

# Communication and bargaining in the spatial model

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**Abstract** This paper studies collective choice by participants possessing private information in policymaking institutions that involve cheap-talk communication and bargaining. The main result establishes a connection between the extent to which problems of this type possess fully-revealing equilibria that select policies in the full information majority rule core (when it is well-defined) and the extent to which a fictitious sender-receiver game possesses a fully revealing equilibria. This result allows us to extend Banks and Duggan's (Am polit Sci Rev 94(1) 73–88, 2000) core equivalence results to the case of noisy policymaking environments with private information and communication when some combination of non exclusivity and preference alignment conditions are satisfied.

## 1 Introduction

In many collective choice settings participants face uncertainty about the relationship between the policy levers that they can control and the eventual outcomes that they care about. In the presence of this uncertainty participants may collect information or be chosen on the basis of expertise. Thus, it is likely that collective choice problems also involve private information about the uncertain relationship between policies and outcomes. In addition to asymmetric information the participants may differ in their preferences or ideologies; they may disagree about which information contingent rule for selecting policy is optimal. The presence of divergent preferences opens up the possibility that agents may not be willing to reveal their information.

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Despite the canonical nature of this description, basic questions about the possibility of efficiently aggregating information and preferences remain open. Much is known about strategic behavior in policymaking institutions without uncertainty (e.g., [Baron and Ferejohn 1989](#); [Banks and Duggan 2000](#)) and questions of information transmission between agents and a principal ([Crawford and Sobel 1982](#); [Gilligan and Krehbiel 1989](#); [Baron 2000](#); [Battaglini 2002](#)). However, little is known about strategic behavior amongst a collective of policymakers in the presence of asymmetric information. One might expect these considerations to surface in the study of deliberative democracy, an area that political scientists have become increasingly preoccupied with (e.g., [Gutmann and Thompson 1996](#)). Unfortunately, scholars of deliberation tend to ignore the incentives for information transmission in deliberative settings. The few game theoretic works that focus on incentives ([Austen-Smith and Feddersen 2003a,b](#); [Coughlan 2000](#); [Gerardi and Yariv 2003](#); [Meirowitz 2003, 2006](#)) consider problems in which the set of alternatives is binary. This paper moves beyond existing theoretic work on deliberation, specifically, and collective choice, generally. It considers endogenous agendas, voting, and communication in the presence of informational asymmetries and preference divergence. More precisely, this paper investigates the extent to which institutions that allow for cheap talk communication and bargaining over policy can effectively aggregate preferences and information.

The spatial model has become a centerpiece of the literatures on legislative politics, agenda theory, and social choice theory. Because of this, we focus on the problem of simultaneously aggregating information and preferences when agents have spatial preferences over outcomes which admit a non-empty majority rule core and agents possess private information about a policy shock. The first main result connects two distinct literatures – bargaining and signaling. We establish an equivalence between the problem of finding equilibria that reach the full information majority rule core in communication and bargaining games and the problem of finding truthful equilibria in particular cheap-talk signaling games. Motivated by this equivalence, the two remaining results offer a characterization of the preference profiles and informational environments in which cheap-talk signaling games possess truthful equilibria. In the case of private signals that are neither conditionally independent nor identically distributed these results may be of particular interest.

It is amusing to note that this work brings the literature on cheap talk communication full circle. [Crawford and Sobel \(1982\)](#) motivate their path-breaking investigation of cheap-talk signaling with a discussion of bargaining problems.

Bargainers typically have different information about preferences and even what is feasible. Sharing information makes available better potential agreements but it also has strategic effects that make one suspect that revealing all to an opponent is not usually the most advantageous policy. . . . While our primary motivations stem from the theory of bargaining, we have found it useful to approach these questions in a more abstract setting, which allows us to identify the essential prerequisites for the solution we propose. (p. 1431).

While the literature on cheap talk signaling games is now quite extensive, connections between this literature and the problem of communication and bargaining still need to be explored. The equivalence result presented here, moves in this direction by showing that in the context of well behaved spatial policymaking models, the solution to a bargaining problem with communication is “the same as” the solution to a cheap-talk signaling game with multiple senders and one receiver.

Many of the logical steps needed for the development are present in the extant literature. An extension of Banks and Duggan’s (2000) core characterization result to the case of symmetric uncertainty about of a shock to policy leads to the conclusion that when preferences over outcomes satisfy the [Plott \(1967\)](#) conditions no delay stationary Bayesian equilibria reach the expected ideal policy of the participant with the core ideal point. Following the approach of [Myerson’s \(1982\)](#) revelation principle for direct coordination mechanisms we augment the endogenous agenda game with a round of communication, and show that the incentive compatibility conditions for information revelation correspond to those in a simple cheap-talk game in which the receiver has the preferences of the core voter.<sup>1</sup> Finally, a result in [Baron and Meirowitz \(2006\)](#), and a generalization of the conditions satisfied in [Battaglini \(2002\)](#) allow us to present necessary and sufficient conditions on the informational environment and preferences for satisfaction of these incentive compatibility conditions.

## 2 Preliminaries

We consider the following collective choice problem. A policy  $p \in \mathbb{R}^d$  must be chosen. A set of  $n$  (odd) participants,  $N$ , have preferences that depend on the policy,  $p$ , and a random shock  $\varepsilon \in \mathbb{R}^d$ . Participants do not observe the shock, but each  $i \in N$  observes a private signal  $s_i \in \mathbb{R}^d$  that is correlated with  $\varepsilon$ . In this setting an informational environment is a joint distribution on the random variables  $(\varepsilon, \mathbf{s}) := (\varepsilon, s_1, s_2, \dots, s_n)$ . Let  $F(\varepsilon, \mathbf{s})$  denote such a joint distribution and assume that the informational environment is sufficiently well-behaved that for any sub vectors  $a$  and  $b$  of the random variables the conditional distribution  $F(a \mid b)$  exists. Participant  $i$  has an ideal point  $y_i \in \mathbb{R}^d$  and preferences representable by the Bernoulli utility function

$$u_i(p, \varepsilon) = - \|p + \varepsilon - y_i\|^2. \quad (1)$$

The quadratic loss function and additive shock is commonly used in the literature.<sup>2</sup> For our purposes a particularly important property of this representation is the fact that mean-variance analysis is appropriate. Specifically, if

<sup>1</sup> [Baliga and Morris \(2002\)](#) and [Kim \(2005\)](#) consider the value of pre-play communication in two player-games.

