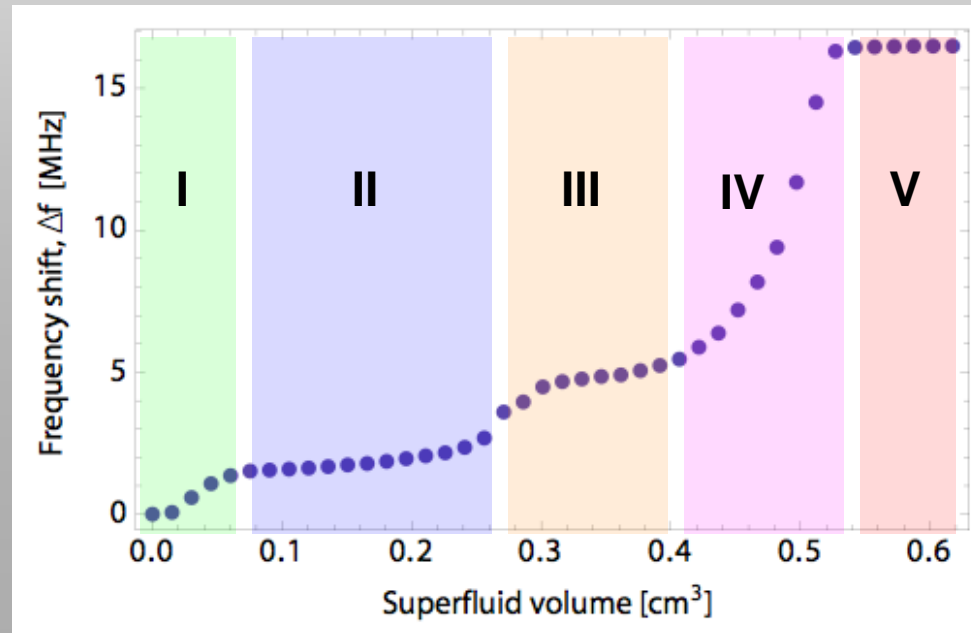
Superconducting Cavities as liquid He-Meters



