Spatial Sorting:
Why New York, Los Angeles and Detroit
attract the greatest minds as well as the unskilled

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Abstract

We propose a theory of skill mobility across cities. It predicts the well documented city size–wage premium: the wage distribution in larger and more productive cities first-order stochastically dominates that in less productive cities. Yet, because this premium reflects higher house prices, this does not necessarily imply that this stochastic dominance relation also exists in the distribution of skills. Our model predicts that instead of first-order, there is second-order stochastic dominance in the skill distribution. The demand for skills is non-monotonic as our model predicts a “Sinatra” as well as an “Eminem” effect: both the very high and the very low skilled disproportionately sort into the biggest cities, while those with medium skill levels sort into small cities. Based on our theory, the pattern of spatial sorting is explained by a simple technology with varying elasticity of substitution by skill. Using CPS data on wages and Census data on house prices, this technology with the elasticity of substitution decreasing in skill density is consistent with the observed patterns of skills.


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1 Introduction

New York, NY. Making it there rather than in Akron, OH is the ultimate aim of many professionals. And this is true for many trades and skills: artists, musicians, advertising and media professional, consultants, lawyers, financiers,... While there are certainly notable exceptions (the IT sector comes to mind), most people can provide casual evidence that the skill level in the top percentiles of NY and large cities in general is higher than anywhere else. Yet, to date there is little or no empirical evidence to back this up. While there is certainly ample evidence of a city-size wage premium, there is little evidence of sorting of both the skilled and the unskilled across different size cities (see for example Baum-Snow and Pavan (2010a,b)).

In this paper we show that there is indeed evidence that disproportionately more skilled citizens locate in larger cities. However, we provide a key new insight: larger cities also disproportionately attract lower skilled agents. And it turns out that large cities like New York and Detroit in that respect are more similar to each other than to small cities. For example, we find that New York city attracts the low skilled as well as the high skilled. Most who do not live there are usually most familiar with Manhattan, but there is a huge low skill contingent in the South Bronx and Newark. And likewise Detroit, the 14th largest metro area in 2009 has disproportionately many low skilled individuals and a reputation for inner city poverty and low skilled work. Yet, quite contrary to most common preconceived notions, the Detroit metro area also disproportionately attracts high skilled individuals. We show that there is a systematic pattern of fat tails in the skill distribution of large cities. To our knowledge, the relation between city size and the disproportionate presence of both the high and the low skilled has not been documented in the literature.

As will become apparent, it is precisely the fact that large cities attract the low skilled citizens as well as the high skilled that explains why to date little or no evidence has been found on sorting. Our finding thus also encompasses a methodological contribution. In the literature, skills are often partitioned into two classes,\(^1\) which allows for inference of a linear approximation when the underlying relation is monotonic. However, in the case of skills across cities, the equilibrium skill quantity relative to the economy-wide quantity is essentially non-monotonic: the skill demand in large cities relative to small ones is U-shaped as large cities disproportionately attract both high and low skilled workers, but not those with medium skill levels. There is no hope to satisfactorily identify this non-monotonic relation with two points only. Our approach is to allow for many skill classes, in fact, as many as there are observations. We can thus characterize a smooth distribution of skills.

\(^1\)The same is true when the focus is on occupations instead of skills. Gould (2007) partitions the set of workers into blue and white collar occupations.
The city-size wage premium is well documented. For example, the gap between average wages in the smallest cities in our sample (with a population around 160,000, more than 100 times smaller than New York) and the largest cities is 25%. Below in Figure 1.A, we plot a kernel of the wage distribution of those living in all cities larger than 2.5 million inhabitants and that of those in cities smaller than one million inhabitants. Not only are average wages higher, there is a clear first-order stochastic dominance relation. At all wage levels, more people earn less in small cities than in large cities. This clearly indicates that there is a city-size wage premium across the board. Of course, larger cities tend to be more expensive to live, so in order to be able to compare skill distributions, we need to adjust for house prices. Identical agents will make a location choice based on the utility obtained, which depends both on wages and the cost of housing. Indifference for identical agents will therefore require equalizing differences. We use homothetic preferences to adjust for housing consumption and construct a house price index based on a hedonic regression to calculate the difference in housing values across cities. The resulting distribution of utilities will therefore be isomorphic to the distribution of skills in a world with full mobility and no market frictions. Figure 1.B displays the kernel of the skill distribution. The skill distribution in larger cities has fatter tails both at the top and at the bottom of the distribution. Large cities disproportionately attract more skilled and more unskilled workers. Figure 1.D illustrates that this implies a non-monotonic relative demand for skills in equilibrium, whereas the relative wages are monotonic (Figure 1.C).

We propose a simple theory of city choice and heterogeneous skills. The role of citizens is to earn a living based on a competitive wage, and under perfect mobility, agents need to be indifferent between different consumption-housing bundles, and therefore between different wage-house price pairs. Wages are generated by firms that compete for labor and that have access to a city-specific technology summarized by that city’s total factor productivity (TFP). Output is produced with heterogeneous labor inputs. It values higher skills, but the marginal product of labor is decreasing in the number of workers hired of that skill level. As a result, given a vector of wages, firms want to hire a combination of different skills. Apart from differences in TFP, the technology is the same across cities. The labor aggregating technology of different skilled workers is the Varying Elasticity of Substitution (VES) technology. It is similar to the Constant Elasticity of Substitution (CES) technology, but the exponent on the quantity (and therefore the marginal product) is allowed to vary by skill. As a result, the elasticity of substitution is varying.

For the general technology – both CES and VES –, the size of the city will typically be increasing with TFP and we can establish that wages are higher in larger cities. Firms in high TFP cities are more productive and can attract workers paying higher wages. In equilibrium, labor demand will also push up house prices. The citizens’ location decision will equalize utility and a worker of a given skill will be indifferent between a high wage, high house price city and a low wage, low house price city.

The shape of the distribution is crucially determined by the technology. In the benchmark case of CES, cities of different TFP have different population sizes, but the distribution of skills is the
Figure 1: Left-to-right-top-to-bottom. A. Wage distribution for small and large cities; B. Skill distribution for small and large cities; C. Relative wages between large and small cities; D. Relative demand for skills between large and small cities.

same across cities, and for that matter across the entire economy. In contrast, when the elasticity of substitution is decreasing in the measure of a given skill, then larger cities have skill distributions with fatter tails.

The primitive of our model is city-specific total factor productivity. Like in models of growth, this is likely to be generated in part endogenously. It thus consists of both a pure productivity portion as well as a portion that is ascribed to externalities from agglomeration, the presence of amenities,\textsuperscript{2} We propose a micro-foundation for this particular VES technology. Consider the standard CES technology with in addition knowledge spillovers between workers of different skill levels. People randomly meet someone with a different skill level in the city and benefit from some newly acquired knowledge as a result. They can only learn from differently skilled types. As a result, those in scarce skills are

\textsuperscript{2}While realistically it is determined endogenously, for the purpose of our model we take it is as given and assume it is not affected directly by investment by individuals or institutions. For example, a local government may be able to affect its city-specific TFP through investment, for example in local transportation or the construction of an airport.
more likely to meet a different skilled type and therefore benefit more from the spillover than those in abundant skills. As a result, the marginal product of the scarce skilled types is larger.

The key feature of our approach is to use revealed preference choice of location and wages paid to back out skills. This is in contrast to the commonly used approach of using observable skills (levels of education, test scores,...). One reason for doing things this way is that observable skills only explain a fraction of skills (see for example Keane and Wolpin (1997)). Moreover, skill categories are typically very coarse, and given the non-monotonicity observed using our approach – that relative to small cities, the equilibrium demand for skills in large cities is U-shaped in skill – identifying this non-monotonicity from coarse data is challenging for the obvious reasons mentioned above.

In addition to our wage based measure, we also derive the skill distribution based on observable skill, either by schooling category or actual years of schooling, derived from self-reported educational attainment in the CPS data. We find the same qualitative prediction of fatter tails and second order stochastic dominance in larger cities. With the objective of providing external validation, we further use the observable skill categories to calculate the determinants of the technology and how they vary by skill. We find that the marginal product (and therefore the elasticity of substitution) is higher for the scarce skills, i.e., both for the highest and the lowest skills. This U-shaped pattern is precisely the driving force in our theory behind the fat tailed skill distribution.

2 Related Literature

The model we propose builds on the urban location model in Eeckhout (2004) and Davis and Ortalo-Magné (2009) where identical citizens who have preferences over consumption and housing choose a city in order to maximize utility. Because of differences in productivity across cities, wages differ and house prices adjust in function of the population size of the city. Productivity differences are due to TFP and agglomeration effects. Given perfect mobility and identical agents, utility equalizes across cities. Here we add heterogeneity in the inputs of production (skills) which gives rise to a distribution of skills within the city. The production technology aggregates different skilled inputs within a firm without assuming a constant elasticity of substitution technology as in Eeckhout and Pinheiro (2010). Equilibrium is determined by the sorting decision of agents. The work by Behrens, Duranton and Robert-Nicouud (2010) also analyzes sorting of heterogeneous agents into cities. They find that more productive workers locate in large cities and less productive workers in small cities. As a result, they predict as we do the effect in the upper tail, however not that in the lower tail.

Our empirical exercise compares the entire distribution of real wages across cities of different sizes in the United States. We are not the first to study wages across cities. Behrens, Duranton and Robert-Nicouud (2010) regress log nominal wages on log city size across 276 MSA areas using 2000 Census data. They find an average urban premium of 8% without controlling for talent, measured by education, and 5% when controlling for it. In addition, they regress housing costs on city size using both rental prices
and an index formed of rental price and housing values of owner-occupied units. They find similar coefficients for housing costs as for nominal wages, suggesting that there is no substantial difference in real wages. This is consistent with our finding that the mean of house-price adjusted wages is the same. They do not analyze the higher variance in larger cities.

Moretti (2010) calculates real urban wages using wage data across 315 MSAs using the 1980, 1990 and 2000 Census and focusses on the change in inequality over time. He compares two different local price indices, one based on rental prices only and one including local differences for consumption goods. The latter being based on BLS data for the 23 largest MSAs. Real wages are calculated as the nominal wage divided by one of local price indices and then used to estimate the wage difference between workers with a high school degree and workers with college or more. He finds that the cost of living has gone up more for college graduates and as a result, real wage inequality has increases less than nominal wage inequality.

Baum-Snow and Pavan (2010b) use wages from the 1980, 1990 and 2000 Census (5% PUMS) plus the 2005-2007 American Community Surveys (ACS). Wages are deflated for inflation but not for local differences in housing prices. They document that the variance of hourly wages in increasing with city size. This relationship is weak in 1980 and increases steadily until 2007. Baum-Snow and Pavan (2010a) in addition use the local cost-of-living index from the Commerce Research Association (ACCRA) for 244 metropolitan areas and 179 rural counties 2000 to 2002. Real wages are then used to estimate both log wage level and log wage growth differences across city size groups. They also control for different education groups. They find that real wages are up to 30% higher in MSAs of over 1.5 million inhabitants than rural areas. Baum-Snow and Pavan (2010a) does not study the variance of real wages.

Albouy (2008) calculates real urban wages for 290 MSAs using the 2000 Census (5% IPUMS). Nominal wages are deflated using rental prices from the Census and local prices for consumption goods. The ACCRA Cost-of-Living index is the basis of the latter but not directly used because of its limited quality. Albouy regresses the ACCRA index on local rental prices and uses the predictions as index for local cost-of-living differences. Differences in real wages across MSAs are interpreted as quality-of-live differences. He finds that controlling for local differences in federal taxes, non-labor income and observable amenities such as seasons, sunshine, and coastal location, quality of life does not depend on city size.

All this body is consistent with our finding that the average of the skill distribution is remarkably constant across different size cities. Of course, that does not allow us to conclude that there is no sorting or that there is sorting of high skilled workers in large cities and low skilled workers in small cities. As we will show below, quite to the contrary. The mean is constant across cities of different size, but the variance is significantly increasing. The latter indicates an important role of sorting of high and low types into large cities and of medium types into small cities.