<sup>2</sup> [Bendor and Meirowitz \(2004\)](#) note that reliance on these assumptions has hurt the delegation literature and demonstrate that the preference assumption is far less relevant than the assumption that randomness is of this form.

$F(\cdot)$  is a distribution function then the extension of preferences to lotteries is representable by the Von Neumann-Morgenstern utility function

$$\int u_i(p, \varepsilon)dF(\varepsilon) = - \|p + \bar{\varepsilon} - y_i\|^2 - v \tag{2}$$

where  $\bar{\varepsilon} = \int \varepsilon dF(\varepsilon)$ , and  $v = \int (\varepsilon - \bar{\varepsilon})'(\varepsilon - \bar{\varepsilon})dF(\varepsilon)$  are the expectation and variance of  $\varepsilon$  under the marginal distribution  $F(\cdot)$ .

First, we describe the bargaining framework, ignoring private information and communication. We draw on the extensive literature following [Baron and Ferejohn \(1989\)](#), and assume that policymaking occurs in a sequential process. Specifically, we consider the simple majority rule bargaining game of [Banks and Duggan \(2000\)](#). In period  $t = 1, 2 \dots$  participant  $i \in N$  is chosen with probability  $\rho_i \in (0, 1)$  to make a proposal  $p_i^t \in \mathbb{R}^d$ . Following a proposal, the participants simultaneously cast ballots to accept or reject the proposal. If at least  $\frac{n+1}{2}$  participants vote to accept then the game ends and the policy  $p_i^t$  is enacted. If at least  $\frac{n+1}{2}$  participants vote to reject then the game moves on to period  $t + 1$  and the process repeats. A termination history is then characterized by a policy  $p_i^t$  and a time  $t$ , at which the policy is enacted. The results in [Banks and Duggan \(2000\)](#) are sharpest under the assumption that agents do not discount, so we maintain this assumption. The expected payoff to participant  $j$  from such a termination history is

$$\int u_j(p_i^t, \varepsilon)dF(\varepsilon) = - \|p_i^t + \bar{\varepsilon} - y_j\|^2 - v. \tag{3}$$

Most scholars choose to focus on stationary equilibria to bargaining games of this form. See [Baron and Kalai \(1993\)](#) for a justification of this selection. A stationary strategy to the bargaining game is a proposal  $p_i$  that  $i$  will make at any history in which she is recognized to propose and a measurable mapping  $v_i : \mathbb{R}^d \rightarrow \{\text{accept, reject}\}$ . Thus,  $v_i(p)$  specifies how  $i$  will vote if  $p$  is proposed. An equilibrium in the Banks and Duggan game involves sequentially rational proposal strategies and voting strategies that satisfy weak dominance. In the presence of the random shock, weak dominance requires that voter  $j$  support proposal  $p_i^t$  if  $\int u_j(p_i^t, \varepsilon, )dF(\varepsilon)$  is higher than the continuation value obtained from the defeat of proposal  $p_i^t$  and equilibrium play in subsequent periods. In [Banks and Duggan \(2000\)](#) there is no policy uncertainty, so that  $\varepsilon$  is commonly known to be the 0 vector. Banks and Duggan focus on a subset of the stationary equilibria (termed no delay equilibria) that involve agreement on a policy in the first period. Given the simplification afforded by (3) for a fixed distribution  $F(\varepsilon)$  we can characterize the no delay equilibria in a bargaining game with common uncertainty about the shock. A few definitions are needed first.

Given a profile of ideal points,  $\mathbf{y} = (y_1, y_2, \dots, y_n) \in \mathbb{R}^{nd}$  the majority rule core is the set of policies that are unbeatable by pair-wise comparisons and defined as

$$C_m(\mathbf{y}) = \left\{ x \in \mathbb{R}^d : \forall z \in X, \#\{i : \|y_i - x\| \leq \|y_i - z\|\} \geq \frac{n + 1}{2} \right\} \tag{4}$$

where  $\#A$  is the cardinality of the set  $A$ . In the case of no uncertainty, Plott's (1967) result offers a characterization of the profiles for which the core is non-empty. With  $n$  odd, we can restate the characterization in a convenient manner, using the notion of a half space. For two policies,  $x, t \in \mathbb{R}^d$  the open half space at  $x$  including  $t$  is

$$H_t^+(x) = \{z \in \mathbb{R}^d : z't > x't\}. \tag{5}$$

The number of participants with ideal points in  $H_t^+(x)$  is denoted  $\#H_t^+(x) = \#\{i \in N : y_i \in H_t^+(x)\}$ . We say that  $x$  is a *median in all directions* if for every  $t$ ,  $\#H_t^+(x) < \frac{n+1}{2}$ . With  $n$  odd, Plott's result can then be stated in the following simple manner: *the majority rule core coincides with the set of medians in all directions.*

With the quadratic loss function and an odd number of voters, Banks and Duggan (2004) use the representation in (3) to show that if  $x$  is a median in all directions then the majority preference relation over lotteries on  $\mathbb{R}^d$  is the same as the preference relation of the participant with ideal point  $x$ . Results in Banks and Duggan (2000) can be extended to bargaining games in which no agent has private information but there is public uncertainty about the consequences of policy in the form of a distribution  $F(\varepsilon)$ .

**Lemma 1** *Assume that ideal points  $\mathbf{y}$  are such that  $x \in \mathbb{R}^d$  is a median in all directions. Consider a majority rule bargaining game in which, (1) each agent is recognized with positive probability; (2) agents do not discount; (3) there is uncertainty about the shock  $\varepsilon$  characterized by a commonly known distribution  $F(\varepsilon)$ -so no agent possesses private information. In this game there exists a no delay stationary equilibrium and all no delay stationary equilibria select the policy  $x - \bar{\varepsilon}$  with probability 1.*

*Proof* Existence follows from lemma 1 of Banks and Duggan (2000). To see this, it is sufficient to note that the payoffs are strictly quasi-concave in  $p$ , majority rule is proper and under the assumption that  $x$  is a median in all directions,  $\{x\} = C_m(\mathbf{y})$ . The fact that all no delay stationary equilibria yield  $x - \bar{\varepsilon}$  with probability 1 requires appeal to theorem 6 of Banks and Duggan (2000). With fixed  $F(\varepsilon)$ ,  $\int u_i(p, \varepsilon) dF(\varepsilon) = -\|p + \bar{\varepsilon} - y_i\|^2 - v$  and thus the payoffs over lotteries are quadratic with ideal points  $y_i - \bar{\varepsilon}$  plus a constant scaler  $-v$ . Given this and the fact that majority rule is strong with  $n$  odd, Theorem 6 applies.  $\square$