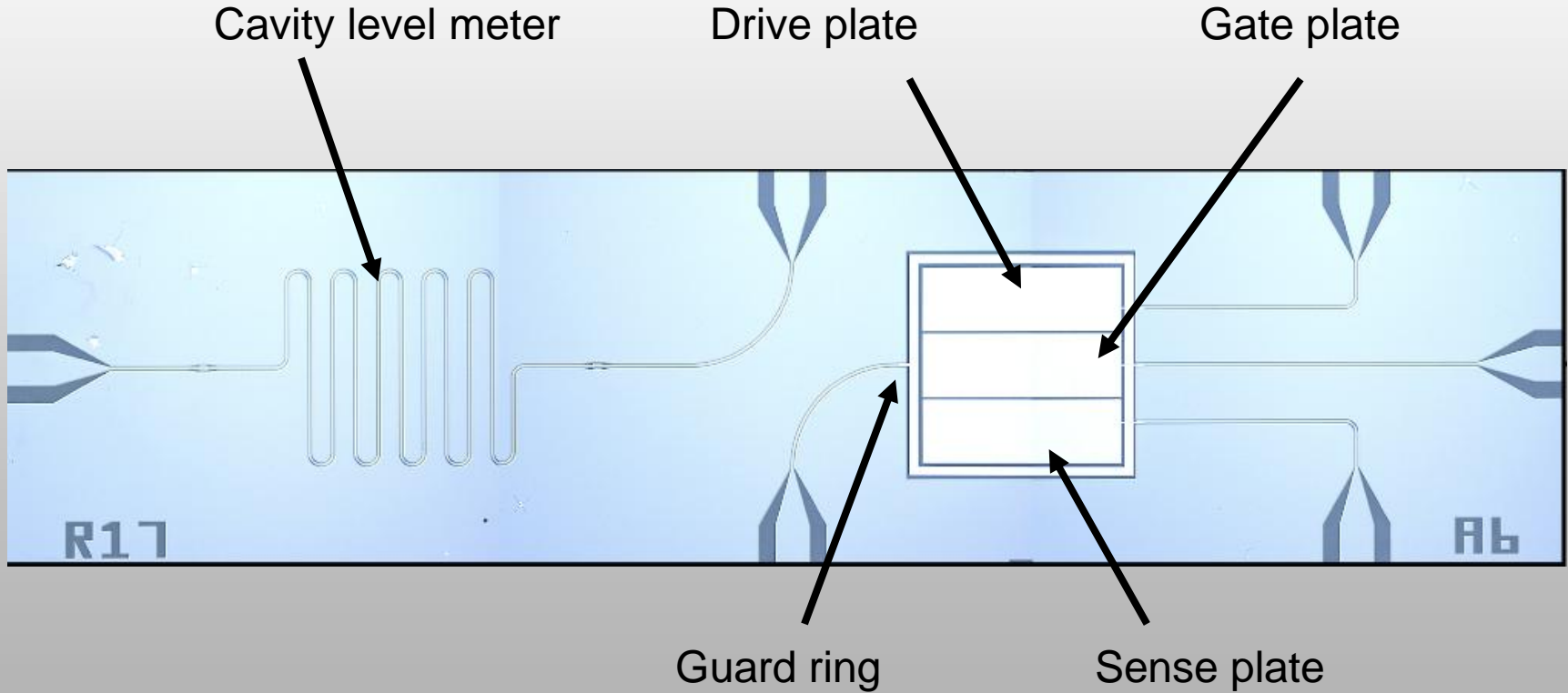
IV. Linear Filling



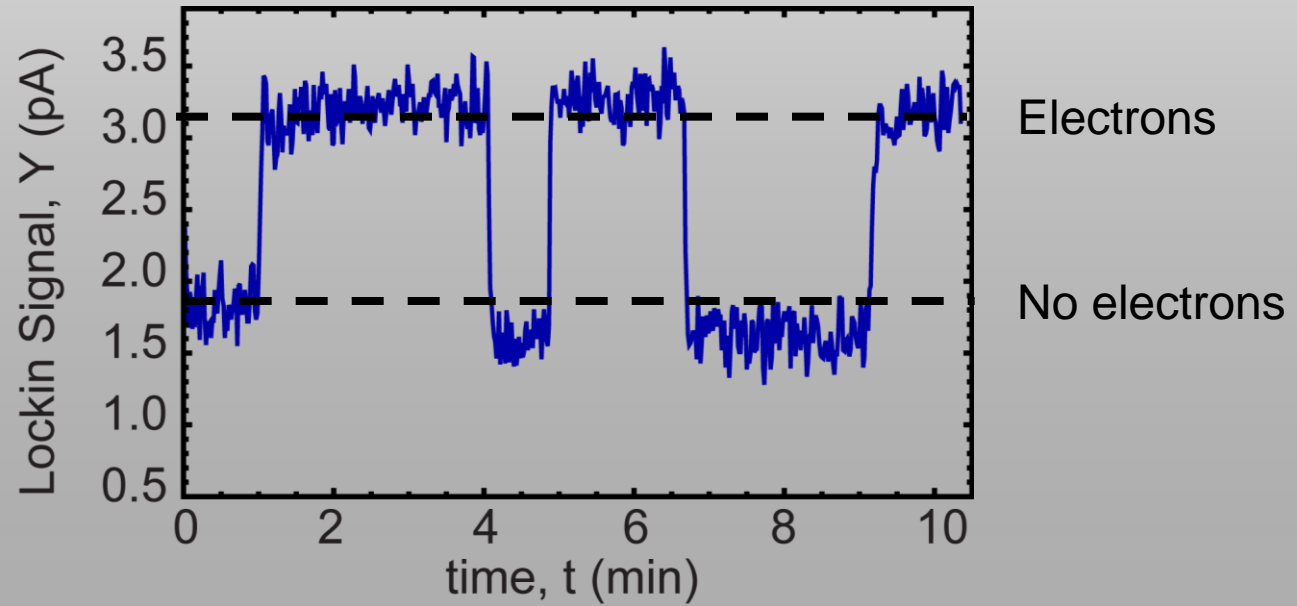