Our findings are also related to the previous literature on variations of skill distributions across city sizes. Bacolod, Blum and Strange (2009) studied the difference in skill distributions across city sizes,
using jointly Census and NLSY data and the Dictionary of Occupational Titles (DOT), defining skills as a combination of qualities instead of just education. They found a small variation in cognitive, people, and motor skills across city sizes, which they attributed to skills being defined nationally, not being able to address local differences in occupations’ requirements of skills. Once they look at differences in Armed Forces Qualification Test (AFQT) and Rotter Index - measures of intelligence and social skills, respectively - they found that, even though the average scores were quite similar across city sizes, the scores at large cities for the lowest scores (10th percentile) were much lower than the ones at small cities. Similarly, the highest scores (90th percentile) were much higher in large cities than small ones. These results corroborate the idea that we have fat tails in the distribution of skills, even though differences in average skill may be small.

3 The Model

Population. Consider an economy with heterogeneously skilled workers. Workers are indexed by a skill type $i$. For now, let the types be discrete: $y_i, i \in \mathcal{I} = \{1, ..., I\}$, where the skill level $y_i$ is increasing in $i$. Denote the country-wide measure of skills of type $i$ by $M_i$. Let there be $J$ locations (cities) $j \in \mathcal{J} = \{1, ..., J\}$. The amount of land in a city is fixed and denoted by $H_j$. Land is a scarce resource, and it will be assumed that the total stock of land available is for residential use.

Preferences. Citizens of skill type $i$ who live in city $j$ have preferences over consumption $c_{ij}$, and the amount of land (or housing) $h_{ij}$. The consumption good is a numeraire good with price equal to one. The price per unit of land is denoted by $p_j$. We think of the expenditure on housing as the flow value that compensates for the depreciation, interest on capital,... In a competitive rental market, the flow payment will equal the rental price. A worker of type $i$ has consumer preferences in city $j$ that are represented by:

$$u(c_{ij}, h_{ij}) = c_{ij}^{1-\alpha} h_{ij}^\alpha$$

where $\alpha \in [0, 1]$. Workers and firms are perfectly mobile, so they can relocate instantaneously and at no cost to another city. Because workers with the same skill are identical, in equilibrium each of them should obtain the same utility level wherever they choose to locate. Therefore for any two cities $j, j'$ it must be the case that:

$$u(c_{ij}, h_{ij}) = u(c_{ij}', h_{ij}')$$

for all skill types $\forall i \in \{1, ..., I\}$.

Technology. Cities differ in their total factor productivity (TFP) which is denoted by $A_j$. We treat this

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3We will abstract from the housing production technology, for example we can assume that the entire housing stock is held by a zero measure of landlords.
as exogenous and represents a city’s productive amenities, infrastructure, historical industries,...⁴. In each city, firms compete to operate in this market. Firms all assumed to be identical and to have access to the same, city-specific TFP. Output is produced from choosing the right mix of different skilled workers $i$. For each skill $i$, a firm in city $j$ chooses a level of employment $m_{ij}$ and produces output

$$A_j \sum_{i=1}^{I} (m_{ij})^{\gamma_i} y_i^\beta,$$

where $\gamma_i$ is skill-dependent. When $\gamma_i$ is constant for all $i$, this technology is the standard CES (constant elasticity of substitution). Because $\gamma_i$ is skill-varying, we refer to this technology as VES (varying elasticity of substitution). Firms pay wages $w_{ij}$ for workers of type $i$. It is important to note that wages will depend on the city $j$ because citizens freely locate between cities not based on the highest wage, but given house price differences, based on the highest utility.

Entry into the market entails a cost $k p_j$. We assume that the entry cost are city specific and depend on housing prices. Firms need to rent housing space for production and house prices affect the expenditure (e.g., municipal taxes) that a firm incurs to finance infrastructure. Competitive entry will drive down profits to zero, which are given by:

$$A_j \sum_{i=1}^{I} (m_{ij})^{\gamma_i} y_i^\beta - \sum_{i=1}^{I} w_{ij} m_{ij} - k p_j = 0.$$

The measure of firms entering the market in city $j$ is denoted by $N_j$ and is determined by this zero profit condition and the market clearing conditions below.

**Market Clearing.** In the housing market of each city $j$, market clearing in the housing market requires:

$$\sum_{i=1}^{I} h_{ij} m_{ij} = \frac{H_j}{N_j}, \forall j.$$

In the country-wide market for skilled labor, markets for skills clear market by market:

$$\sum_{j=1}^{J} N_j m_{ij} = M_i, \forall i.$$

## 4 The Equilibrium Allocation

**The Citizen’s Problem.** Within a given city $j$ and given a wage schedule $w_{ij}$, a citizen chooses consumption bundles $\{c_{ij}, h_{ij}\}$ to maximize utility subject to the budget constraint (where the tradable

⁴We assume this exogenous because our focus is on the allocation of skills across cities, but one can easily think of this being the outcome of investment choices made by firms, local governments,...
consumption good is the numeraire, i.e. with price unity)

\[
\max_{\{c_{ij}, h_{ij}\}} u(c_{ij}, h_{ij}) = c_{ij}^{1-\alpha} h_{ij}^\alpha \\
\text{s.t. } c_{ij} + p_j h_{ij} \leq w_{ij}
\]

for all \(i,j\). Solving for the competitive equilibrium allocation for this problem we obtain:

\[
c_{ij} = (1 - \alpha) w_{ij} \\
h_{ij} = \alpha \frac{w_{ij}}{p_j}
\]

Substituting the equilibrium values in the utility function, we can write the indirect utility for a type \(i\) as:

\[
U_i = \alpha^\alpha (1 - \alpha)^{1-\alpha} \frac{w_{ij}}{p_j^\alpha} \Rightarrow w_{ij} = U_j p_j^\alpha K,
\]

where \(K = 1/\alpha^\alpha (1 - \alpha)^{1-\alpha}\). This allows us to link the wage distribution across different cities \(j,j'\).

Wages across cities relate as:

\[
w_{ij} = w_{ik} \left( \frac{p_j}{p_{j'}} \right)^\alpha.
\]

The Firm’s Problem. Given the city production technology, a firm’s problem is given by:

\[
\max_{m_{ij}, \forall i} A_j \sum_{i=1}^I (m_{ij})^\gamma_i y_i^\beta - \sum_{i=1}^I w_{ij} m_{ij} - kp_j \\
\text{s.t. } m_{ij} \geq 0, \forall i
\]

The first-order condition is:\footnote{In what follows, the non-negativity constraints on \(m_{ij}\) will be dropped since the marginal product at zero tends to infinity whenever \(\gamma_i\) and \(A_j\) are positive.}

\[
\gamma_i A_j (m_{ij})^{\gamma_i-1} y_i^\beta = w_{ij}, \forall i.
\]

All firms are price-takers and do not affect wages. Wages are determined simultaneously in each submarket \(i,j\). Even without fully solving the system of equations for the equilibrium wages, observation of the first-order condition reveals that productivity between different skills \(i\) in a given city are governed by two components: 1. the productivity \(y_i\) of the skilled labor and how fast it changes between different \(i\) (determined by \(\beta\)); and 2. the measure of skills \(m_{ij}\) employed (wages decrease in the measure employed from the concavity of the technology).

We take the view that wages are monotonic in skills.\footnote{Whenever the density is upward sloping, then the second effect will imply that higher skilled workers will see an increase in productivity only provided the first effect (productivity) is large enough. In fact, when \(\beta = 0\), the effect of skills is only through \(m_{ij}\) and wages will be decreasing if the density is increasing. Likewise, the first effect completely dominates when \(\beta\) tends to infinity. For every economy, there exists a critical \(\beta^*\) such that productivity (and therefore}
across cities, the utility distribution is therefore a monotonic transformation of the skill distribution. The skill distribution may have a different shape than the utility distribution, but its ordinal features are preserved. In particular, if we compare two utility distributions, the densities of which intersect twice, then also the skill densities will intersect twice. In other words, if there are fat tails in the utility distribution, then there are also fat tails in the skill distribution.

In order to simplify the exposition and the derivations, we now proceed the analysis with two cities \( j = 1, 2 \) and any number \( I \) of skills. From the labor market clearing condition and using the first-order condition in both cities we can substitute for \( m_{ij} \) to obtain:

\[
\left( \frac{w_{ij}}{\gamma_i A_j y_i^{\beta}} \right)^{\frac{1}{\gamma_i - 1}} = \frac{M_i}{N_j} - \frac{N_j'}{N_j} \left( \frac{w_{ij'}}{\gamma_i A_j y_i^{\beta}} \right)^{\frac{1}{\gamma_i - 1}}.
\]

Then we can write the wage ratio as:

\[
\frac{w_{i1}}{w_{i2}} = \frac{\left[ A_2 \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i - 1}}}{\left[ A_1 \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i - 1}}} \frac{M_i}{1 + \frac{N_i}{N_2} \left[ A_2 \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i - 1}} N_2}
\]

Since from perfect mobility in the consumer’s optimization problem we have utility equalization and as a result \( \frac{w_{i1}}{w_{i2}} = \left( \frac{p_1}{p_2} \right)^{\alpha} \), we can write the equilibrium employment levels for each skill \( i \) in both cities as:

\[
m_{i1} = \frac{\left[ A_2 \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i - 1}}}{1 + \frac{N_i}{N_2} \left[ A_2 \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i - 1}} N_2} M_i
\]

\[
m_{i2} = \frac{1}{1 + \frac{N_i}{N_2} \left[ A_2 \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i - 1}} N_2} M_i
\]

We can then express the equilibrium wages explicitly as

\[
w_{i1} = \left[ A_2 \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i - 1}} \frac{M_i}{N_2} \left( \frac{w_{i1}}{\gamma_i A_1 y_i^{\beta}} \right)^{\frac{1}{\gamma_i - 1}}
\]

equilibrium wages) is increasing in skill \( i \) in every city \( j \). We will in what follows therefore assume that productivity is monotone in skills: \( \beta > \beta^* \). This is without loss of generality if one interprets the order of skills to be determined by the marginal product. Suppose \( \beta < \beta^* \) and for some \( i \) wages decrease in skill \( i \), then one can suitably reorder skills such that wages that pay lower wages are assigned a lower index such that under the new index wages are increasing. This might be the case for the average artist or architect for example, who in terms of years of schooling are more skilled than accountants, yet they earn less (either because they are abundant or because the productivity is low). In our view of skills, the account would be more skilled than the artist.
and similarly for $w_{i2}$.

This wage equation allows us to establish the relation between skills and wages in the data. It also confirms that there is a one-to-one relation between skills and equilibrium utility $U_i$. Subject to a transformation between $w_{ij}$ and $y_i$ we can therefore without loss of generality express skill qualitatively by $U_i = \alpha^\alpha (1 - \alpha)^{1-\alpha} \frac{w_{ij}}{y_i}$.

Finally, the equilibrium is fully specified once we satisfy market clearing in the housing market in each city and we pin down the measure of firms $N_j$ from the zero profit condition. Expressing the housing market clearing condition as a ratio, we get together with the zero profit conditions:

\[
\sum_{i=1}^I \left( \frac{M_i}{N_2} \right)^{\gamma_i} \gamma_i y_i^\beta \left\{ \frac{\left[ A_i^\alpha \left( \frac{p_1}{p_2} \right)^\alpha \right]^{1 - \gamma_i}}{1 + \frac{\Delta_i^\alpha}{A_i^\alpha} \left[ \frac{p_1}{p_2} \right]^\alpha} \right\}^{\gamma_i} = \frac{H_1 A_2 N_2 p_1}{H_2 A_1 N_1 p_2} \tag{1}
\]

\[
\sum_{i=1}^I \left( \frac{M_i}{N_2} \right)^{\gamma_i} \gamma_i y_i^\beta \left\{ \frac{\left[ A_i^\alpha \left( \frac{p_1}{p_2} \right)^\alpha \right]^{1 - \gamma_i}}{1 + \frac{\Delta_i^\alpha}{A_i^\alpha} \left[ \frac{p_1}{p_2} \right]^\alpha} \right\}^{\gamma_i} = \frac{k}{A_1} p_1 \tag{2}
\]

\[
\sum_{i=1}^I \left( \frac{M_i}{N_2} \right)^{\gamma_i} (1 - \gamma_i) y_i^\beta \left\{ \frac{\left[ A_i^\alpha \left( \frac{p_1}{p_2} \right)^\alpha \right]^{1 - \gamma_i}}{1 + \frac{\Delta_i^\alpha}{A_i^\alpha} \left[ \frac{p_1}{p_2} \right]^\alpha} \right\}^{\gamma_i} = \frac{k}{A_2} p_2 \tag{3}
\]

In what follows we refer to these as the three equilibrium conditions (1)–(3).