In the remainder of the paper we assume that a median in all directions exists. Now consider an augmented version of an endogenous agenda bargaining game with uncertainty in which (1) agents have private information in the form of the private signals  $s_i$  and (2) prior to bargaining there is a round of simultaneous communication. For a fixed information environment characterized by the joint distribution  $F(\varepsilon, \mathbf{s})$  and a profile of preferences characterized by  $\mathbf{y}$  we define the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y} \rangle$ -deliberation game as follows. In the first period participants make simultaneous public announcements,  $m_i \in \mathbb{R}^d$ , about  $s_i$  and then the bargaining game is played. Analysis of this game requires that we consider an equilibrium concept which involves sequential rationality and

consistent belief formation. We are interested in perfect Bayesian Nash equilibria in which conditional on beliefs about  $(\varepsilon, \mathbf{s})$  voting and proposing strategies are stationary and voting strategies satisfy weak dominance. A strategy for player  $i$  is then a measurable message mapping,  $m_i : \mathbb{R}^d \rightarrow \mathbb{R}^d$ , a measurable proposal mapping,  $p_i : \mathbb{R}^{d(n+1)} \rightarrow \mathbb{R}^d$ , and a measurable voting mapping,  $v_i : \mathbb{R}^{d(n+2)} \rightarrow \{\text{accept, reject}\}$ . An equivalent way to conceptualize voting strategies is to think about message contingent acceptance sets. In addition to strategies an equilibrium requires that players have beliefs about  $(\varepsilon, \mathbf{s})$  conditional on the observed history. For any period  $t$  there must be two types of beliefs, those for proposers that condition on the messages  $\mathbf{m}$ , as well as play in previous periods and those for voters that condition on  $\mathbf{m}$  and the proposal  $p_i^t$  and the play in previous periods. For a fixed history of play up to period  $t - 1, h^{t-1}$ , and message profile  $\mathbf{m}$  a belief for player  $i$  is then a joint distribution function on  $\mathbb{R}^{d(n+1)}$  and we use the notation  $\mu_i(\cdot \mid \mathbf{m}, h^{t-1}), \mu_i(\cdot \mid p_j^t, \mathbf{m}, h^{t-1})$  to denote such conditional beliefs. We sometimes call an equilibrium of this form a *deliberative equilibrium*. If such an equilibrium involves passage of the first period proposal with probability 1 we call it a *no-delay deliberative equilibrium*.

In the remainder of the paper we focus on the existence of no delay deliberative equilibria in which participants are truthful in the communication stage. We say a *deliberative equilibrium is truthful* if for all  $i \in N, m_i(s_i) = s_i$ . Since our focus is on no delay equilibria in which the messages are truthful very few types of histories need to be studied. We will, however, need to address beliefs following a proposal  $p_i^t$  that is not consistent with equilibrium behavior by  $i$  given the observed profile of messages; this type of history occurs if a single agent deviates from a no delay stationary strategy profile.

First, we characterize the relationships between  $\mathbf{s}$  and policy that are supportable in truthful no delay deliberative equilibria.

**Lemma 2** *Consider an informational environment characterized by the joint distribution  $F(\varepsilon, \mathbf{s})$  and assume that ideal points  $\mathbf{y}$  are such that  $x \in \mathbb{R}^d$  is a median in all directions. Any truthful no delay deliberative equilibrium to the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y} \rangle$ -deliberation game results in policy selection according to the rule*

$$p^*(\mathbf{s}) = x - \int \varepsilon dF(\varepsilon \mid \mathbf{s}). \tag{6}$$

*Proof* In any truthful equilibrium consistency of beliefs requires that all agents have the same message conditional posteriors of the form  $F(\varepsilon \mid \mathbf{s})$ . This and Lemma 1 yield the result. □

Our goal is to show that in order to understand whether an informational environment and preference profile admit truthful deliberative equilibria it is sufficient to study a simpler cheap talk signaling game in which the agents in  $N$  simultaneously submit messages to a receiver that selects policy. For a fixed information environment and preference profile  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y} \rangle$  and point  $x \in \mathbb{R}^d$

we define the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$ -signaling game as follows. In period 1 each  $i \in N$  simultaneously submits a message  $m_i \in \mathbb{R}^d$  to a receiver,  $r$ , with ideal point  $x$ . In period 2 the receiver selects a policy  $p \in \mathbb{R}^d$ . So a pure strategy for sender  $i$  is a measurable mapping  $m_i : \mathbb{R}^d \rightarrow \mathbb{R}^d$ , a pure strategy for the receiver is a measurable mapping  $p : \mathbb{R}^{dn} \rightarrow \mathbb{R}^d$  and for each message profile, a belief for the receiver is a joint distribution on  $\mathbb{R}^d$  which we denote by  $\eta(\cdot \mid \mathbf{m})$ . We focus on perfect Bayesian equilibria, requiring that message functions are simultaneous best responses given the policy function, that the policy function is optimal for  $r$  given the beliefs  $\eta(\cdot \mid \mathbf{m})$ , and that given the message functions the beliefs are consistent with Bayes' rule – when it applies. We call such an equilibrium a *signaling equilibrium* and say a *signaling equilibrium is truthful* if  $m_i(s_i) = s_i$  for all  $i \in N$ . The analogue to Lemma 2 is.

**Lemma 3** *Consider an informational environment characterized by the joint distribution  $F(\varepsilon, \mathbf{s})$ . Any truthful signaling equilibrium to the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$ -signaling game results in policy selection according to the mapping  $p^*(\mathbf{s})$  defined in Eq. (6).*

*Proof* The requirement that any equilibrium to the signaling game involves consistent beliefs and sequentially rational policy selection implies that  $p^*(\mathbf{m}) = x - \int \varepsilon dF(\varepsilon \mid \mathbf{m})$ . In a truthful equilibrium  $m_i = s_i$  for each  $i \in N$ .  $\square$

### 3 The equivalence result

In this section we show that if given the ideal points  $\mathbf{y}$  the point  $x$  is a median in all directions then the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y} \rangle$ -deliberation game possesses a truthful no delay deliberative equilibrium if and only if there is a truthful signaling equilibria in the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$ -signaling game. The subsequent section builds on Proposition 1 and focuses on signaling games to isolate conditions on preferences and informational environments that are necessary and sufficient for the existence of truthful equilibria in either type of game.