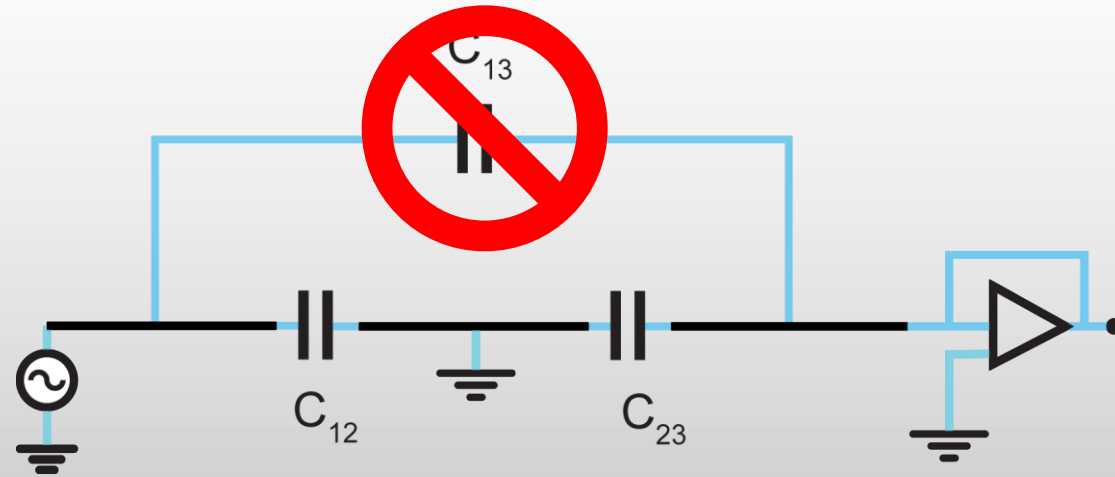
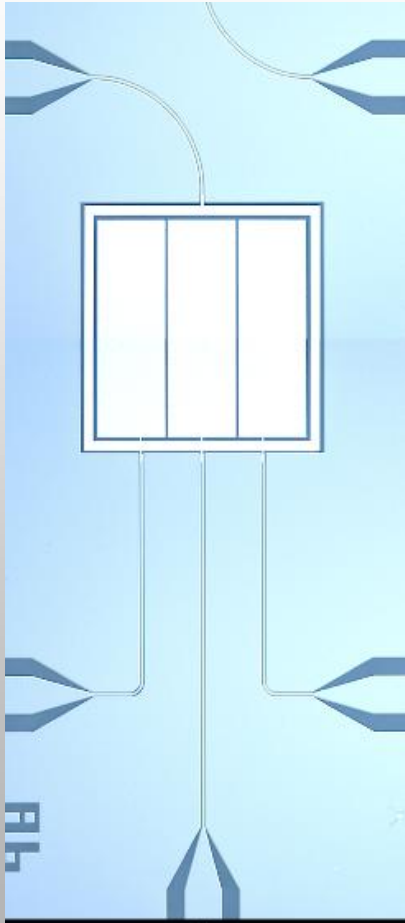
Experiment