The Main Theoretical Results. First we consider the benchmark case where the technology has a constant elasticity of substitution (CES). This provides a benchmark for our main findings about the distribution of skills across cities.

**Theorem 1** CES technology. If $\gamma_i = \gamma$ for all $i$, then the skill distribution across cities is identical.

**Proof.** In Appendix. ■

The CES technology implies that cities have identical skill compositions. This is due to the homotheticity of the CES technology: the marginal rate of technical substitution is proportional to total employment, and as a result, firms in different cities and with different technologies will employ different skills in the same proportions.

We now establish the relation between TFP and city size. Denote by $S_j$ the size of city $j$ where $S_j = \sum_{i=1}^I N_j m_{ij}$. When cities have the same amount of land, we can establish the following result for a general technology.
Proposition 1  City Size and TFP. Let $A_1 > A_2$ and $H_1 = H_2$, then $S_1 > S_2$.

Proof. In Appendix.  

We establish this result for cities with identical supply of land. Clearly, the supply of land is important in our model since a city with an extremely tiny geographical area would drive up housing prices all else equal. This may therefore make it more expensive to live even if the productivity is lower. Because in our empirical application we consider large metropolitan areas (NY city for example includes large parts of New Jersey and Connecticut with relatively low population density), we believe that this assumption is without much loss of generality.\footnote{In fact, the equal supply of housing condition is only sufficient for the proof, not necessary. However, our model does not speak to the important issue of within-city geographical heterogeneity, as analyzed for example in Lucas and Rossi-Hansberg (2002). In our application, all heterogeneity is absorbed in the pricing index by means of the hedonic regression.}

We now proceed to showing the main result. We already know that more productive cities are larger, but that does not necessarily mean that the distribution of skills in larger cities differs from that in smaller cities. In fact, it depends on the technology. We know from Theorem 1 that for the CES technology the large cities have exactly the same distribution as the smaller cities.

We therefore make the following assumption on how the coefficient $\gamma_i$ varies with $i$. Below, we provide a simple micro-foundation for this assumption.

Assumption 1 $\gamma_i$ is decreasing in the economy-wide density of skill $i$.

In other words, scarce skills have a higher $\gamma_i$ than abundant skills. This is illustrated in Figure 4. It is important to note here that $\gamma_i$ does not depend on the firm’s employment in skill $i$. This would affect the firm’s first order condition as it will take into account how the marginal product is affected by the change in $m_{ij}$. Because the firm is infinitesimally small relative to the market, it takes the aggregate employment level as given.

We can now establish the main theorem characterizing the skill distribution across firms:

Theorem 2 Fat Tails. Consider a symmetric, uni-modal skill distribution economy-wide. Then under Assumption 1, $A_1 > A_2$, and $H_1 = H_2$, the skill distribution in larger cities has fatter tails.

Proof. In Appendix.  

To see the nature of this result, consider the benchmark of CES. Homotheticity implies that even though the level of employment differs across skills, firms will always choose to hire different skills in exactly the same proportions for a given wage ratio. Since house prices affect all skills within a city in the same way, the wage ratio is unaffected. Instead, when the marginal product is higher for low and high skilled workers relative to the medium skilled, the higher TFP cities have a comparative advantage
in hiring those scarce skills relative to the abundant skills. Due to the complementarity between TFP and the labor aggregator, firms in large cities have a comparative advantage in hiring scarce skills where the marginal product is highest.

We now discuss some further implications of the model.

**Housing Consumption and Expenditure.** It is immediate from our model that in large cities, citizens will spend more on housing, yet they will consume less of it.

**Proposition 2** Let $A_1 < A_2$ and $H_1 = H_2$. For a given skill $i$, expenditure on housing $p_jh_{ij}^*$ is higher in larger cities. The size of houses $h_{ij}^*$ in larger cities is smaller.

**Proof.** From the consumer’s problem, we have: $p_jh_{ij} = \alpha w_{ij}$. Then, since we established in the proof of Proposition 1, that $w_{i1} > w_{i2}$, we must have $p_1h_{i1} > p_2h_{i2}$, $\forall i$. Similarly, from the same equality in the consumer’s problem, we have $h_{ij} = \alpha w_{ij}/p_j$. Again, from the proof of Proposition 1, we have:

$$\frac{w_{i1}}{p_1} < \frac{w_{i2}}{p_2}$$

which implies $h_{i1} < h_{i2}$. ■

Then given homothetic preferences for consumption, it immediately follows that:

**Corollary 1** Expenditure on the consumption good is higher in larger cities.
Our model predicts that expenditure on both housing and consumption is higher in larger cities, though the equilibrium quantity of housing $h^*_ij$ is lower. As cities become larger (or as the difference in TFP increases), at all skill levels total income increases and therefore total expenditure increases. Because house prices increase as well, there will be substitution away from housing to the consumption good. As a result, inequality in consumption expenditure will increase.

**Firm Size.** Our model is ambiguous when it comes to predicting firm size across cities. By assumption, there is a representative firm within a given city, and the firm size in city $j$ is given by $\sum_i m_{ij}$. Due to the free entry condition for firms and the ensuing general equilibrium effects, the firm size can

**Proposition 3** *Firm size is ambiguous across different cities.*

**Proof.** We know that $S_j = N_j \sum_i m_{ij}$. Therefore we can write relative firm size as

$$\frac{\sum_i m_{i1}}{\sum_i m_{i2}} = \frac{S_1 N_2}{S_2 N_1}. $$

The ratio of populations $S_1/S_2 > 1$. We also know that

$$\frac{N_1}{N_2} < \frac{A_2 p_1}{A_1 p_2},$$

however the RHS can be either smaller or larger than 1 (the TFP ratio is smaller and the price ratio is larger than one). It follows that

$$\frac{\sum_i m_{i1}}{\sum_i m_{i2}} \leq 1.$$ 

In the data section, we will verify how firm size changes across cities.

**Labor Productivity and TFP.** Even though large cities attract low skilled workers, those low skilled workers are more productive in large cites. In fact, as we pointed out earlier, the wage and therefore labor productivity in the largest cities is on average 25% larger than that in the smallest cities in our sample. Even under CES, more low skilled workers go to large cities because their productivity is higher there (though they do this to proportional the high skilled under CES). When the elasticity is varying, then in addition, the larger marginal product $\gamma_i$ for scarce skills relative to abundant skills makes the labor productivity of the scarce skills even larger in large cities.

Given the wage distribution within the city, house prices and the city size, we can infer information about the underlying productivity. For example, for the two-city economy, all else equal, an increase in the city size of the largest city is driven by an increase in TFP in that city. Our model is static, and therefore silent on the evolution of wages across cities. Nonetheless, based on these comparative statics, one can infer from the evolution of wages and skills across cities how productivity has evolved over time across cities.
5 The Empirical Evidence of Fat Tails

5.1 Empirical Strategy

We use the one-to-one relation between skills and equilibrium utility to back out the skill distribution from easily observable variables. The worker’s indirect utility in equilibrium is independent of the city, given perfect mobility, and assuming Cobb-Douglas preferences, it satisfies

\[ U_i = \alpha^\alpha (1 - \alpha)^{1-\alpha} \frac{w_{ij}}{p_j^\alpha} \]  

where we need to observe the distribution of wages \( w_{ij} \) by city \( j \), the housing price level \( p_j \) by city and the budget share of housing \( \alpha \).

5.2 Data

The analysis is performed at the city level. We define a city as a Core Based Statistical Area (CBSA), the most comprehensive functional definition of metropolitan areas published by the Office of Management and Budget (OMB) in 2000. See Table 1 for examples of cities and their 2009 population.

![Insert Table 1 here](image)

We use wage data from Current Population Survey (CPS) for the year 2009. We observe weekly earnings for 102,577 full-time workers in 257 U.S. metropolitan areas. CPS wages are top-coded at around $150,000 which we will take into account in the statistical analysis.

Local housing price levels are estimated using the 5% Public Use Microsample (PUMS) of the 2000 U.S. Census of Housing. We observe monthly rents for 3,274,198 housing units and assessed housing values for 7,680,728 owner-occupied units in 533 CBSAs. The Census also reports the number of rooms and bedrooms, the age of the structure, the number of units in the structure and whether the unit has kitchen facilities. City specific price indices from the Federal Housing Finance Agency (FHFA) based on the Case and Shiller (1987) repeat sales method are used to adjust for 2000-2009 growth in housing prices.

See the data appendix for more details on data source, sample restrictions and variables.

5.3 Wage distribution

Figure 3 shows the distribution of weekly wages for full-time earners both in cities with a population of more than 2.5 million and cities with population between 100,000 and 1 million. We clearly see that wages in larger cities are higher and that the top tail of the distribution is substantially bigger in large cities. A simple t-test shows that wages in large cities are 13.4% higher than in small ones \((t = 28.7, p < 0.000)\). Controlling for right censoring from top-coding and weights in a censored
Figure 3: Wage distribution for small and large cities. Full-time wage earners from 2009 CPS. A. Kernel density estimates (Epanechnikov kernel, bandwidth = 0.2), adjusted for top-coding; B. Empirical CDF.

Figure 4: Wage distribution by population size. A. Mean (slope average=0.046 (s.e.=0.007); B. Standard Deviation (slope st.dev.=0.023 (s.e.=0.003)).

(tobit) regression leads to almost exactly the same comparison: $\Delta \log \text{wage}= 13.4\%$ (robust $t = 25.54$, $p < 0.000$).

The above partitioning of wages into a group of small cities and a group of large cities ignores substantial differences across different cities of similar size. We therefore also relate the wage distribution of individual cities to city size. We estimate the mean and the standard deviation of the right-censored wage distribution for each city with maximum likelihood assuming log normality, i.e. a tobit regression on a constant. Figure 4 plots these estimates against 2009 population size. We see that both average wages and the variance of wages increases with population size. A simple linear regression estimates a slope coefficient of 0.046 for mean log wages (robust $t = 7.07$, $p > 0.000$) and of 0.023 (robust $t = 8.03$, $p > 0.000$).
for the standard deviation of log wages. On average, a one percent increase in the city population leads to 0.046% increase in the wage. Table 2 shows the top 10 and bottom 10 cities with respect to average wages.

[ Insert Table 2 here ]

5.4 Housing Prices

We model housing as a homogenous good $h$ with a location specific per unit price $p_j$. In practice, however, housing differs in many observable dimensions. Observed housing prices therefore reflect both the location and the physical characteristics of the unit. Sieg et al. (2002) show the conditions under which housing can be treated as if it were homogenous and how to construct a price index for it. Take our Cobb-Douglas utility function

$$u(c, h(z)) = c^{1-\alpha} h^\alpha(z)$$

and assume that housing $h(z)$ is a function, for simplicity of exposition only, of two characteristics $z = (z_1, z_2)$ with a nested Cobb-Douglas structure

$$h(z) = z_1^{\delta_1} z_2^{1-\delta_1}.$$ 

The indirect utility given the market prices $q_1$ and $q_2$ for, respectively, characteristic $z_1$ and $z_2$ is then

$$U_i = \alpha^\alpha (1 - \alpha)^{1-\alpha} \left[ L q_1^{\delta_1} q_2^{1-\delta_1} \right]^{-\alpha} w$$

where $L = 1/[\delta (1 - \delta)^{1-\delta}]$. Defining the price index $p = L q_1^{\delta_1} q_2^{1-\delta}$ the indirect utility is

$$U_i = \alpha^\alpha (1 - \alpha)^{1-\alpha} \frac{w}{p^\alpha}$$

and thus identical to the one derived assuming homogenous housing $h$ with market price $p$. The sub-expenditure function $e(q_1, q_2, h)$ is defined as the minimum expenditure necessary to obtain $h$ units of housing and given by

$$e(q_1, q_2, h) = L q_1^{\delta_1} q_2^{1-\delta_1} h = ph = pz_1^{\delta_1} z_2^{1-\delta}.$$ 

Taking logarithms and assuming that we observe $z_1$ but not $z_2$ yields a linear hedonic regression model

$$\log(e_{jn}) = \log(p_j) + \delta \log(z_{1jn}) + u_{jn}$$

where $e_{jn}$ is the observed rental price of housing unit $n$ and $\log(p_j)$. We can therefore estimate the city specific price level as location-specific fixed effect in a simple hedonic regression of log rental prices on the physical characteristics.
Figure 5: Skill distribution for small and large cities. A. Kernel density estimates (Epanechnikov kernel, bandwidth = 0.2), not adjusted for city-specific top-coding; B. Empirical CDF adjusted for top-coding using the Kaplan-Meier method.