**Proposition 1** *Consider an informational environment characterized by the joint distribution  $F(\varepsilon, \mathbf{s})$  and assume that ideal points  $\mathbf{y}$  are such that  $x \in \mathbb{R}^d$  is a median in all directions. In the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y} \rangle$ -deliberation game there exists a truthful no delay deliberative equilibrium if and only if the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$ -signaling game possesses a truthful signaling equilibrium.*

*Proof* Assume that  $x$  is a median in all directions.

( $\implies$ ) Assume that in the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y} \rangle$ -deliberation game there exists a truthful no delay perfect Bayesian Nash equilibrium. Let  $p^e(\mathbf{m}) : \mathbb{R}^{nd} \rightarrow \mathbb{R}^d$  denote the mapping from message profiles into policies that results from the bargaining strategies in this equilibrium; from Lemma 2  $p^e(m) = p^*(m)$ . Let  $\mu_i^e(\cdot \mid \mathbf{m})$  denote the message conditional belief of player  $i$  in the equilibrium to the deliberation game. Now suppose that in the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$ -signaling game the receiver uses the strategy  $p^e(\mathbf{m})$ . Since  $m_i(s_i) = s_i$  is an equilibrium strategy in

the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y} \rangle$ -deliberation game, it must be a best response in the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$ -signaling game if all participants  $j \in N \setminus i$  are truthful and  $r$  uses  $p^e(m)$ . It remains only to verify that there are consistent beliefs for the receiver which make this strategy sequentially rational. Since the equilibrium to the deliberation game is truthful all participants must form the same beliefs (i.e.,  $\mu_i^e(\cdot \mid \mathbf{m})$  is almost surely equal to  $\mu^e(\cdot \mid \mathbf{m}), \forall i \in N$ ) following any  $\mathbf{m}$  that is feasible (i.e.,  $\mathbf{m}$  is in the support of  $F(\mathbf{s})$ ). Let  $\eta(\cdot \mid \mathbf{m})$  denote the marginal of  $\mu^e(\cdot \mid \mathbf{m})$  with respect to  $\varepsilon$ . Since beliefs are consistent in the equilibrium to the deliberation game this belief is consistent in the signaling game. By Lemma 2 we have  $p^e(\mathbf{m}) = p^*(\mathbf{m}) = x - \int \varepsilon dF(\varepsilon \mid \mathbf{s}) = x - \int \varepsilon d\mu^e(\cdot \mid \mathbf{m})$  and thus the receiver's strategy is sequentially rational given the belief.

( $\Leftarrow$ ) Assume that the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$ -signaling game possesses a truthful perfect Bayesian Nash equilibrium. Let  $p^E(\mathbf{m}): \mathbb{R}^{nd} \rightarrow \mathbb{R}^d$  denote the receiver's strategy and let  $\mu^E(\cdot \mid \mathbf{m})$  denote the receiver's posterior in this truthful equilibrium. Consider the strategy profile to the deliberation game in which  $m_i(s_i) = s_i$ , each participant's proposal strategy is  $p^E(\mathbf{m})$ , and each participant's message contingent belief is given by  $\mu^E(\cdot \mid \mathbf{m})$ . Moreover, let the message and proposal contingent beliefs correspond to  $\mu^E(\cdot \mid \mathbf{m})$ . Finally, let the voting strategies of each  $i$  satisfy weak dominance given the utility function  $\int u_i(p, \varepsilon, \cdot) d\mu^E(\varepsilon \mid \mathbf{m})$ . By construction the beliefs are consistent and the voting strategies satisfy sequential rationality. It remains to check that no agent has an incentive to unilaterally deviate in the message or proposing strategies. By Lemma 3  $p^E(\cdot)$  selects the unique policy in the majority rule core. Thus, the proposal strategy selects the unique policy that is in the majority rule core given  $\mathbf{m}$ , so any proposal other than  $p^E(\mathbf{m})$  will not be accepted by a majority and, thus, such a proposal will fail. This means that if player  $i$  deviates only in her proposal strategy the deviation will not pass and the next proposer (other than  $i$ ) following the equilibrium strategies will propose  $p^E(\mathbf{m})$  and it will pass. Since each agent's recognition probability is less than one, when agent  $i$  is recognized and makes a rejected proposal a different proposer will eventually be recognized and the proposal  $p^E(\mathbf{m})$  will eventually be proposed and pass. This implies that the only deviation that agent  $i$  can unilaterally make which will affect her payoffs is to deviate in her message, sending  $m'_i \neq m_i$ . Given that everyone else plays the conjectured strategy profile, following such a deviation the resulting outcome will be  $p^E(\mathbf{m}_{-i}, m'_i)$  regardless of how  $i$  proposes if she is recognized. Specifically, if  $i$  deviates at the message level and is not recognized to propose, the equilibrium strategies will result in the policy  $p^E(\mathbf{m}_{-i}, m'_i)$ . If  $i$  is recognized to propose and proposes  $p^E(\mathbf{m}_{-i}, m'_i)$  this policy will pass. The remaining possibility is that  $i$  is recognized and proposes a policy  $p'$  that she strictly prefers to  $p^E(\mathbf{m}_{-i}, m'_i)$ . But unless  $y_i = x$  this policy will not be supported by a majority of voters and, thus, the policy  $p^E(\mathbf{m}_{-i}, m'_i)$  will eventually be passed. If  $y_i = x$  then the equilibrium profile results in  $i$ 's optimum and the deviation cannot be desirable. Thus, the only deviation that  $i$  can make which affects her payoff is to cause the policy  $p^E(\mathbf{m}_{-i}, m'_i)$  to pass instead of the policy  $p^E(\mathbf{m})$ . But, since the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$ -signaling game possesses a truthful perfect

Bayesian Nash equilibrium, agent  $i$  weakly prefers  $p^E(\mathbf{m})$  to  $p^E(\mathbf{m}_{-i}, m'_i)$  as this is the necessary incentive compatibility condition for truthfulness in the signaling game.  $\square$

It should be noted that the equivalence does not hold for general policy-making games. Specifically, in representing a game with communication as a mechanism it is generally necessary to include the additional requirement that players are willing to play the game in a prescribed manner. In Myerson (1982) there are two types of incentive compatibility conditions: truthful and obedient. In the current problem, however, it turns out that all unilateral deviations reach payoffs that are achievable through just a deviation at the message stage and thus only the truthful conditions bind.