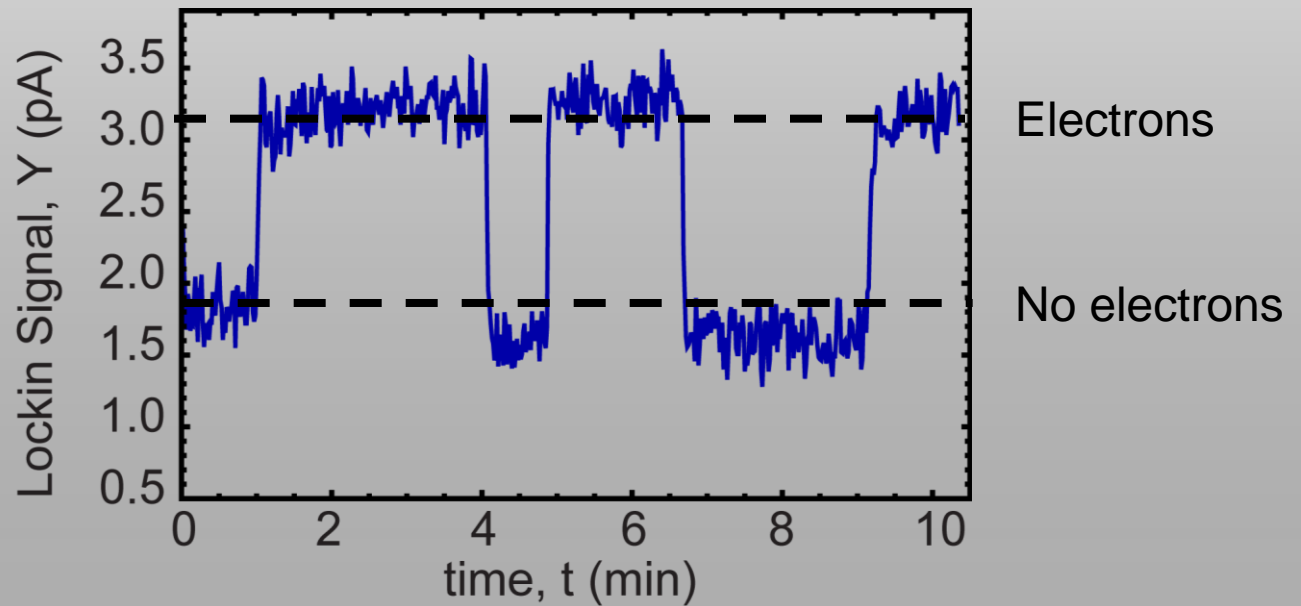
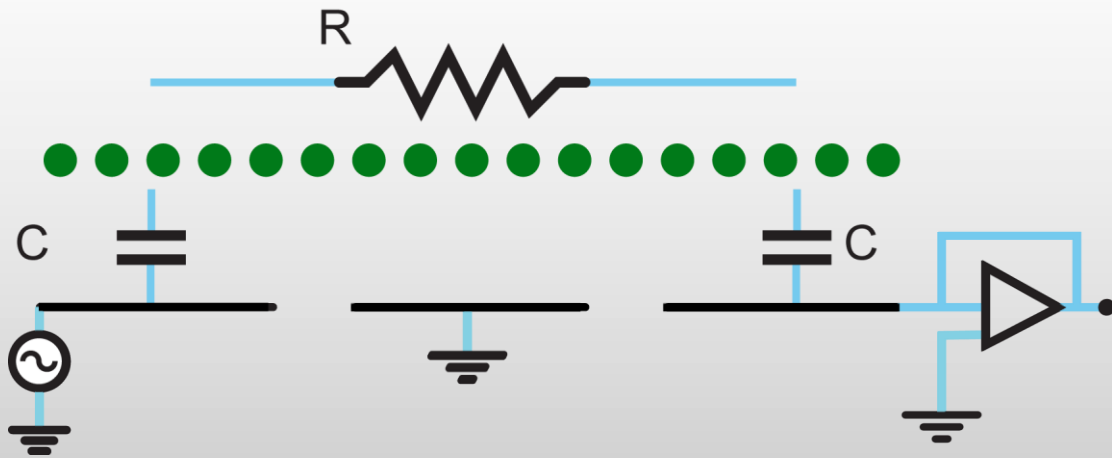
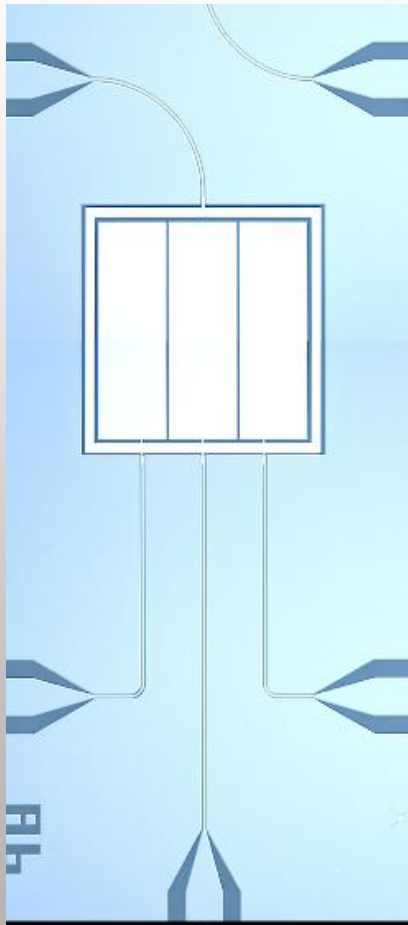
Anatomy of an “eon” trap