Table 3 shows the results of the hedonic regressions both for rental units and owner-occupied units using Census data. We use all available housing characteristics in the data and add all categories as dummy variables without functional form assumptions. All coefficients are highly significant with expected signs: housing prices increase with the number of rooms and decrease with the age of the structure. We find a non-monotonic relationship in the numbers of units in the structure with highest prices for single-family detached homes and buildings with more than 50 units.

We adjust our estimated price levels from the 2000 Census for the 2000-2009 price changes using data from the Federal Housing Finance Agency (FHFA). Table 4 shows the resulting house price indices for the highest and lowest priced cities in our sample.

5.5 Skill distribution

Davis and Ortalo-Magné (2007) document that expenditure shares on housing are very constant across U.S. metropolitan areas with a median expenditure share of 0.24. We use this as our estimate of $\alpha$. Together with our estimate for local housing prices $p_j$ we can back out the indirect utility $u_{ij}$ for the observed wages using equation (4).

Figure 5 shows the distribution of skills for full-time earners both in cities with a population of more than 2.5 million and cities with population between 100,000 and 1 million. In contrast to the wage distribution, the skill distribution in large cities is only marginally shifted to the right. However,
both the upper and the lower tail of the distribution is thicker in the large cities thus confirming the theoretical prediction of fat tails.

The above partitioning of skills into a group of small cities and a group of large cities ignores substantial differences across different cities of similar size. We therefore estimate the mean and the standard deviation of the skill distribution for each city. As with wages, we take into account the city-specific right censoring from top-coded wages by estimating a censored (tobit) regression on a constant. The top two graphs in Figure 6 plot these estimates against 2009 population size. We see that while average skills vary little with population size, the standard deviation increases substantially. A simple linear regression estimates a slope coefficient of 0.018 for mean log utility (robust $t = 2.90$, $p > 0.004$) and of 0.023 (robust $t = 7.79$, $p > 0.000$) for the standard deviation of log utility. The lower two graphs in Figure 6 show non-parametric local linear regressions for the size relationship and 95% confidence intervals. Both the parametric and non-parametric estimates clearly confirm the fat tail hypothesis.
Table 5 shows the top 10 and bottom 10 cities with respect to average wages.

As we did in the introduction, to emphasize the fat tails result, in Figure 7 we reproduce the ratio of the wage demand and the ratio of the density functions. In panel A, the ratio of wages in large cities relative to small cities is increasing in wages, thus illustrating that relative wages are monotonic. In panel B, the relative densities of the utilities is non-monotonic. It is important here to point out that the decrease in the ratio at the very top skill levels is driven by the top coding. Note that for large cities the impact of top coding is further to the left due to on average higher house prices.

Figure 7: A. Relative wages between large and small cities; B. Relative demand for skills between large and small cities.

6 Other Measures of Skills

As a robustness check and as external validation, we compare our implicit skill distribution with observed measures of skill. Figure 8.A. shows the distribution of educational attainment for the same CPS population as our wage data, where workers are grouped in 7 education categories. The same pattern as with our implicit measure arises: both the highest and the lowest skilled workers are disproportionately more frequent in larger cities than in smaller ones.

This can be observed even more transparently when we group the education levels into three groups. This is reported in Figure 8.B. What is most striking about this observation is that the fat tails in the distribution of educational attainment is obtained independently of how we obtained our measure of skills before. No theory is needed and the measure of skills is determined exogenously.
The fat tails in the distribution of educational attainment in larger cities can also be established at the individual city level. Below in Figure 9, we report the scatter plot of the variance of educational attainment when educational attainment categories are given a score corresponding to the years of schooling.

Like in the case where the skill measure is derived from the wage distribution, when we use an observable, reported measure of skill, we find little correlation between city size and average skill, but a significant and positive relation between city size and the standard deviation of the skill measure.

Using observable, self-reported measures of skills, either education categories or years of schooling, we find a distribution with fatter tails in larger cities, both in the aggregate and at the individual city level.

The key identifying assumption to derive the skill distribution from wages is perfect mobility of identically skilled workers. For our wage-based skill measure that implies that utility of a given skilled worker is the same across different cities. Here we can verify whether this assumption holds when we use observable skills instead. Note that utility need not be equalized for identical observed skill levels across different cities when our predicted skill level is imperfectly correlated with the observable skill measure. Nonetheless, it is instructive to investigate how average utility (wages corrected for house prices) for individual skill groups vary across different city size.

In Table 7 we report the linear regression by observable skill group of the average utility its standard deviation on city size (Figure 15 depicts for each skill category the scatter plot for each city together the regression line). Before discussing the findings, an important caveat is due. By dividing workers in subgroups, some of the subgroups include city-education subgroup that have not enough observations to calculate the mean and standard deviation. Those with city-education subgroups with less than two
Figure 9: Distribution of educational attainment (translated into years) by population size. Left graphs: Mean; Right graphs: Standard Deviation. Top graphs: linear regression (slope average=0.12 (s.e.=0.03); slope st.dev.=0.12 (s.e.=0.02)). Bottom graphs: local linear regression (Epanechnikov kernel, bandwidth = 0.53 and 0.68, respectively)

observations are dropped. The lack of observations is most acute in the highest skill categories. Table 7 reports the number of cities N in each skill category out of all 253 cities where there are at least two observations. Because the censoring of the data may well be systematic, these results should be taken as merely indicative.

[ Insert Table 7 here ]

For what the data is worth, we find that by observable education category, in 6 out of the 7 groups utilities (real wages) do not significantly vary with city size. The one exception is those with Master degrees. This effect is strong enough to render the overall effect to be positive as well, though the effect is small. This seems to indicate there is some systematic variation wages across cities for this education group. For example, there could be systematic variation in the location decision and the enrollment
in masters degrees, which predominantly happens after several years of work experience (e.g., MBA degrees).

This indicates that on average our price-theory measure of skills appears to be quite correlated with the measure from observable skills. What the remainder of the table suggests is that even within each observable skill category there is residual heterogeneity in skills. In each skill category, the standard deviation of utility (real wages) is increasing in city size. Even within the observable skill category (degree obtained), there is systematic sorting of the highest and lowest skilled types into large cities and those that are medium skilled locate in medium sized cities. This holds true for all seven skill categories. This is consistent with the well-known finding that a large part of wage heterogeneity is not explained by observable skills (see for example Keane and Wolpin (1997)).

7 Discussion and Extensions

7.1 Firm size

In our model, firm size is endogenous. We can therefore identify primitive parameters from the empirical firm size distribution. We use Census data\(^8\) on the number of employees and establishments for counties or CBSAs. This allows us to calculate the average number of employees per establishment by city.

Figure 10 reports the average firm size by city size. The linear regression coefficient is positive and positive. The kernel estimate is inverted U-shaped, though the downward sloping portion is not significant. In terms of the magnitude, the average firm size increases between 15 and 17 employees, from the kernel estimate.\(^9\)

We can exploit the fact that theory pins down the relation between TFP and house prices. From Lemma 1 in the Appendix, we know that \(m_{i1} > m_{i2} \iff \frac{A_1}{A_2} > \left(\frac{p_1}{p_2}\right)^\alpha\). This therefore implies that the ratio of TFP between two cities can be bounded by:

\[
\frac{A_1}{A_2} > \left(\frac{p_1}{p_2}\right)^\alpha = \frac{w_{i1}}{w_{i2}},
\]

where use the equilibrium condition of mobility across cities that the wage ratio must be proportional to the price ratio. TFP in the largest cities in our sample is at least 25% higher than that in the smallest cities (with a population around 160,000). The fact that the TFP is larger than labor productivity is due free entry of firms and the fact that the cost of entry depends on the house price index and is therefore different across cities.

\(^8\)County Business Patterns, U.S. Census: http://www.census.gov/econ/cbp/index.html.

\(^9\)For the service sector, Holmes and Stevens (2003) find a positive relation between city size and establishment size, and a negative relation in manufacturing. Given the modest size of the manufacturing sector (9% of all non-farm employment – www.bls.gov) relative to services (69%), this is consistent with our finding that across all sectors this relation is increasing.
7.2 The Role of Migration

Casual observation suggests that large cities tend to have a disproportionate representation of low skilled immigrant workers. Often kitchen staff in restaurants or construction workers are immigrants with low skills and incomes. And indeed, while foreign borns are overall a relatively small fraction of the working population (less than 10%), the data confirms that they are much more likely to locate in large cities (12% of the work force) than in small cities (5%). Maybe the effect of disproportionate representation of the low skilled in large cities is driven by immigration.

In the context of our model it does not matter whether it is the low skilled Americans or low skilled immigrants who disproportionately locate in large cities. In equilibrium they should be indifferent. Of course, there is likely to be within-skill heterogeneity (in preferences for example), and some low skilled workers will strictly prefer to locate in either large or small cities. While we do not model this, in equilibrium there should still be arbitrage by the marginal worker within a skill type. Thus it may well be the case that migrants have certain benefits from locating in large cities. For example networks (see Munshi (2003)) play an important role for the location decision of migrants, and if only migrants have that benefit, at a competitively set wage, migrants will strictly prefer to locate in the city that offers the same utility plus the network benefit. Alternatively, migrants may locate in large cities due to limited information about smaller cities.

In any event, because even with those additional benefits for migrants, or any within skill heterogeneity, the model still predicts that in equilibrium, low skilled workers disproportionately move into large cities. It is sufficient that the marginal type within a skill class arbitrages the difference.

To evaluate the role of migrants in the location decision, we split the sample up into natives and foreign born workers. Figure 11 reports the plot of both distributions. Not surprisingly, the implied
skill distribution for the foreign born is more skewed to the left than that of the natives. We find that even the distribution of foreign born workers has fat tails, both for the low and the high skilled. The latter is maybe most surprising: not only do the low skilled foreign born disproportionately migrate to large cities, so do the high skilled migrants. Most importantly, even after subtracting all the migrants, the distribution of natives has fatter tails in large cities. The fat tails are therefore not exclusively driven by non-natives.

7.3 Variation in Consumption Prices: Using ACCRA data

The purpose of this sections is double. First, we investigate the role of systematic variation in consumption prices across different cities. Maybe consumption prices in large cities are systematically higher than in smaller cities, thus adding also further to the real cost of living in large cities. We use the ACCRA Cost of Living Index from C2ER (The Council for Community and Economic Research). ACCRA reports local prices for 60 goods such as e.g., a sausage, a house, a phone call, gasoline, the drug Lipitor, or a haircut. The data is collected by volunteers from the local chamber of commerce and then used to build price indices for the six broad consumption categories: grocery items, housing, utilities, transportation, health care and services. ACCRA is the only data for price comparisons across a large set of MSAs. Koo et al. (2000) discuss several problems of the ACCRA data. Besides being collected by volunteers and stemming from a very limited set of items, the most fundamental critique is the lack of proper adjustment for quality differences.

The first finding is that the variation in consumption prices is substantially lower than in housing prices (standard deviation across metropolitan areas is 30.1 for the housing prices index compared to 9.6 for grocery items, 14.7 for utilities, 6.7 for transport, 8.9 for health and 6.9 for services; all prices indices are normalized to mean 100).
Figure 12 plots the distribution for large and small cities of price adjusted wages for two measures. In panel A, the measure is wages adjusted for local price differences in all goods categories reported in the ACCRA data, including housing, consumption goods and services. Panel B uses the measure where wages are adjusted for house prices only as reported in ACCRA by dividing by that price index to the power $\alpha = 0.24$, the share of housing in total consumption. Panel B illustrates that despite the shortcomings of the ACCRA data, the result of fat tails continues to hold. When including the price index for all consumption and housing as in panel A, we find that the left tail difference becomes more pronounced while the right tail difference less so. This indicates that consumption prices are systematically higher in larger cities, but to a limited extent since this effect does not annihilate the existing of fat tails.

