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Phugoid and Short Period
Differential Equations Produce State Rates of Change
$\begin{bmatrix} \Delta \dot{V}(t) \\ \Delta \dot{\gamma}(t) \\ \Delta \dot{q}(t) \\ \Delta \dot{\alpha}(t) \end{bmatrix} = \begin{bmatrix} -0.02 & -9.8 & 0 & 0 \\ 0.02 & 0 & 0 & 1.3 \\ 0 & 0 & -1.3 & -8 \\ -0.02 & 0 & 1 & -1.3 \end{bmatrix} \begin{bmatrix} \Delta V(t) \\ \Delta \gamma(t) \\ \Delta q(t) \\ \Delta \alpha(t) \end{bmatrix} + \begin{bmatrix} 4.7 & 0 \\ 0 & 0 \\ 0 & -9.1 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta \delta T(t) \\ \Delta \delta E(t) \end{bmatrix}$
Difference Equations Produce State Increments $\delta t = 0.1 \text{sec}$
$\begin{bmatrix} \Delta V_{k+1} \\ \Delta \gamma_{k+1} \\ \Delta q_{k+1} \\ \Delta \alpha_{k+1} \end{bmatrix} = \begin{bmatrix} 1 & -0.98 & -0.002 & -0.06 \\ 0.002 & 1 & 0.006 & 0.12 \\ 0.0001 & 0 & 0.84 & -0.69 \\ -0.002 & 0.0001 & 0.09 & 0.84 \end{bmatrix} \begin{bmatrix} \Delta V_k \\ \Delta \gamma_k \\ \Delta q_k \\ \Delta \alpha_k \end{bmatrix} + \begin{bmatrix} 0.47 & 0.0005 \\ -0.002 & -0.002 \\ 0 & -0.84 \\ 0 & -0.04 \end{bmatrix} \begin{bmatrix} \Delta \delta T_k \\ \Delta \delta E_k \end{bmatrix}$ 49