

Category theory in philosophy of mathematics and philosophy of science

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March 9, 2011

An updated version with links will be available at: www.princeton.edu/~hhalvors/teaching/phi536_s2011/reading-list.pdf

1 Does category theory break set theory?

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2 Does category theory provide an alternative foundation of mathematics?

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4 Miscellaneous

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