These findings should be interpreted with some caution and a few caveats are due. First, the quality of the ACCRA data is dubious. Second, even within a given location, there could be variation in consumption prices paid by skill level. For example, due to different search intensity, the existence of locally segregated markets,... the low skilled may end up paying different prices for similar goods within the same city. Using scanner data on household purchases, Broda, Leibtag and Weinstein (2009) find that the poor pay less. Third, data consisting of price indexes and price surveys are likely to not fully account for quality and diversity differences. Due to their size, large cities have more variety on offer and the quality of goods may differ substantially across different cities. Even if a consumer is paying higher prices, a price index incorporating the diversity and quality on offer will be lower. This also appears to be an issue when studying price differences across different countries. Comparing the results

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$^{10}$ACCRA reports a composite price index which is the weighted average of the six sub-indices, i.e. $P_{\text{composite}} = \alpha_{\text{grocery}}P_{\text{grocery}} + \ldots + \alpha_{\text{services}}P_{\text{services}}$, where the $\alpha$s are the expenditure shares of the six categories summing up to 1. We do not use this aggregation as it is inconsistent with Cobb-Douglas utility. Instead, we use $P_{\text{composite}} = (P_{\text{grocery}})^{\alpha_{\text{grocery}}} \cdot \ldots \cdot (P_{\text{services}})^{\alpha_{\text{services}}}$. 

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26
of price differences across borders, Broda and Weinstein (2008) find that significant price differences that are found using price indexes are not replicated once they use US and Canadian barcode data. Their work is supportive of simple pricing models where the degree of market segmentation across the border is similar to that within borders. We therefore see the left panel A as a very conservative upper bound of how the inclusion of consumption price differentials affects our initial findings.

7.4 A Micro-foundation for VES: Spillovers from Skill Diversity

So far we have been agnostic about what determines the VES technology. It is well documented that agglomeration externalities are important (see for example Davis, Fisher and Whited (2009) among many others). Here we propose a simple micro-foundation for the technology with varying elasticities of substitution that generates the fat tails, and that is derived from spillovers across skill types.

The production technology in a city $j$ is given by:

$$Y_j = A_j \sum_i a(\cdot) m_{i,j}^{\gamma} y_i^\beta.$$ 

This technology is completely standard CES except for the fact that there is a knowledge spillover $a(\cdot) = m_{i,j}^{\chi(\cdot)}$ that affects the marginal productivity of the worker. Knowledge spillovers are generated by the input of diversely skilled workers. Having a different viewpoint helps solve a problem (e.g., the input from the baggage loader at Southwest airlines on the performance of the logistics manager to streamline luggage flows). There is no spillover from meeting a same skilled type as that knowledge is already embodied in your own skill. We assume that spillovers arise whenever individuals meet, which occurs through uniform random matching. So if a worker meets one other worker per period, the probability that she is of another skill type is given by:

$$1 - \frac{M_i}{\sum_i M_i},$$

and the effect of the spillover on the marginal productivity then is

$$\chi \left(1 - \frac{M_i}{\sum_i M_i}\right)$$

and increasing. The nature of the spillover is illustrated in Figure 13.

Output for each skill now consists of

$$A_j m_{i,j}^{\chi\left(1 - \frac{M_i}{\sum_i M_i}\right)} m_{i,j}^{\gamma} y_i^\beta$$

and introducing the notation $\gamma(M_i) = \chi \left(1 - \frac{M_i}{\sum_i M_i}\right) + \gamma$ where $\gamma(M_i)$ is a decreasing function, we can
Figure 13: A. Spillover technology $\chi(\cdot)$, increasing in measure of other skills; B. The marginal product $\gamma(m_{ij})$ (and the Elasticity of Substitution $\rho$) are decreasing in abundance of skill.

write the technology as

$$Y_j = A_j \sum_i m_{ij} \gamma(M_i) y_i^\beta.$$  

Irrespective of the functional form of $\gamma(\cdot)$, the important implication of this formulation of the technology is that it is a variation on the standard CES technology, except for the fact that the elasticity varies by skill. This Varying Elasticity of Substitution (VES) technology of course is no longer homothetic. There is still a direct relation between $\gamma(\cdot)$ and the elasticity of substitution $\rho_{ik}$ between skill $i$ and $k$ is given by (see Appendix for the derivation):

$$\rho_{ij} = \frac{\gamma_i n_i^{\gamma_i} y_i + \gamma_j n_j^{\gamma_j} y_j}{\gamma_i n_i^{\gamma_i} y_i (1 - \gamma_j) + \gamma_j n_j^{\gamma_j} y_j (1 - \gamma_i)},$$

where $\gamma_i = \gamma(M_i)$ and $\gamma_k = \gamma(M_k)$. Observe that if $\gamma_i = \gamma_k = \gamma$, the technology is CES and this expression simplifies to the usual constant elasticity $\rho = \frac{1}{1-\gamma}$. The technology with varying elasticity is compared to the constant elasticity technology in Figure 14.

### 7.5 Unemployment

One alternative explanation for the fat tails may emanate from market frictions (see for example Eeckhout and Kircher (2010), Eeckhout, Lentz and Roys (2010), Gautier, Svarer and Teulings (2010) and Helpman, Itskhoki and Redding (2010)). Consider a CES technology but with search frictions. Then more abundant skill types will face a relatively high unemployment to vacancy ratio, whereas scarce skill types face a low ratio. This drives a wedge between the marginal productivity and wages. In a labor market without an urban dimension, Eeckhout, Lentz and Roys (2010) show in a directed search model that this leads to fatter tails in the more productive firms. It remains to be verified though that
empirically the unemployment rate both for high and low skilled workers is substantially higher.

Consideration of search frictions immediately brings up the issue of dynamics, currently completely absent in our analysis. Possibly cities of different size and TFP offer different earnings paths. Those with a steeper earnings path will induce workers to accept lower wages early on which over the entire path leaves them indifferent. This now potentially becomes a hairy dynamic problem. An important related empirical and modeling issue to be addressed in a dynamic framework is the age distribution across cities. Young people move into cities to move out again at middle age. This indicates that the benefits of large cities is non-monotonic over the life cycle which renders the dynamic implications of the model a priori ambiguous. Given the complexity of the issue, we leave dynamics for future work. Nonetheless, the approach adopted by Desmet and Rossi-Hansberg (2010) in solving for a dynamic spatial equilibrium will certainly be promising also here. They show that under certain assumptions on the distribution of property rights, such a complicated dynamic problem leads to static optimization. This also indicates that our static approach is appropriate.

8 Conclusion

We have proposed a tractable theory of spatially dispersed production with perfectly mobile heterogeneous inputs, skilled labor. Differences in TFP lead to differences in demand for skills across cities. In general equilibrium, wages and house prices clear the labor and housing markets. Perfect mobility of citizens leads to utility equalization by skill.
We show that cities with a higher TFP are larger and that a CES production technology entails identical skill distributions across cities with different productivity. When the elasticity of substitution varies across skills such that it is higher for scarce skills, the skill distribution in larger cities exhibits fatter tails.

We find empirical support for our theory using US data. Adjusting wages for the compensating differentials of house prices by means of a hedonic price index, we find skill distributions that have fatter tails in larger cities. Our measure of skill derives directly from wages, and includes therefore also unobservable determinants of skills. For external validation, we also use a measure of observable skills only – years of schooling – and find the same results. Of course, in order to capture the non-monotonic relation in the demand for skills, the partition of skill classes must be sufficiently fine. The robustness of the result to the use of skill measures based on both observables and unobservables and measures based on observables only is indicative of the robustness of the result. The use of a wage based skill measure is not only attractive because it incorporates unobservable characteristics of skill, by construction it is also measured as a continuous variable. While partitioning worker types in two classes of high and low skilled is attractive in many ways, it precludes identification of non-linear relations, let alone non-monotonic relations.
Appendix A: Theory

Proof of Theorem 1

Proof. Given constant $\gamma$, we can rewrite the first equilibrium condition as:

$$
\sum_{i=1}^{t} \left( \frac{M_i}{N_2} \right)^\gamma y_i^\beta \left\{ \frac{\left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^\alpha \right]^{\frac{1}{1-\gamma(1-\alpha)}}}{1 + \frac{N_1}{N_2} \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^\alpha \right]^{\frac{1}{1-\gamma(1-\alpha)}}} \right\}^\gamma = \frac{H_1 A_2 N_2 p_1}{H_2 A_1 N_1 p_2}
$$

and therefore after canceling common terms as:

$$
\left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^\alpha \right]^{\frac{\gamma - 1}{1-\gamma(1-\alpha)}} = \frac{H_1 A_2 N_2 p_1}{H_2 A_1 N_1 p_2},
$$

We solve for the price ratio:

$$
\frac{p_1}{p_2} = \left( \frac{H_1 N_2}{H_2 N_1} \right)^{\frac{\gamma - 1}{1-\gamma(1-\alpha)}} \left( \frac{A_2}{A_1} \right)^{-\frac{1}{1-\gamma(1-\alpha)}}.
$$

Observe that:

$$
\frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^\alpha = \left[ \left( \frac{H_1 N_2}{H_2 N_1} \right)^{\alpha} \left( \frac{A_2}{A_1} \right)^{\alpha-1} \right]^{\frac{\gamma - 1}{1-\gamma(1-\alpha)}}
$$

Substituting into the expressions for $m_{ij}$ we obtain:

$$
m_{i1} = \frac{\left[ \left( \frac{H_1 N_2}{H_2 N_1} \right)^{\alpha} \left( \frac{A_2}{A_1} \right)^{\alpha-1} \right]^{\frac{\gamma - 1}{1-\gamma(1-\alpha)}} M_i}{N_2 + N_1 \left[ \left( \frac{H_1 N_2}{H_2 N_1} \right)^{\alpha} \left( \frac{A_2}{A_1} \right)^{\alpha-1} \right]^{\frac{\gamma - 1}{1-\gamma(1-\alpha)}}}
$$

$$
m_{i2} = \frac{1}{N_2 + N_1 \left[ \left( \frac{H_1 N_2}{H_2 N_1} \right)^{\alpha} \left( \frac{A_2}{A_1} \right)^{\alpha-1} \right]^{\frac{\gamma - 1}{1-\gamma(1-\alpha)}} M_i}
$$

The density at any skill level $i$ is simply the ratio of the measure of that skill over the total measure,
and after simplifying, we get:

\[
\frac{m_{i1}}{\sum_{i=1}^{I} m_{i1}} = \frac{\left( \frac{H_1 N_2}{N_1} \left( \frac{A_2}{A_1} \right)^{\alpha-1} \right) - \frac{1}{N_2 + N_1} \left[ \frac{H_1 N_2}{N_1} \left( \frac{A_2}{A_1} \right)^{\alpha-1} \right] \frac{1}{1 - \gamma(1 - \alpha)} m_i}{\sum_{i=1}^{I} M_i} = \frac{M_i}{\sum_{i=1}^{I} M_i}
\]

Likewise for the density in city 2:

\[
\frac{m_{i2}}{\sum_{i=1}^{I} m_{i2}} = \frac{M_i}{\sum_{i=1}^{I} M_i}
\]

Therefore, both distributions are identical and equal to the economy-wide distribution. 

Proof of Proposition 1

First we prove the following Lemma concerning the housing prices.

Lemma 1 When \( \frac{A_1}{A_2} \left( \frac{p_1}{p_2} \right)^{\alpha} < 1 \), \( m_{i1} > m_{i2} \), \( \forall i \in I \).