#### 4 Necessary and sufficient conditions

The remainder of the paper highlights conditions under which truthful equilibria (of either type) exist. The exposition focuses on signaling games. In order to impose slightly more structure we now assume that  $F(\varepsilon)$  is absolutely continuous with respect to Lebesgue measure on a support that is a convex subset of  $\mathbb{R}^d$ . In addition, we assume that each agent's private signal is given by  $s_i = \varepsilon + \delta_i$  where each dimension of  $\delta_i$  is either concentrated at 0 or has a marginal distribution that is absolutely continuous with respect to Lebesgue measure on a support that is an interval in  $\mathbb{R}^1$ . Thus, for each dimension, private signals are either perfectly informative or have a nice density. These conditions are, for example, more general than those in Battaglini (2002, 2004); Baron (2000); Gilligan and Krehbiel (1987, 1989) and Krishna and Morgan (2001) as both perfectly and imperfectly informed agents are allowed. We do not assume that the individual disturbances  $\delta_i$  are independent or identically distributed. These conditions allow us to use the spatial structure and investigate the local incentives for agents to move policy.

A well known condition that appears in the mechanism design literature is non exclusivity (Postlewaite and Schmeidler 1986; Palfrey and Srivastava 1987). Let  $\mathbf{s}_{-i}$  denote the profile of private signals for  $N \setminus \{i\}$  and let  $\mathbf{s}_{-ij}$  denote the profile of private signals for  $N \setminus \{i, j\}$ . The informational environment  $F(\varepsilon, \mathbf{s})$  satisfies *non-exclusivity* if for any  $i \in N$ ,  $F(\varepsilon \mid \mathbf{s}_{-i}) = F(\varepsilon \mid \mathbf{s})$  for every  $\mathbf{s}$ . A related but stronger condition, strong non exclusivity, is considered by Duggan (1997) and Baron and Meiorowitz (2006). The informational environment  $F(\varepsilon, \mathbf{s})$  satisfies *strong non-exclusivity* if for any  $i, j \in N$ ,  $F(\varepsilon \mid \mathbf{s}_{-ij}) = F(\varepsilon \mid \mathbf{s})$  for every  $\mathbf{s}$ . Thus, in a non exclusive environment any coalition of  $n - 1$  participants have collectively observed all of the available information and in a strongly non exclusive environment any coalition of  $n - 2$  participants have collectively observed all of the available information.

In our setting with quadratic loss functions, the receiver only cares about learning the distribution of the mean given  $\mathbf{s}$ . So for our purposes, we can focus on slightly weaker conditions about the conditional distributions of the expectation of  $\varepsilon$ . For any subset  $A \subset N$ , let  $\mathbf{s}_A$  denote the profile of private signals

for the participants in  $A$ . The informational environment  $F(\varepsilon, \mathbf{s})$  satisfies *mean non-exclusivity on  $A$*  if for any  $i \in A$ ,

$$\int \varepsilon dF(\varepsilon \mid \mathbf{s}_{A \setminus \{i\}}) = \int \varepsilon dF(\varepsilon \mid \mathbf{s}_A) \tag{7}$$

for every  $\mathbf{s}$ . Similarly, for any  $A \subset N$ , *mean strong non-exclusivity on  $A$*  is satisfied if for any  $i, j \in A$ ,

$$\int \varepsilon dF(\varepsilon \mid \mathbf{s}_{A \setminus \{i, j\}}) = \int \varepsilon dF(\varepsilon \mid \mathbf{s}_A) \tag{8}$$

for every  $\mathbf{s}$ . In most published work on the spatial model it is assumed that informed agents observe perfect signals, and in this case the term mean in the above conditions is extraneous.

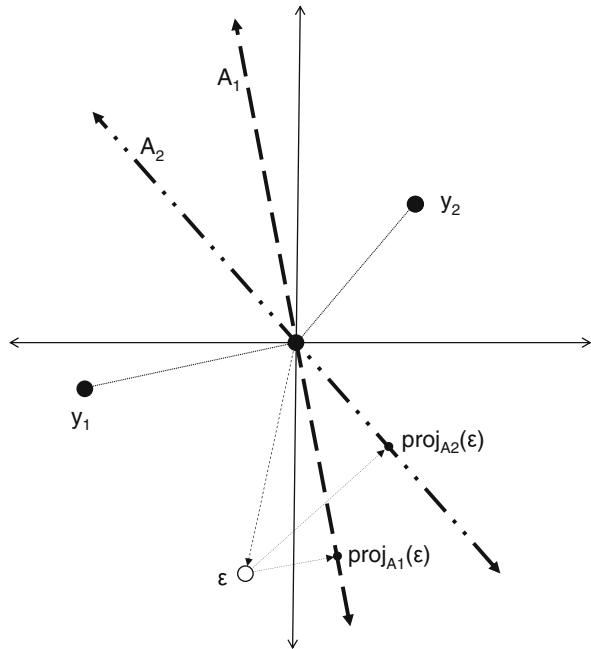
We cannot focus just on the informational environment. In addition we need to consider joint conditions on the information environment and the preference profile,  $\mathbf{y}$ . For any subspace  $X$  of  $\mathbb{R}^d$  let  $\text{proj}_X(s_i)$  denote the projection of  $s_i$  on  $X$ . For any  $A \subset N$ , we say that  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$  satisfies *minimal alignment on  $A$*  and  $x$  if there exists a set of subspaces  $\{X_i\}_{i \in A}$  s.t. (1)

$$\int \varepsilon dF(\varepsilon \mid \{\text{proj}_{X_i}(s_i)\}_{i \in A}) = \int \varepsilon dF(\varepsilon \mid \mathbf{s}_A) \tag{9}$$

for each  $\mathbf{s}$  and (2) for each  $i \in A$ ,  $\text{proj}_{X_i}(y_i) = \text{proj}_{X_i}(x)$ . Minimal alignment on  $A$  and  $x$  is satisfied if it is possible to divide up the information contained in  $\mathbf{s}_A$  in such a way that each agent  $i$  is only asked to report the projection of  $s_i$  onto a subspace on which she and a receiver with ideal point  $x$  have aligned preferences. Battaglini (2002) considers the case where all senders observe the same private information (so non exclusivity is satisfied on  $N$ ) and shows that with two senders possessing ideal points that are not colinear with the receivers', fully revealing equilibria exist. The construction hinges on the fact that each sender has aligned preferences with the receiver over a subspace of the outcome space and the subspaces form a basis for the entire outcome space. When each sender observes  $\varepsilon$  the requirement that ideal points are not colinear is a special case of minimal alignment. Minimal alignment can be thought of as the extension of Battaglini's condition to settings in which  $\varepsilon$  is not observed by each sender. Figure 1 illustrates an example with two senders in which information violates non exclusivity but satisfies minimal alignment at  $x = 0$ . Given the ideal points  $y_1$  and  $y_2$  minimal alignment can only be satisfied on  $N$  and  $x$  if player 1's signal allows her to infer  $\text{proj}_{A_1}(\varepsilon)$  and player 2's signal allows her to infer  $\text{proj}_{A_2}(\varepsilon)$ . In this case a receiver at  $x = 0$  can ask player 1 to announce  $\text{proj}_{A_1}(\varepsilon)$  and ask player 2 to announce  $\text{proj}_{A_2}(\varepsilon)$ . Neither player has an incentive to deviate.

