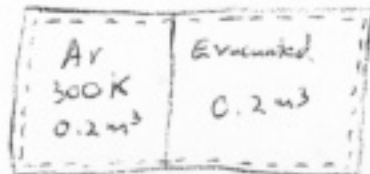
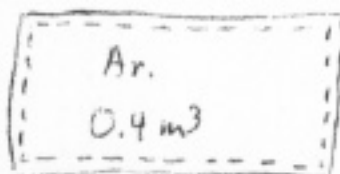


11.46 | 1 kmol Ar.



1.



2.

Assume the system is adiabatic and no work is done.

First Law: $Q = \Delta U + W$, since $W = Q = 0 \Rightarrow \Delta U = 0$.

$$\text{Eq. 11.44: } \Delta u = \int_1^2 c_v dT + \int_1^2 [T \left(\frac{\partial p}{\partial T} \right) - p] dv = 0$$

$$\text{Van der Waals: } p = \frac{RT}{v-b} - \frac{a}{v^2}$$

$$\left[T \left(\frac{\partial p}{\partial T} \right) - p \right] = T \left(\frac{R}{v-b} \right) - p = \frac{RT}{v-b} - \left[\frac{RT}{v-b} - \frac{a}{v^2} \right] = \frac{a}{v^2}$$

Since Ar is a monatomic gas, $C_v = \frac{3}{2} R$

$$\Rightarrow 0 = \int_1^2 \frac{3}{2} R dT + \int_1^2 \frac{a}{v^2} dv$$

$$\frac{3}{2} R (T_2 - T_1) - a \left[\frac{1}{v_2} - \frac{1}{v_1} \right] = 0$$

$$\Rightarrow T_2 = T_1 + \frac{2a}{3R} \left[\frac{1}{v_2} - \frac{1}{v_1} \right]$$

$$a = \frac{27}{64} \frac{R^2 T_c^2}{P_c}, \quad T_c = 151 \text{ K}, \quad P_c = 48.6 \text{ bar (A-1)}$$

$$\Rightarrow \boxed{T_2 = 272.6 \text{ K}}$$

For an ideal gas, u is a function of T only, so

$$\boxed{T_2 = 300 \text{ K}}, \quad \text{since } \Delta u = 0.$$

$$(11.4) \quad p(v-b) = RT$$

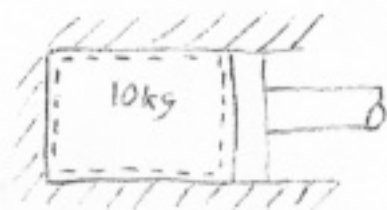
$$\text{Eq. 11.68: } C_p - C_v = -T \left(\frac{\partial v}{\partial T} \right)_p^2 \left(\frac{\partial p}{\partial v} \right)_T$$

$$\left(\frac{\partial v}{\partial T} \right)_p = \frac{R}{p} \quad \left(\frac{\partial p}{\partial v} \right)_T = -\frac{RT}{(v-b)^2} = -\frac{p^2}{RT}$$

$$\Rightarrow C_p - C_v = -T \left[\frac{R}{p} \right]^2 \left(-\frac{p^2}{RT} \right)$$

$$\boxed{C_p - C_v = R}$$

12.12



$$(mf)_{N_2} = 0.5$$

$$(mf)_{CO_2} = 0.3$$

$$(mf)_{O_2} = 0.2$$

$$p_1 = 1 \text{ bar}, T_1 = 280 \text{ K} \quad p_2 = 5 \text{ bar}, T_2 = 450 \text{ K}$$

Assume the system is adiabatic and the mixture behaves like an ideal gas.

$$\text{First Law: } Q = \Delta U + W = 0 \Rightarrow \Delta U = -W$$

$$\Rightarrow \frac{-W}{m} = (mf)_{N_2} \Delta u_{N_2} + (mf)_{CO_2} \Delta u_{CO_2} + (mf)_{O_2} \Delta u_{O_2}$$

from the ideal gas tables:

$$\frac{-W}{m} = (0.5) \left(\frac{9363 - 5813}{28} \right) + 0.3 \left(\frac{11742 - 6369}{44} \right) + 0.2 \left(\frac{9787 - 5822}{32} \right)$$

$$\Rightarrow \boxed{W = -1,229 \text{ kJ}}$$

$$\text{Entropy balance: } \Delta S = S_2 \left(\frac{S_2}{T} \right)_e + \sigma \Rightarrow \sigma = \Delta S$$

$$\sigma = \Delta S = (\Delta S)_{N_2} + (\Delta S)_{CO_2} + (\Delta S)_{O_2}$$

$$\Rightarrow \frac{\sigma}{m} = 0.5 \left[\frac{203.923 - 189.073 - 8.314 \ln 5}{28} \right] + \frac{0.3}{44} (230.194 - 211.376 - 8.314 \ln 5)$$

$$+ \frac{0.2}{32} (217.342 - 203.141 - 8.314 \ln 5)$$

$$\Rightarrow \boxed{\sigma = 0.5024 \text{ kJ/K}}$$