Proof. Recall that we have \( A_1 > A_2 \). Defining \( Z = A_1 \left( \frac{p_1}{p_2} \right)^{\alpha} \). From \( Z < 1 \), we know that \( Z^{\frac{1}{1 - \gamma_i}} > 1 \), since \( \gamma_i \in (0, 1) \). Then, from the first order conditions, we obtain:

\[
m_{i1} = \frac{Z^{\frac{1}{1 - \gamma_i}}}{N_2 + N_1} M_i > \frac{1}{N_2 + N_1} M_i = m_{i2}
\]

\[\blacksquare\]

Now, we prove the Proposition:

Proof. Consider the system of equilibrium equations (1)–(3), with \( H_1 = H_2 \). Equating (2) and (3), we obtain:

\[
\sum_{i=1}^{I} \left( \frac{M_i}{N_2} \right)^{\gamma_i} \frac{A_2}{p_2} \left( 1 - \gamma_i \right) y_i^{\beta} \left[ \frac{A_1}{A_2} \left( \frac{p_2}{p_1} \right) \right]^{\gamma_i} \left\{ \frac{A_1}{A_2} \left( \frac{p_2}{p_1} \right) \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right) \right]^{\alpha} \right\}^{\frac{1}{1 - \gamma_i}} = 0
\]

(5)

and after rearranging, we have:

\[
\frac{A_1}{A_2} \left( \frac{p_2}{p_1} \right) \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right) \right]^{\alpha} = \left( \frac{A_1}{A_2} \right)^{\frac{1}{1 - \gamma_i}} \left( \frac{p_2}{p_1} \right)^{1 + \frac{\alpha \gamma_i}{1 - \gamma_i}}.
\]

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Since \( \left( \frac{A_1}{A_2} \right)^{1 - \gamma_i} > 0 \), it immediately follows that \( p_2 < p_1 \).

The term inside curly brackets can be written as:

\[
\frac{A_1}{A_2} \left( \frac{p_2}{p_1} \right) \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right] = \left( \frac{p_2}{p_1} \right)^{1 - \alpha} \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right] = 1 - \left( \frac{p_2}{p_1} \right)^{1 - \alpha} \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right] - 1,
\]

and given \( \frac{p_2}{p_1} < 1 \), the equality in equation (5) requires that \( \left( \frac{p_2}{p_1} \right)^{1 - \alpha} \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right] \geq 1 \) for some values of \( \gamma_i \). This is only possible if \( \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right] \geq 1 \) for some values of \( \gamma_i \). But this is only possible if \( \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} < 1 \).

Therefore, \( Z < 1 \).

From Lemma 1, this imply that \( m_{i1} > m_{i2} \). Therefore, each individual firm in city 1 is bigger than each individual firm in city 2.

The economy can be fully characterized by the system of equations:

\[
\sum_{i=1}^{N} \alpha \frac{w_{i1}}{p_1} m_{i1} = \frac{H_1}{N_1} \tag{6}
\]

\[
\sum_{i=1}^{N} \alpha \frac{w_{i2}}{p_2} m_{i2} = \frac{H_2}{N_2} \tag{7}
\]

\[
m_{i1} = \left( \frac{w_{i1}}{\gamma_i A_1 y_i} \right)^\frac{1}{\gamma_i - 1}
\]

\[
m_{i2} = \left( \frac{w_{i2}}{\gamma_i A_2 y_i} \right)^\frac{1}{\gamma_i - 1}
\]

\[
N_1 m_{i1} + N_2 m_{i2} = M_i
\]

\[
\frac{w_{i1}}{(p_1)^\alpha} = \frac{w_{i2}}{(p_2)^\alpha}
\]

\[
A_1 \sum_{i=1}^{N} (1 - \gamma_i) (m_{i1})^{\gamma_i} y_i = k p_1
\]

\[
A_2 \sum_{i=1}^{N} (1 - \gamma_i) (m_{i2})^{\gamma_i} y_i = k p_2
\]

From \( \frac{w_{i1}}{(p_1)^\alpha} = \frac{w_{i2}}{(p_2)^\alpha} \), \( \forall i \in \{1,...,N\} \), and \( p_1 > p_2 \) we have that \( w_{i1} > w_{i2} \). Now, consider that:

\[
\frac{w_{ij}}{p_j} = \frac{1}{(p_1)^{1-\alpha}} \frac{w_{i1}}{(p_1)^\alpha} = \frac{1}{(p_1)^{1-\alpha}} \frac{w_{i2}}{(p_2)^\alpha}
\]

\[
\frac{w_{i2}}{p_2} = \frac{1}{(p_2)^{1-\alpha}} \frac{w_{i2}}{(p_2)^\alpha}
\]

Then:

\[
\frac{w_{i1}}{p_1} < \frac{w_{i2}}{p_2},
\]

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since \( p_2 < p_1 < 1 \).

Then, from equations (6) and (7), we obtain, for \( H_1 = H_2 \):

\[
\sum_{i=1}^{N} \alpha \left[ N_1 \frac{w_1}{p_1} m_{i1} - N_2 \frac{w_2}{p_2} m_{i2} \right] = 0
\]

Rearranging, we have:

\[
\sum_{i=1}^{N} \frac{w_2}{p_2} m_{i2} \left[ \alpha \left( \frac{p_2}{p_1} \right)^{1-\alpha} \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i}} - N_2 \right] = 0
\]

Notice that:

\[
\frac{dZ_{\gamma_i}}{d\gamma_i} = -\frac{Z_{\gamma_i-1}}{(\gamma_i - 1)^2} \ln Z.
\]

Since \( Z < 1 \), we have that \( \frac{dZ_{\gamma_i}}{d\gamma_i} > 0 \). This implies that the first term inside squared brackets is increasing in \( \gamma_i \). Since it is definitely positive for \( \gamma_i \approx 1 \), it must be negative around \( \gamma_i = 0 \). Therefore, we have that:

\[
N_1 \left( \frac{p_2}{p_1} \right)^{1-\alpha} \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i}} - N_2 < 0
\]

Rearranging this implies:

\[
\frac{N_1}{N_2} < \frac{A_2}{A_1} \frac{p_1}{p_2}
\]

Now we can compare the size of cities 1 and 2:

\[
S_2 - S_1 = \sum_{i=1}^{N} N_2 m_{i2} \left[ 1 - \frac{N_1 m_{i1}}{N_2 m_{i2}} \right]
\]

Since \( \frac{m_{i1}}{m_{i2}} = \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i}} \) and \( \frac{N_1}{N_2} < \frac{A_2}{A_1} \frac{p_1}{p_2} \), we have:

\[
S_2 - S_1 < \sum_{i=1}^{N} N_2 m_{i2} \left[ 1 - \left( \frac{A_2}{A_1} \frac{p_1}{p_2} \right) \times \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i-1}} \right]
\]

We know that

\[
\left( \frac{A_2}{A_1} \frac{p_1}{A_1 p_2} \right) \times \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i-1}} = \left( \frac{p_1}{p_2} \right)^{1-\alpha} \times \left[ \frac{A_2}{A_1} \left( \frac{p_1}{p_2} \right)^{\alpha} \right]^{\frac{1}{\gamma_i-1}} < 1.
\]

Therefore \( S_1 > S_2 \).
8.1 Proof of Theorem 2

Proof. Denote the mode of the skill distribution by $\bar{i}$. Then the distribution is uni-modal if for all $i' > i, M_{i'} > M_i$ when $i, i' \leq \bar{i}$ and $M_{i'} < M_i$ when $i, i' \geq \bar{i}$.

From the assumptions in the theorem and by the proof of Proposition 1, we know that $Z < 1$ and therefore $Z^{\gamma_{\bar{i}} - 1} > 1$. The density of any skill $i$ in each city is given by

$$m_i = \frac{Z^{\gamma_i - 1}}{N_2 + N_1 Z^{\gamma_i - 1}} M_i$$

and

$$m_i = \frac{1}{N_2 + N_1 Z^{\gamma_k - 1}} M_i$$

Therefore the ratio of densities is

$$\frac{m_i}{m_j} = \frac{Z^{\gamma_i - 1} \sum_{k=1}^I \frac{1}{N_2 + N_1 Z^{\gamma_k - 1}} M_k}{\sum_{k=1}^I \frac{Z^{\gamma_k - 1}}{N_2 + N_1 Z^{\gamma_k - 1}} M_k}.$$

First, we write the ratio of densities in both cities for the highest skills $i = I$ (given a symmetric distribution, exactly the same holds for $i = 1$):

$$\frac{m_I}{m_I} = \frac{Z^{\gamma_{\bar{i}} - 1} \sum_{k=1}^I \frac{1}{N_2 + N_1 Z^{\gamma_k - 1}} M_k}{\sum_{k=1}^I \frac{Z^{\gamma_k - 1}}{N_2 + N_1 Z^{\gamma_k - 1}} M_k} > 1.$$
enough.

As a result, the distribution in city 1, the high TFP city, has fatter tails and less density around the mode. From Proposition 1 we also know that city 1 - the high TFP city - is larger. Therefore the larger city has fatter tails. ■

Elasticity of Substitution

From the definition of the elasticity of substitution:

$$\sigma = \frac{\frac{d(x_2/x_1)}{x_2/x_1}}{\frac{df_1/df_2}{df_1/df_2}}$$

Following Silberberg, the Elasticity of Substitution is given by:

$$\sigma = -\frac{f_1f_2(f_1x_1 + f_2x_2)}{x_1x_2(f_2^2f_{11} - 2f_1f_2f_{12} + f_2^2f_{22})}$$

In our case, we have:

$$f_i = A\gamma_i n_i^{\gamma_i - 1} y_i$$
$$f_j = A\gamma_j n_j^{\gamma_j - 1} y_j$$
$$f_{ii} = A\gamma_i (\gamma_i - 1) n_i^{\gamma_i - 2} y_i$$
$$f_{jj} = A\gamma_j (\gamma_j - 1) n_j^{\gamma_j - 2} y_j$$
$$f_{ij} = 0$$

Then, we have:

$$f_if_i + f_jf_j = A\gamma_i n_i^{\gamma_i - 1} y_i + A\gamma_j n_j^{\gamma_j - 1} y_j$$
$$f_if_j = A^2\gamma_i\gamma_j n_i^{\gamma_i - 1} n_j^{\gamma_j - 1} y_i y_j$$

Therefore, the numerator is:

$$A^3\gamma_i\gamma_j y_i y_j n_i^{\gamma_i - 1} n_j^{\gamma_j - 1} x (\gamma_i n_i^{\gamma_i} y_i + \gamma_j n_j^{\gamma_j} y_j)$$

and

$$f_i^2f_{jj} = A^3\gamma_i^2 n_i^{2\gamma_i - 2} y_i^2 \gamma_j (\gamma_j - 1) n_j^{\gamma_j - 2} y_j$$
$$f_j^2f_{ii} = A^3\gamma_j^2 n_j^{2\gamma_j - 2} y_j^2 \gamma_i (\gamma_i - 1) n_i^{\gamma_i - 2} y_i$$
Then, the denominator is:

$$n_i n_j \times \left( A^3 \gamma_i^2 n_i^{2\gamma_i-2} y_i^{\gamma_i} \gamma_j (\gamma_j - 1) n_j^{\gamma_j-2} y_j^+ + A^3 \gamma_j^2 n_j^{2\gamma_j-2} y_j^{\gamma_j} \gamma_i (\gamma_i - 1) n_i^{\gamma_i-2} y_i^+ \right)$$

Rearranging, we have:

$$A^3 \gamma_i \gamma_j y_i y_j n_i^{\gamma_i-1} n_j^{\gamma_j-1} \times \left( \gamma_i n_i^{\gamma_i} y_i (\gamma_j - 1) + \gamma_j n_j^{\gamma_j} y_j (\gamma_i - 1) \right)$$

Therefore, the elasticity of substitution becomes:

$$\sigma = -\frac{A^3 \gamma_i \gamma_j y_i y_j n_i^{\gamma_i-1} n_j^{\gamma_j-1} \times \left( \gamma_i n_i^{\gamma_i} y_i + \gamma_j n_j^{\gamma_j} y_j \right)}{A^3 \gamma_i \gamma_j y_i y_j n_i^{\gamma_i-1} n_j^{\gamma_j-1} \times \left( \gamma_i n_i^{\gamma_i} y_i (\gamma_j - 1) + \gamma_j n_j^{\gamma_j} y_j (\gamma_i - 1) \right)}$$

Simplifying, we get:

$$\sigma = \frac{\gamma_i n_i^{\gamma_i} y_i + \gamma_j n_j^{\gamma_j} y_j}{\gamma_i n_i^{\gamma_i} y_i (1 - \gamma_j) + \gamma_j n_j^{\gamma_j} y_j (1 - \gamma_i)}$$

Notice that if $\gamma_i = \gamma_j = \gamma$, this expression simplifies to $\frac{1}{1-\gamma}$. 
Appendix B: Data

Wage Data

Wage data is taken from the Current Population Survey (CPS), a joint effort between the Bureau of Labor Statistics (BLS) and the Census Bureau.\textsuperscript{11} The CPS is a monthly survey and used by the U.S. Government to calculate the official unemployment and labor force participation figures. We use the 2009 merged outgoing rotation groups (MORG) as provided by the National Bureau of Economic Research (NBER)\textsuperscript{12}. The MORG are extracts of the basic monthly data during the household’s fourth and eighth month in the survey, when usual weekly hours/earnings are asked.