This example suggests that non exclusivity is not necessary even with diverse preferences. Allowing each sender to have an informational monopoly is acceptable as long as her preferences are aligned with the receiver's preferences in a particular manner. We begin with a sufficiency result.

Fig. 1



**Proposition 2** Consider an informational environment characterized by the joint distribution  $F(\epsilon, \mathbf{s})$  and assume that the senders have ideal points  $\mathbf{y}$  and the receiver has ideal point  $x$ . Let  $A_x$  denote the set of individuals in  $N$  with ideal points not equal to  $x$ . (1) If mean strong non exclusivity on  $A_x$  is satisfied then the signaling game possesses a truthful perfect Bayesian Nash equilibrium, and if in addition the ideal points  $\mathbf{y}$  are such that  $x \in \mathbb{R}^d$  is a median in all directions then the  $\langle F(\epsilon, \mathbf{s}), \mathbf{y} \rangle$ -deliberation game possesses a truthful deliberative equilibrium. (2) If minimal alignment on  $A_x$  and  $x$  is satisfied then the signaling game possesses a truthful perfect Bayesian Nash equilibrium, and if in addition the ideal points  $\mathbf{y}$  are such that  $x \in \mathbb{R}^d$  is a median in all directions then the  $\langle F(\epsilon, \mathbf{s}), \mathbf{y} \rangle$ -deliberation game possesses a truthful deliberative equilibrium.

*Proof*

- (1) For signaling games the result is an immediate consequence of Proposition 3 in Baron and Meiwitz (2006). To see this consider a game between the senders  $A_x$  and a receiver that knows  $\mathbf{s}_{N \setminus A_x}$  and assume that the random shock is just the expectation of  $\epsilon$ . Mean strong non exclusivity in the signaling game corresponds to strong non exclusivity in this new signaling game, and Lemma 3 shows that this game has a truthful perfect Bayesian equilibrium. The construction relies on beliefs which render any unilateral deviation inconsequential. Given this the result for deliberation games follows from Proposition 1 above.

- (2) The proof is by construction. Assume that minimal alignment on  $A$  and  $x$  is satisfied. By this condition, there exists a list of subspaces  $\{X_i\}_{i \in A_x}$  s.t.

$$\int \varepsilon dF(\varepsilon \mid \{proj_{X_i}(s_i)\}_{i \in A_x}) = \int \varepsilon dF(\varepsilon \mid \mathbf{s}_{A_x}). \tag{10}$$

Let

$$\eta^E(\varepsilon \mid \mathbf{m}) = F(\varepsilon \mid \{proj_{X_i}(m_i)\}_{i \in A}, \mathbf{m}_{N \setminus A_x}). \tag{11}$$

By minimal alignment, given truthful strategies this defines a consistent belief for every possible  $\mathbf{m}$ . By lemma 3, the policy function is

$$p(\mathbf{m}) = x - \int \varepsilon d\eta^E(\varepsilon \mid \mathbf{m}), \tag{12}$$

so no participant in  $N \setminus A_x$  has an incentive to deviate from a truthful message as the policy is optimal given the group information. To show that no unilateral deviation is desirable assume that for  $j \in A_x$  it is the case that  $N \setminus \{j\}$  are truthful. Also fix  $s_j$  and consider a deviation  $m'_j \neq s_j$  that improves  $j$ 's utility. By (12),  $p(\mathbf{s}_{-j}, m_j)$  solves

$$\min_z \left\{ proj_{X_j} \left( \left\| x - z - \int \varepsilon d\eta^E(\varepsilon \mid \mathbf{s}_{-j}, m_j) \right\| \right) \right\} \tag{13}$$

for each value of  $\mathbf{s}_{-j}$ . By condition (2) of minimal alignment,  $proj_{X_i}(y_i) = proj_{X_i}(x)$ , which means that any announcement  $m_j$  satisfying  $proj_{X_j}(m_j) = proj_{X_j}(s_j)$  solves

$$\min_{m_j} \left\{ proj_{X_j} \left( \left\| y_i - p(\mathbf{s}_{-j}, m_j) - \int \varepsilon d\eta^E(\varepsilon \mid \mathbf{s}_{-j}, m_j) \right\| \right) \right\}. \tag{14}$$

Thus  $m_j = s_j$  solves this problem. By (11)  $j$ 's message only influences the policy choice through its influence on  $proj_{X_j}(m_j)$ . By (12), the assumption that  $N \setminus \{j\}$  are truthful and condition (1) of minimal alignment imply that for each  $\mathbf{s}_{-j}$ ,  $p(\mathbf{s}_{-j}, s_j)$  and  $p(\mathbf{s}_{-j}, m'_j)$  differ only on  $X_j$ . Thus, such an  $m'_j$  cannot exist. Given this the result for deliberation games follows from Proposition 1 above.  $\square$

The converse of this proposition is not true. Krishna and Morgan (2001) analyze a game in which neither strong non exclusivity nor minimal alignment are satisfied. Their example does, however, satisfy non exclusivity and this is critical to the equilibrium construction. The receiver, can detect when at least one sender is lying and chooses policy to punish this behavior. We now focus on a necessity result. This requires combining non exclusivity and minimal alignment. Again letting  $A_x$  denote the agents with ideal points other than  $x$ , we say  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$  satisfies *divisibility* if there exist two (not necessarily disjoint) subsets of  $A_x$ , denoted  $B$  and  $C$  such that (1) minimal alignment is satisfied

on  $B$  and  $x$ , (2) mean non exclusivity is satisfied on  $C$  and (3) the vectors of private signal profiles from these groups plus  $N \setminus A_x$ ,  $(\mathbf{s}_B, \mathbf{s}_C, \mathbf{s}_{N \setminus A_x})$  is sufficient to predict the expectation of  $\varepsilon$ ,

$$\int \varepsilon dF(\varepsilon \mid \mathbf{s}_{N \setminus A_x}, \mathbf{s}_B, \mathbf{s}_C) = \int \varepsilon dF(\varepsilon \mid \mathbf{s}). \tag{15}$$

for every  $\mathbf{s}$ .