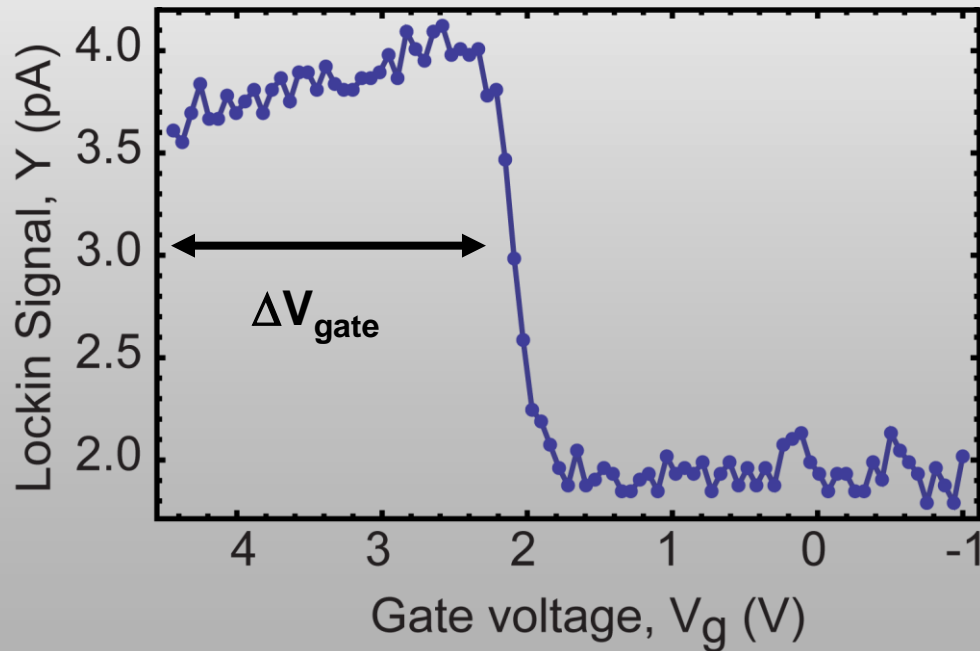
Detecting trapped electrons on helium



Detecting trapped electrons on helium

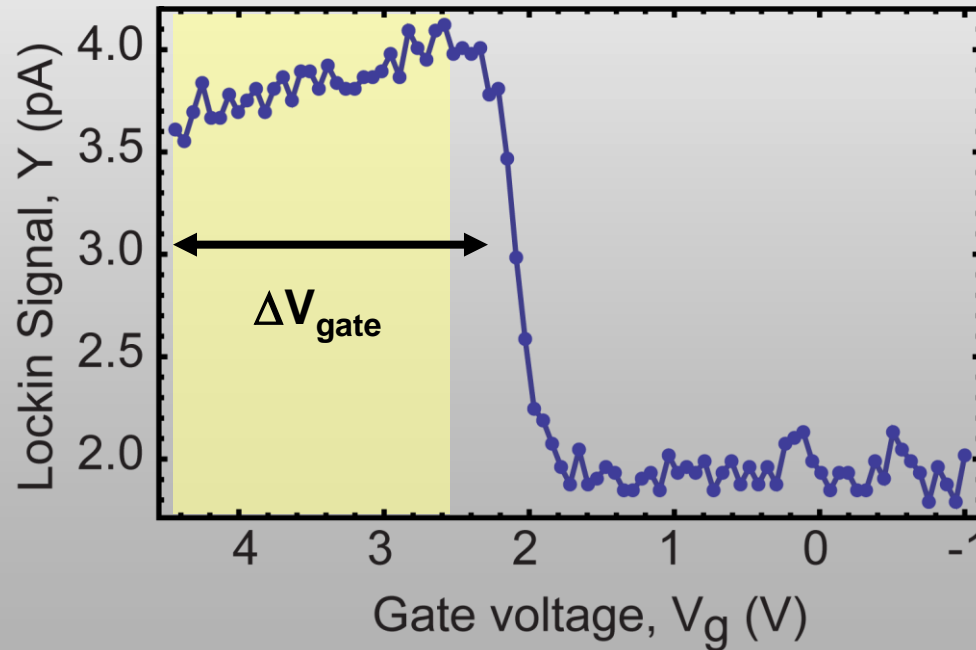


Making an eonhe transistor (eonFET)