We use the variable ‘earnwke’ as created by the NBER.\textsuperscript{13} This variable reports earnings per week in the current job. It includes overtime, tips and commissions. For hourly workers, Item 25a (“How many hours per week does...usually work at this job?”) times Item 25c (“How much does ...earn per hour?”) appears here. For weekly workers, Item 25d (“How much does...usually earn per week at this job before deductions?”) appears here.

We restrict the sample to full time workers (between 36 and 60 usual hours per week) with hourly wages above the federal minimum wage of 7.25 USD. Our final wage sample includes 102,599 workers out of the 320,941 surveyed persons. CPS wage data is in 2009 top-coded at a weekly wage of 2884.61 USD which applies to 2616 or 2.5% of workers. All estimations use the weights in variable ‘earnwt’ provided by the NBER.

The NBER version of the CPS identifies the core-based statistical area (CBSA) of the observation. It uses the New England city and town areas (NECTA) definition and codes for metro areas in the 6 New England states and the Federal Information Processing Standards (FIPS) definition and codes for all other states.

Local house and commodity price indices

We use the 5% Public Use Micro Sample (PUMS) of the 2000 U.S. Census. The U.S. is a decennial random sample of housing units across the U.S. The data is provided by the Minnesota Population Center in its Integrated Public Use Microdata Series (IPUMS).\textsuperscript{14}

The variable ‘rent’ reports the monthly contract rent for rental units and the variable ‘valueh’ the value of housing units in contemporary dollars. We also use all the reported housing characteristics of the unit: ‘rooms’ is the number of rooms, ‘bedrooms’ is the number of bedrooms, ‘unitsstr’ is the units in structure (in 8 groups), ‘builtyr’ is the age of structure (in 9 age groups) and ‘kitchen’ is a dummy variable if the unit has kitchen or cooking facilities.

\textsuperscript{11} See http://www.bls.gov/cps/
\textsuperscript{12} Stata data file available at http://www.nber.org/morg/annual/morg09.dta
\textsuperscript{13} See details of the variable creation at the NBER website http://www.nber.org/cps/
\textsuperscript{14} See Ruggles et al. (2010) for the data source and http://usa.ipums.org/usa/ for a detailed description of data and variables.
We drop housing units in group quarters, farmhouses, drop mobile homes, trailers, boats, and tents and only use data from housing units in identified metropolitan or micropolitan core based statistical areas (CBSA). Our final sample contains 3,274,198 rental and 7,680,728 owner occupied units.

The 5% PUMS discloses the co-called Public Use Microdata Area (PUMA). PUMA’s are areas with a maximum of 179,405 housing units and only partly overlap with political borders of towns and counties. We use the Geographic Correspondence Engine with Census 2000 Geography from the Missouri Census Data Center (MCDC) to link PUMA areas to CBSAs. The MCDC data matches every urban PUMA code to one or more CBSA codes and reports the fraction of housing units that are matched. We assign a PUMA to a CBSA if this fraction is bigger than 33%. In cases where the PUMA does not fully belong to a CBSA, we assign the PUMA to the CBSA where most of its housing units belong to. Our final sample contains data from 533 metropolitan or micropolitan core based statistical areas (CBSA) out of a total of 940 existing CBSAs. Not that we do not use the metropolitan area code provided in the PUMS in variable ‘metaread’. This variable reports a mixture of metropolitan area codes (MSA, PMSA, central city or county) which is difficult to match with the CBSA definition.

We adjust our estimated price levels from the 2000 Census for the 2000-2009 price changes using data from the Federal Housing Finance Agency (FHFA). The FHFA publishes quarterly time series of local house price indices for 384 CBSAs based on the Case and Shiller (1987) repeat sales method. 11 of the CBSAs are divided into 29 metropolitan divisions. We average these divisions over the respective CBSA using the 2000 housing stock (provided by the MCDC) as weights.

For robustness checks, we also purchased the ACCRA Cost of Living Index from C2ER (The Council for Community and Economic Research). ACCRA data are collected by local chambers of commerce and similar organization who have volunteered to participate. They are reported for 269 core-based statistical areas (CBSA) and 80 metropolitan divisions for the 33 largest CBSAs. The ACCRA Cost of Living Index consists of six major categories: grocery items, housing, utilities, transportation, health care, and miscellaneous goods and services. These major categories in turn are composed of subcategories, each of which is represented by one or more items in the Index. In total, local prices of 60 items are reported, e.g. t bone steak (item 1), phone (31), gasoline (33), Lipitor (38), pizza (40) haircut (42), movie (52). Indices for major categories and an overall composite index are calculated as weighted averages where weights come from the Consumer Expenditures Survey conducted by the U.S. Bureau of Labor Statistics. We use the average of quarterly data from Q2.2008 to Q2.2009 in order to minimize the number of missing cities from non-reporting places. We use the average across metropolitan divisions to match ACCRA data to our wage data.

\[15\text{Available at http://mcdc2.missouri.edu/websas/geocorr2k.html.}
\[16\text{See http://www.fhfa.gov.}
Firm size distribution

Data on the local distribution of firm sizes is taken from the county business patterns compiled by U.S. Census Bureau as an extract from its own Business Register (BR). Data for establishments are presented by geographic area, 6-digit NAICS industry, legal form of organization (U.S. only), and employment size class. Data consist of number of establishments, employment during the week of March 12, first quarter payroll, and annual payroll. We use aggregate data for 939 CBSAs in 2008.
Appendix C: Tables and Additional Figures

Table 1: Rank of cities by 2009 population.

<table>
<thead>
<tr>
<th>City</th>
<th>Population</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 New York-Northern New Jersey-Long Island, NY-NJ-PA</td>
<td>19,069,796</td>
</tr>
<tr>
<td>2 Los Angeles-Long Beach-Santa Ana, CA</td>
<td>12,874,797</td>
</tr>
<tr>
<td>3 Chicago-Naperville-Joliet, IL-IN-WI</td>
<td>9,580,567</td>
</tr>
<tr>
<td>4 Dallas-Fort Worth-Arlington, TX</td>
<td>6,447,615</td>
</tr>
<tr>
<td>5 Philadelphia-Camden-Wilmington, PA-NJ-DE-MD</td>
<td>5,968,252</td>
</tr>
<tr>
<td>6 Houston-Sugar Land-Baytown, TX</td>
<td>5,867,489</td>
</tr>
<tr>
<td>7 Miami-Fort Lauderdale-Pompano Beach, FL</td>
<td>5,547,051</td>
</tr>
<tr>
<td>8 Washington-Arlington-Alexandria, DC-VA-MD-WV</td>
<td>5,476,241</td>
</tr>
<tr>
<td>9 Atlanta-Sandy Springs-Marietta, GA</td>
<td>5,475,213</td>
</tr>
<tr>
<td>10 Boston-Cambridge-Quincy, MA-NH</td>
<td>4,588,680</td>
</tr>
<tr>
<td>244 Albany, GA</td>
<td>165,440</td>
</tr>
<tr>
<td>245 Waterloo-Cedar Falls, IA</td>
<td>164,913</td>
</tr>
<tr>
<td>246 Panama City-Lynn Haven-Panama City Beach, FL</td>
<td>164,767</td>
</tr>
<tr>
<td>247 Oshkosh-Neenah, WI</td>
<td>163,370</td>
</tr>
<tr>
<td>248 Parkersburg-Marietta-Vienna, WV-OH</td>
<td>160,905</td>
</tr>
<tr>
<td>249 Niles-Benton Harbor, MI</td>
<td>160,472</td>
</tr>
<tr>
<td>250 Janesville, WI</td>
<td>160,155</td>
</tr>
<tr>
<td>251 Abilene, TX</td>
<td>160,070</td>
</tr>
<tr>
<td>252 Eau Claire, WI</td>
<td>160,018</td>
</tr>
<tr>
<td>253 Jackson, MI</td>
<td>159,828</td>
</tr>
</tbody>
</table>

Notes: cities are defined as core based statistical areas (CBSA). The Office of Management and Budget (OMB) defines 940 metropolitan and micropolitan areas of which we use the largest 253.
Table 2: Rank of cities by average log wages.

<table>
<thead>
<tr>
<th>Rank</th>
<th>City</th>
<th>Population</th>
<th>Avg. Log Wage</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Bridgeport-Stamford-Norwalk, CT</td>
<td>901,208</td>
<td>7.10</td>
</tr>
<tr>
<td>2</td>
<td>Barnstable Town, MA</td>
<td>221,151</td>
<td>7.05</td>
</tr>
<tr>
<td>3</td>
<td>San Francisco-Oakland-Fremont, CA</td>
<td>4,317,853</td>
<td>6.99</td>
</tr>
<tr>
<td>4</td>
<td>Boulder, CO</td>
<td>303,482</td>
<td>6.99</td>
</tr>
<tr>
<td>5</td>
<td>Ann Arbor, MI</td>
<td>347,563</td>
<td>6.99</td>
</tr>
<tr>
<td>6</td>
<td>Washington-Arlington-Alex., DC-VA-MD-WV</td>
<td>5,476,241</td>
<td>6.96</td>
</tr>
<tr>
<td>7</td>
<td>San Jose-Sunnyvale-Santa Clara, CA</td>
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<td>6.95</td>
</tr>
<tr>
<td>8</td>
<td>Worcester, MA</td>
<td>803,701</td>
<td>6.95</td>
</tr>
<tr>
<td>9</td>
<td>Hartford-West Hartford-East Hartford, CT</td>
<td>1,195,998</td>
<td>6.94</td>
</tr>
<tr>
<td>10</td>
<td>Oxnard-Thousand Oaks-Ventura, CA</td>
<td>802,983</td>
<td>6.94</td>
</tr>
<tr>
<td>244</td>
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<tr>
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<td>Columbia, SC</td>
<td>744,730</td>
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<td>246</td>
<td>Johnson City, TN</td>
<td>197,381</td>
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</tr>
<tr>
<td>247</td>
<td>Corpus Christi, TX</td>
<td>416,095</td>
<td>6.40</td>
</tr>
<tr>
<td>248</td>
<td>Bowling Green, KY</td>
<td>120,595</td>
<td>6.39</td>
</tr>
<tr>
<td>249</td>
<td>El Paso, TX</td>
<td>751,296</td>
<td>6.38</td>
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<td>250</td>
<td>Utica-Rome, NY</td>
<td>293,280</td>
<td>6.38</td>
</tr>
<tr>
<td>251</td>
<td>Waco, TX</td>
<td>233,378</td>
<td>6.37</td>
</tr>
<tr>
<td>252</td>
<td>Jacksonville, NC</td>
<td>173,064</td>
<td>6.36</td>
</tr>
<tr>
<td>253</td>
<td>Madera-Chowchilla, CA</td>
<td>148,632</td>
<td>6.36</td>
</tr>
</tbody>
</table>

Notes: Wages from CPS. Averages from tobit regression accounting for top-coding.
Table 3: Hedonic regressions for rental and owner-occupied units.