**Proposition 3** *If the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y}, x \rangle$ -signaling game possesses a truthful perfect Bayesian Nash equilibrium then divisibility is satisfied.*

*Proof* Suppose that there is a truthful equilibrium in the signaling game and divisibility is not satisfied. Since divisibility fails, for any  $B \subset A_x$  on which minimal alignment is satisfied and  $C \subset A_x$  on which mean non exclusivity is satisfied it is the case that

$$\int \varepsilon dF(\varepsilon \mid \mathbf{s}_{N \setminus A_x}, \mathbf{s}_B, \mathbf{s}_C) \neq \int \varepsilon dF(\varepsilon \mid \mathbf{s}) \tag{16}$$

for some  $\mathbf{s}$ . However, since a truthful equilibrium exists in the  $\langle F(\varepsilon, \mathbf{s}), \mathbf{y} \rangle$ -signaling game it is the case that for at least one such selection of  $B$  and  $C$  it is the case that a non-empty set of agents,  $R$ , that don't view  $x$  as optimal and are not in  $B$  or  $C$  (i.e.  $R = N \setminus \{(N \setminus A_x) \cup B \cup C\}$ ), are willing to reveal their private information and this information influences the final policy for some values of  $\mathbf{s}$ . Since divisibility is not satisfied, if we take  $B, C, R$  and move agents around to construct sets  $B^*, C^*, R^*$  such that  $R^*$  is a smallest set containing agents that cannot be moved to  $B^*$  or  $C^*$  while maintaining the assumption that minimal alignment is satisfied on  $B^*$  at  $x$  and mean non-exclusivity is satisfied on  $C^*$  the resulting  $R^*$  is non empty. Specifically, let  $\mathbb{B}$  denote the set of binary partitions of  $N \setminus A_x$  into sets  $B'$  and  $C'$  with minimal alignment satisfied on  $B'$  at  $x$  and non exclusivity satisfied on  $C'$ . For each pair of sets  $B'$  and  $C'$ , define  $R' = N \setminus \{(N \setminus A_x) \cup B' \cup C'\}$ . By divisibility  $R'$  is non-empty. Since  $N \setminus A_x$  is finite the set  $\mathbb{B}$  is finite and thus there exists a non-empty collection of elements of  $\mathbb{B}$  which minimize the cardinality of  $R', \#R'$ . Let  $B^*, C^*$  be an element of this collection. Since we have assumed a truthful equilibrium exists it must be the case that in a signaling game between the agents  $R^*$  and a receiver with ideal point  $x$  observing  $(\mathbf{s}_{N \setminus A_x}, \mathbf{s}_{B^*}, \mathbf{s}_{C^*})$  a truthful equilibrium exists. This is true because in a truthful equilibrium the receiver does observe  $(\mathbf{s}_{N \setminus A_x}, \mathbf{s}_{B^*}, \mathbf{s}_{C^*})$ . To derive a contradiction from this conclusion we consider such a signaling game and the incentives of the senders in  $R^*$ . Consider an agent  $i \in R^*$  who's information is not redundant, meaning that for some  $\mathbf{s}$

$$\int \varepsilon dF(\varepsilon \mid \mathbf{s}_{N \setminus A_x}, \mathbf{s}_{B^*}, \mathbf{s}_{C^*}, \mathbf{s}_{R^* \setminus \{i\}}) \neq \int \varepsilon dF(\varepsilon \mid \mathbf{s}). \tag{17}$$

Such an  $i$  must exist or else we will have shown that divisibility is satisfied. In this game assume that all senders  $j \in R^* \setminus \{i\}$  are truthful. Since  $i \in R^*$  it is the case that (1)  $i \in A_x$  and thus  $y_i \neq x$  and (2) it is not possible to find a set of agents that observe the information contained in  $s_i$  and on which mean non exclusivity is satisfied. Given that  $s_i = \varepsilon + \delta_i$  these two conclusions and Lemma 3 imply that for some subspace  $X$  of  $\mathbb{R}^d$ , in the truthful equilibrium

$$p^*(\mathbf{m}_{-i}, m_i) = x - \int \varepsilon dF(\varepsilon \mid \mathbf{s}_{-i}, \text{proj}_X(m_i)). \tag{18}$$

Since  $i$  has no incentive to be dishonest it must be the case that

$$\left\| y_i - x - \int \int \varepsilon dF(\varepsilon \mid \mathbf{s}_{-i}, \text{proj}_X(m_i)) dF(\mathbf{s}_{-i} \mid s_i) \right\| \tag{19}$$

is optimized by  $m_i = s_i$ . Given the assumptions on the distributions,  $\int \int \varepsilon dF(\varepsilon \mid \mathbf{s}_{-i}, \text{proj}_X(m_i)) dF(\mathbf{s}_{-i} \mid s_i)$  is continuous in  $m_i$ . This and the fact that  $m_i = s_i$  is an optimizer means that  $\text{proj}_X(x) = \text{proj}_X(y_i)$ . But this implies that  $i$  can be added to the set  $B^*$ , contradicting the fact that  $B^*, C^*$  solve the minimization problem defined above. Thus, divisibility is satisfied or the truthful equilibrium does not exist.  $\square$

Note that divisibility uses mean non exclusivity and not mean strong non exclusivity and thus Propositions 2 and 3 do not provide a tight characterization. A second point worth noting is that Proposition 2 does not require  $s_i = \varepsilon + \delta_i$  or the absolute continuity assumptions. Proposition 3 does, however, rely on these assumptions. Without them it is possible to come up with settings that posses truthful equilibria but violate divisibility. One unidimensional example involves one sender with ideal point  $y_1 = 1$ , a receiver with ideal point  $x = 0$ , a shock taking possible values  $\varepsilon \in \{-3, 3\}$ , and a perfectly informative signal  $s_1 = \varepsilon$ . If the sender is truthful, and the receiver selects a sequentially rational policy given the message the sender’s utility is 1 in either state. However, a deviation by the sender results in a sender utility of either  $-49$  or  $-25$  depending on the realization of  $\varepsilon$ . Thus, a truthful equilibrium exists but divisibility is not satisfied. It should also be noted that the sufficiency part of Proposition 2 can be extended to a modified version of divisibility – with the second condition using mean strong non-exclusivity. This result follows from Proposition 2, if we consider two separate signaling games, one between the receiver and the agents on which mean strong non exclusivity is satisfied, and the other between the receiver and the agents on which minimal alignment is satisfied.