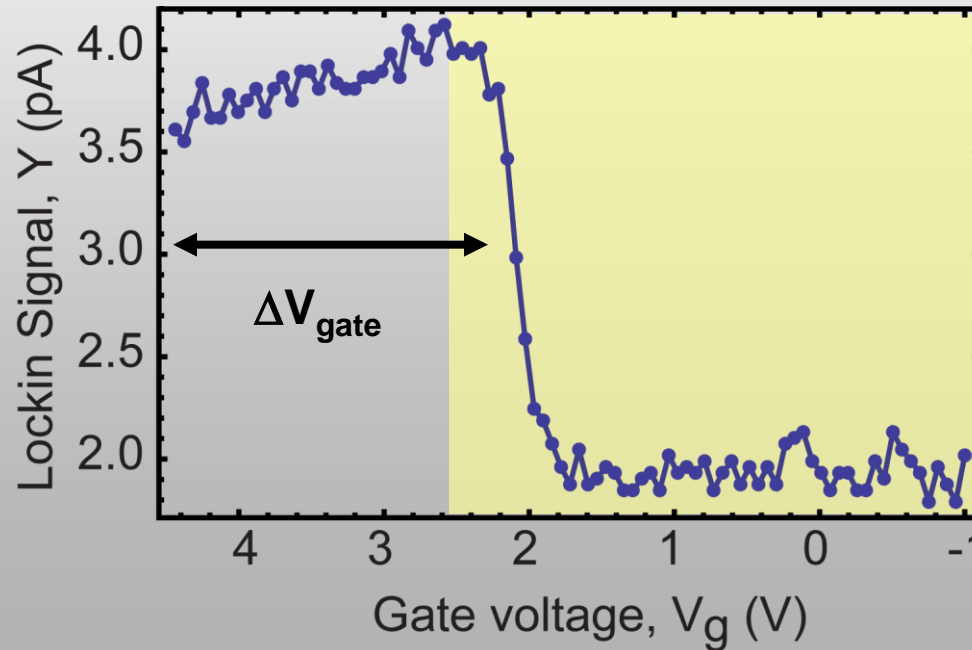
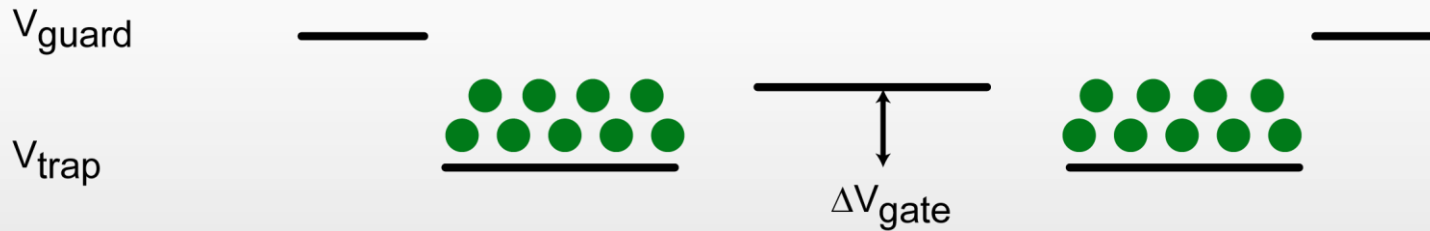
- ✧ Modulate density without losing electrons
- ✧ Measure density $\sim 10^9$ e/cm² (\sim few e/um²)

Making an eonhe transistor (eonFET)



- ✧ Modulate density without losing electrons
- ✧ Measure density $\sim 10^9$ e/cm² (\sim few e/um²)

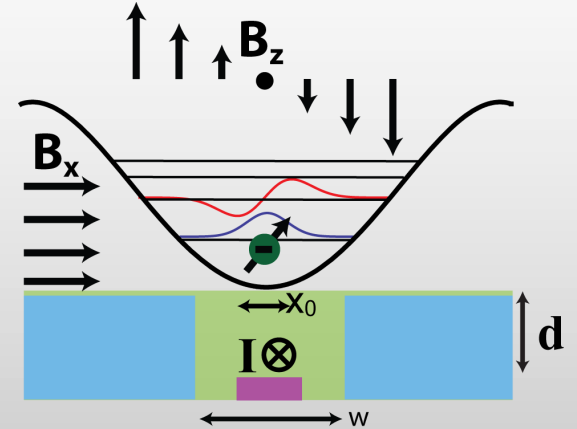
Making an eonhe transistor (eonFET)



- ✧ Modulate density without losing electrons
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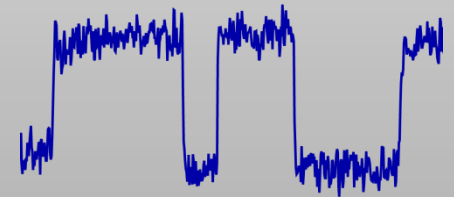
Electrons on Helium:

- Strong coupling limit easily reached
- Good coherence times for motion and spin
- Rich physics - single electron dynamics, motional and spin coherence, superfluid excitations, etc.



We see electrons on helium!!

- Can trap at 10 mK without much heating ($\sim 100\text{mK}$)
- Can hold them for hours



Next up: Trapping single electrons