<table>
<thead>
<tr>
<th></th>
<th>log rent</th>
<th>log value</th>
</tr>
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<td></td>
<td>(0.0018)</td>
<td>(0.0058)</td>
</tr>
<tr>
<td></td>
<td>(0.0019)</td>
<td>(0.0055)</td>
</tr>
<tr>
<td></td>
<td>(0.0019)</td>
<td>(0.0055)</td>
</tr>
<tr>
<td></td>
<td>(0.0020)</td>
<td>(0.0055)</td>
</tr>
<tr>
<td></td>
<td>(0.0021)</td>
<td>(0.0055)</td>
</tr>
<tr>
<td></td>
<td>(0.0025)</td>
<td>(0.0055)</td>
</tr>
<tr>
<td></td>
<td>(0.0029)</td>
<td>(0.0055)</td>
</tr>
<tr>
<td></td>
<td>(0.0032)</td>
<td>(0.0055)</td>
</tr>
<tr>
<td></td>
<td>(0.0034)</td>
<td>(0.0014)</td>
</tr>
<tr>
<td></td>
<td>(0.0033)</td>
<td>(0.0014)</td>
</tr>
<tr>
<td></td>
<td>(0.0031)</td>
<td>(0.0013)</td>
</tr>
<tr>
<td></td>
<td>(0.0031)</td>
<td>(0.0013)</td>
</tr>
<tr>
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<td>(0.0031)</td>
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<tr>
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<tr>
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<td>(0.0031)</td>
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<tr>
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<td></td>
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<td>(0.0018)</td>
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<tr>
<td></td>
<td>(0.0031)</td>
<td>(0.0023)</td>
</tr>
<tr>
<td></td>
<td>(0.0030)</td>
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</tr>
<tr>
<td></td>
<td>(0.0030)</td>
<td>(0.0034)</td>
</tr>
<tr>
<td></td>
<td>(0.0031)</td>
<td>(0.0033)</td>
</tr>
<tr>
<td></td>
<td>(0.0030)</td>
<td>(0.0026)</td>
</tr>
<tr>
<td></td>
<td>(0.0031)</td>
<td>(0.0035)</td>
</tr>
<tr>
<td></td>
<td>(0.0060)</td>
<td>(0.0067)</td>
</tr>
<tr>
<td></td>
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<td>yes</td>
</tr>
<tr>
<td>Within-R2</td>
<td>0.0675</td>
<td>0.283</td>
</tr>
<tr>
<td>N</td>
<td>3,274,198</td>
<td>7,680,728</td>
</tr>
<tr>
<td>Cities</td>
<td>533</td>
<td>533</td>
</tr>
</tbody>
</table>

Notes: * $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$.  
!! Reference group for units in structure is N/A and needs to be changed.
Table 4: Rank of cities by estimated housing price index.

<table>
<thead>
<tr>
<th>City</th>
<th>Population</th>
<th>Rent Index</th>
</tr>
</thead>
<tbody>
<tr>
<td>Honolulu, HI</td>
<td>907,574</td>
<td>1312.76</td>
</tr>
<tr>
<td>San Jose-Sunnyvale-Santa Clara, CA</td>
<td>1,839,700</td>
<td>1252.62</td>
</tr>
<tr>
<td>Los Angeles-Long Beach-Santa Ana, CA</td>
<td>12,874,797</td>
<td>1157.05</td>
</tr>
<tr>
<td>San Francisco-Oakland-Fremont, CA</td>
<td>4,317,853</td>
<td>1148.75</td>
</tr>
<tr>
<td>Washington-Arlington-Alex., DC-VA-MD-WV</td>
<td>5,476,241</td>
<td>1142.28</td>
</tr>
<tr>
<td>New York-New Jersey-Long Isl., NY-NJ-PA</td>
<td>19,069,796</td>
<td>1118.46</td>
</tr>
<tr>
<td>Santa Barbara-Santa Maria-Goleta, CA</td>
<td>407,057</td>
<td>1117.70</td>
</tr>
<tr>
<td>Oxnard-Thousand Oaks-Ventura, CA</td>
<td>802,983</td>
<td>1095.97</td>
</tr>
<tr>
<td>Santa Cruz-Watsonville, CA</td>
<td>256,218</td>
<td>1012.10</td>
</tr>
<tr>
<td>San Diego-Carlsbad-San Marcos, CA</td>
<td>3,053,793</td>
<td>1001.02</td>
</tr>
<tr>
<td>Lawton, OK</td>
<td>113,228</td>
<td>330.28</td>
</tr>
<tr>
<td>Anniston-Oxford, AL</td>
<td>114,081</td>
<td>329.33</td>
</tr>
<tr>
<td>Saginaw-Saginaw Township North, MI</td>
<td>200,050</td>
<td>325.06</td>
</tr>
<tr>
<td>Huntington-Ashland, WV-KY-OH</td>
<td>285,624</td>
<td>323.11</td>
</tr>
<tr>
<td>Decatur, AL</td>
<td>151,399</td>
<td>321.53</td>
</tr>
<tr>
<td>Brownsville-Harlingen, TX</td>
<td>396,371</td>
<td>320.61</td>
</tr>
<tr>
<td>Flint, MI</td>
<td>424,043</td>
<td>316.47</td>
</tr>
<tr>
<td>Johnstown, PA</td>
<td>143,998</td>
<td>307.73</td>
</tr>
<tr>
<td>Monroe, LA</td>
<td>174,086</td>
<td>297.80</td>
</tr>
<tr>
<td>McAllen-Edinburg-Mission, TX</td>
<td>741,152</td>
<td>291.55</td>
</tr>
</tbody>
</table>

Table 5: Rank of cities by average of log utility.

<table>
<thead>
<tr>
<th>City</th>
<th>Population</th>
<th>Average utility</th>
</tr>
</thead>
<tbody>
<tr>
<td>1  Ann Arbor, MI</td>
<td>347,563</td>
<td>4.91</td>
</tr>
<tr>
<td>2  Bridgeport-Stamford-Norwalk, CT</td>
<td>901,208</td>
<td>4.89</td>
</tr>
<tr>
<td>3  Jackson, MI</td>
<td>159,828</td>
<td>4.88</td>
</tr>
<tr>
<td>4  Barnstable Town, MA</td>
<td>221,151</td>
<td>4.87</td>
</tr>
<tr>
<td>5  Flint, MI</td>
<td>424,043</td>
<td>4.87</td>
</tr>
<tr>
<td>6  Worcester, MA</td>
<td>803,701</td>
<td>4.85</td>
</tr>
<tr>
<td>7  Detroit-Warren-Livonia, MI</td>
<td>4,403,437</td>
<td>4.82</td>
</tr>
<tr>
<td>8  Boulder, CO</td>
<td>303,482</td>
<td>4.82</td>
</tr>
<tr>
<td>9  Decatur, AL</td>
<td>151,399</td>
<td>4.81</td>
</tr>
<tr>
<td>10 Hartford-West Hartford-East Hartford, CT</td>
<td>1,195,998</td>
<td>4.81</td>
</tr>
<tr>
<td>244 Corpus Christi, TX</td>
<td>416,095</td>
<td>4.37</td>
</tr>
<tr>
<td>245 Honolulu, HI</td>
<td>907,574</td>
<td>4.36</td>
</tr>
<tr>
<td>246 Laredo, TX</td>
<td>241,438</td>
<td>4.36</td>
</tr>
<tr>
<td>247 El Paso, TX</td>
<td>751,296</td>
<td>4.34</td>
</tr>
<tr>
<td>248 Lynchburg, VA</td>
<td>247,447</td>
<td>4.32</td>
</tr>
<tr>
<td>249 Utica-Rome, NY</td>
<td>293,280</td>
<td>4.32</td>
</tr>
<tr>
<td>250 Chico, CA</td>
<td>220,577</td>
<td>4.30</td>
</tr>
<tr>
<td>251 Madera-Chowchilla, CA</td>
<td>148,632</td>
<td>4.28</td>
</tr>
<tr>
<td>252 Jacksonville, NC</td>
<td>173,064</td>
<td>4.28</td>
</tr>
<tr>
<td>253 Amarillo, TX</td>
<td>246,474</td>
<td>4.25</td>
</tr>
</tbody>
</table>
Table 6: Rank of cities by variance of log utility.

<table>
<thead>
<tr>
<th>City</th>
<th>Population</th>
<th>S.D. Utility</th>
</tr>
</thead>
<tbody>
<tr>
<td>1  Santa Cruz-Watsonville, CA</td>
<td>256,218</td>
<td>0.75</td>
</tr>
<tr>
<td>2  Punta Gorda, FL</td>
<td>156,952</td>
<td>0.74</td>
</tr>
<tr>
<td>3  Boulder, CO</td>
<td>303,482</td>
<td>0.70</td>
</tr>
<tr>
<td>4  Springfield, OH</td>
<td>139,671</td>
<td>0.69</td>
</tr>
<tr>
<td>5  Springfield, IL</td>
<td>208,182</td>
<td>0.68</td>
</tr>
<tr>
<td>6  San Jose-Sunnyvale-Santa Clara, CA</td>
<td>1,839,700</td>
<td>0.67</td>
</tr>
<tr>
<td>7  Durham-Chapel Hill, NC</td>
<td>501,228</td>
<td>0.66</td>
</tr>
<tr>
<td>8  Bridgeport-Stamford-Norwalk, CT</td>
<td>901,208</td>
<td>0.66</td>
</tr>
<tr>
<td>9  San Francisco-Oakland-Fremont, CA</td>
<td>4,317,853</td>
<td>0.65</td>
</tr>
<tr>
<td>10 Lubbock, TX</td>
<td>276,659</td>
<td>0.65</td>
</tr>
<tr>
<td>244 South Bend-Mishawaka, IN-MI</td>
<td>317,538</td>
<td>0.42</td>
</tr>
<tr>
<td>245 Myrtle Beach-North Myrtle Beach-Conway, SC</td>
<td>263,868</td>
<td>0.41</td>
</tr>
<tr>
<td>246 Anderson, IN</td>
<td>131,417</td>
<td>0.41</td>
</tr>
<tr>
<td>247 Warner Robins, GA</td>
<td>135,715</td>
<td>0.41</td>
</tr>
<tr>
<td>248 Lynchburg, VA</td>
<td>247,447</td>
<td>0.40</td>
</tr>
<tr>
<td>249 Appleton, WI</td>
<td>221,894</td>
<td>0.40</td>
</tr>
<tr>
<td>250 Janesville, WI</td>
<td>160,155</td>
<td>0.37</td>
</tr>
<tr>
<td>251 Waco, TX</td>
<td>233,378</td>
<td>0.37</td>
</tr>
<tr>
<td>252 Macon, GA</td>
<td>231,576</td>
<td>0.36</td>
</tr>
<tr>
<td>253 Panama City-Lynn Haven, FL</td>
<td>164,767</td>
<td>0.35</td>
</tr>
</tbody>
</table>
Table 7: Regression coefficient on 2009 population size of average and standard deviation of real wage by skill category.

<table>
<thead>
<tr>
<th>Skill Category</th>
<th>average</th>
<th>standard deviation</th>
<th>N</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. No high school</td>
<td>-0.0112</td>
<td>0.0300***</td>
<td>205</td>
</tr>
<tr>
<td>2. High school degree</td>
<td>-0.0116*</td>
<td>0.0131***</td>
<td>253</td>
</tr>
<tr>
<td>3. Some college</td>
<td>-0.0051</td>
<td>0.0158***</td>
<td>252</td>
</tr>
<tr>
<td>4. Bachelor</td>
<td>0.0078</td>
<td>0.0240***</td>
<td>251</td>
</tr>
<tr>
<td>5. Master</td>
<td>0.0429***</td>
<td>0.0419***</td>
<td>221</td>
</tr>
<tr>
<td>6. MD,...</td>
<td>-0.0352</td>
<td>0.0543***</td>
<td>89</td>
</tr>
<tr>
<td>7. PhD</td>
<td>-0.0332</td>
<td>0.0405**</td>
<td>92</td>
</tr>
<tr>
<td>All skill categories</td>
<td>0.0179***</td>
<td>0.0232***</td>
<td>253</td>
</tr>
</tbody>
</table>

Notes: 1. For many small cities we observe less than two workers in the very low and very high education groups and cannot estimate the standard deviation. These city-group pairs are dropped; the samples on which the regressions are based do therefore systematically vary and the results are only indicative.
2. Standard error in parentheses; * $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$. 
Figure 15: Skill distribution by population size conditional on 7 observed educational levels. Left graphs: Mean; Right graphs: Standard Deviation.
Figure 15: continued.
References