### 5 Conclusion

Bargaining problems in which agents posses private information and communicate may posses large equilibrium sets. Moreover, in these problems it is difficult to assess the extent to which information sharing is possible. However, when

agents are patient and preferences satisfy the Plott conditions, we can answer questions about the possibility of full information revelation by analyzing simpler sender-receiver models. It is easy to demonstrate this point in the case of a unidimensional policy space and smooth shocks. Cheap talk communication and bargaining can result in policy selection that is optimal for the median committee member only if all pieces of information are observed by at least two committee members. Equivalently in sender–receiver models like Krishna and Morgan (2001) in which the players have distinct ideal points on the line, fully-revealing equilibria only exist if any information that is observed by one sender and not the receiver is also observed by another sender. A second informative example involves a two dimensional policy space with five committee members possessing the ideal points  $y_0 = (0, 0)$ ,  $y_1 = (2, 0)$ ,  $y_2 = (1, 2)$ ,  $y_3 = (-1, 0)$ ,  $y_4 = (-2, -4)$ . Is there an equilibrium to the communication and bargaining game which aggregates all of the available private information to select agent 0's favorite policy,  $-\int \varepsilon dF(\varepsilon \mid \mathbf{s})$ ? We find that such an equilibrium exists in the bargaining and communication game if and only if there is a truthful equilibrium in a signaling game in which agents 1,2,3,4, are senders and agent 0 is the receiver. This is the case if, for example, each dimension of the shock is observed by three agents or one of the odd indexed agents observes the first coordinate and one of the even indexed agents observes the second coordinate. In general, combinations of non exclusivity and preference alignment conditions are necessary for truthful equilibria.

While progress has been made in understanding when truthful equilibria exist for “nice preference profiles”, this paper addresses only a small set of the questions pertaining to policymaking in the spatial model. Since the presence of a non-empty majority rule core is non-generic, questions about the possibility of aggregation when the Plott conditions are not satisfied need to be answered. While Banks and Duggan (2000) present results about the upper hemicontinuity of the equilibrium correspondence, the approach taken here does not seem particularly applicable to the study of communication and bargaining in settings that are “close” to ones in which the Plott conditions are satisfied. Results about profiles that do not satisfy the Plott conditions are likely to hinge on analysis of partially revealing equilibria, a direction that is left for future work.

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## References

- Austen-Smith D, Feddersen T (2003a) Deliberation and voting rules. Northwestern University Typescript
- Austen-Smith D, Feddersen T (2003b) The inferiority of deliberation under unanimity rule. Northwestern University Typescript
- Baliga S, Morris S (2002) Co-ordination, spillovers, and cheap talk. *J Econ Theory* 105:450–468
- Banks J, Duggan J (2000) A bargaining model of collective choice. *Am Polit Sci Rev* 94(1):73–88
- Banks J, Duggan J (2004) A social choice lemma on voting over lotteries with applications to a class of dynamic games. *Soc Choice Welfare* (forthcoming)

- Baron DP (2000) Legislative Organization with Informational Committees. *Am J Polit Sci* 44(3):485–505
- Baron D, Ferejohn J (1989) Bargaining in Legislatures. *Am Polit Sci Rev* 83:1181–206
- Baron D, Kalai E (1993) The simplest equilibrium of a majority rule division game. *J Econ Theory* 61:290–301
- Baron DP, Meirowitz A (2006) Fully-revealing equilibria of multiple-sender signaling and screening models. *Soc Choice Welfare* 26:455–470
- Battaglini M (2002) Multiple referrals and multidimensional cheap talk. *Econometrica* 70:1379–1401
- Battaglini M (2004) Policy advice with imperfectly informed agents. *Adv Theoretical Econ* 4(1)
- Bendor J, Meirowitz A (2004) Spatial Models of Delegation. *Am Polit Sci Rev* 98:293–310
- Coughlan PJ (2000) In Defense of Unanimous Jury Verdicts: Mistrials, Communication, and Strategic Voting. *Am Polit Sci Rev* 94:375–393
- Crawford VP, Sobel J (1982) Strategic Information Transmission. *Econometrica* 50(6):1431–1451
- Duggan J (1997) Virtual bayesian implementation. *Econometrica* 65(5):1175–1199
- Fishkin JS (1991) Democracy and deliberation: new directions for democratic reform. Yale University Press, New Haven
- Gerardi D, Yariv L (2003) Putting your ballot where your mouth is: an analysis of collective choice with communication. Yale University Typescript
- Gilligan TW, Krehbiel K (1987) Collective decision-making and standing committees: an informational rationale for restrictive amendment procedures. *J Law Econ Organ* 3(2):287–335
- Gilligan TW, Krehbiel K (1989) Asymmetric information and legislative rules with a heterogeneous committee. *Am J Polit Sci* 33(2):459–90
- Gutmann A, Thompson D (1996) Democracy and Disagreement. Belknap, Harvard Press, Cambridge
- Kim J (2005) Pe-play communication in games of two-sided incomplete information. University of Rochester Typescript
- Krishna V, Morgan J (2001) Asymmetric information and legislative rules: some amendments. *Am Polit Sci Rev* 95(2):435–452
- Palfrey TR, Srivastava S (1987) On bayesian implementable allocations. *Rev Econ Stud* 54:193–208
- Plott C (1967) A notion of equilibrium and its possibility under majority rule. *Am Econ Rev* 57:787–806
- Postlewaite A, Schmeidler D (1986) Implementation in differential information economies. *J Econ Theory* 39:14–33
- Meirowitz A (2003) In defence of exclusionary deliberation: communication and voting with private beliefs and values. *J Theor Polit* (in press)
- Meirowitz A (2006) Designing institutions to aggregate preferences and information. *Q J Polit Sci* 1(4):373–392
- Myerson R (1979) Incentive compatibility and the bargaining problem. *Econometrica* 47:61–73
- Myerson R (1982) Optimal coordination mechanisms in generalized principal-agent problems. *J Math Econ* 10:67–81