

Institutional Finance

Lecture 09 : Banking and Maturity Mismatch

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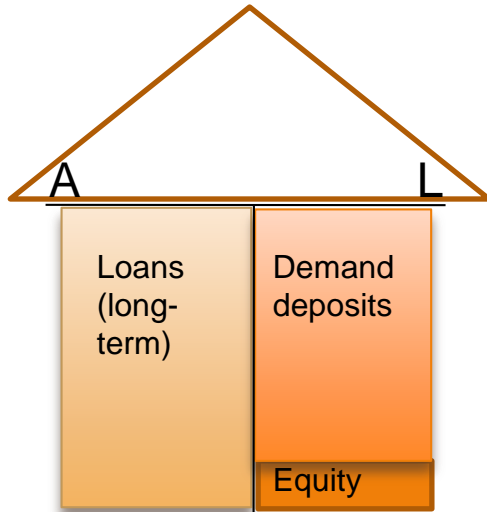
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|| ROLE OF BANKS

- Select/monitor borrowers
 - Sharpe (1990)
- Reduce
 - asymmetric info
 - idiosyncratic riskby bundling assets/mortgages (security design)
 - Opaqueness is not necessarily bad
 - Gorton-Pennachi (1990)
- Insurer of idiosyncratic liquidity shocks
 - Diamond-Dybvig (1983), Allen-Gale,

SHADOW BANKING SYSTEM

Traditional Banking



Role of banks

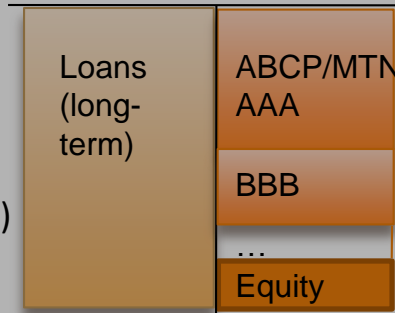
Channel funds	Long-run repayment
Maturity transformation	Retail funding
Info-insensitive securities	Demand deposits

Originate & distribute

Securitization

- Pooling
- Tranching
- Insuring (CDS)

SIV/Conduit



Dual purpose

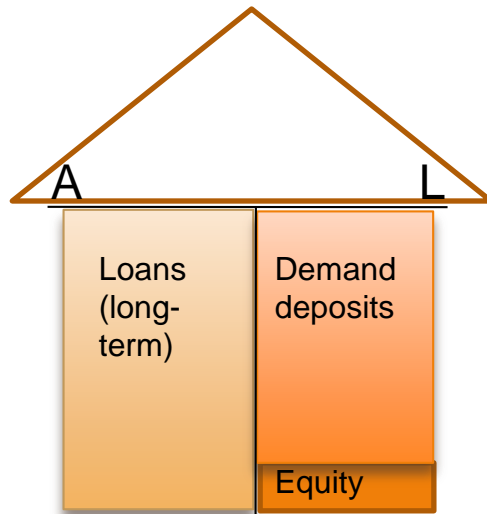
- Tradable asset
- Collateral

→ feeds repo market for leveraging

Prospect of selling off
 Wholesale funding (money market funds, repo partners, conduits, SIVs, ...)
 ABCP, MTN, overnight repos, securities lending

CHANGING BANKING LANDSCAPE

Traditional Banking



Role of banks

Channel funds	Long-run repayment	Prospect of selling off
Maturity transformation	Retail funding	Wholesale funding (money market funds, repo partners, conduits, SIVs, ...)
Info-insensitive securities	Demand deposits	ABCP, MTN, overnight repos, securities lending

Originate & distribute

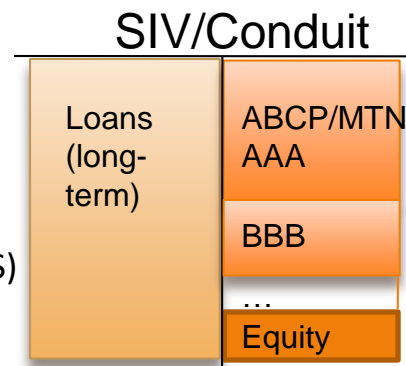
Securitization

- Pooling
- Tranching
- Insuring (CDS)

Dual purpose

- Tradable asset
- Collateral

→ feeds repo market for leveraging



|| MATURITY MISMATCH: DIFFERENT THEORIES

- Diamond-Dybvig (1983)
 - Insure against liquidity shocks (sudden expenditures)
- Calomiris-Kahn (1991), Diamond-Rajan (2001)
 - Control management – withdraw funds when CEO shirks
- Brunnermeier-Oehmke (2009)
 - Maturity rat race
 - Excessive short-term funding
- Extending leveraging theory

DIAMOND AND DYBVIK MODEL

- Three dates, $t \in \{0, 1, 2\}$
- Continuum of ex ante identical agents
- Everyone endowed with one unit good each
- Assume CRRA utility

$$u(c) = \frac{1}{1-\gamma} c^{1-\gamma} \quad \gamma > 0$$

if $\gamma=1$, log utility $u(c)=\log(c)$

TECHNOLOGY

- Two assets are available
 - Short-term project
 - : one unit invested at t gives 1 unit at $t+1$.
 - Long-term project
 - : one unit invested at t gives R units at $t+2$, but only $L \leq 1$ if liquidated early at $t+1$.

Investment projects	t=0	t=1	t=2
Risky investment project			
(a) Continuation	-1	0	$R > 1$
(b) Early liquidation	-1	L	0
Storage technology			
(a) From $t=0$ to $t=1$	-1	1	
(b) From $t=1$ to $t=2$		-1	1

|| PREFERENCE SHOCK

- At date 0, uncertainty over preferences
 - With probability λ , “early consumers” only consume at $t=1$
 - With probability $1-\lambda$, “late consumers” only consume at $t=2$

$$U(c_1, c_2) = \begin{cases} u(c_1) & \text{with prob } \lambda \\ u(c_2) & \text{with prob } 1 - \lambda \end{cases}$$

- Uncertainty is resolved at date 1.
 - ➔ Agents try to insure themselves against their uncertain liquidity needs.
- Independence across individual
 - ➔ No aggregate uncertainty.
 λ of them are “early consumers” with certainty.

|| CASE 1 : AUTARKY CASE

- No trading
- Each agent invests
 - x in the long-term project and
 - $(1-x)$ in the short-term project to maximize ex ante expected utility

$$\begin{aligned} \max_x \quad & \lambda u(c_1) + (1 - \lambda)u(c_2) \\ \text{s.t.} \quad & c_1 = xL + (1 - x) \\ & c_2 = xR + (1 - x) \end{aligned}$$

- Note that $c_1 \in [L,1]$, $c_2 \in [1,R]$
- Welfare can be improved if trading of asset is allowed at $t=1$

|| CASE 2 : MUTUAL FUND ARRANGEMENT

- Agents can sell their long-term project at $t=1$
- Early consumers will sell their long-asset to late consumers and get short-asset to consume
- Price of long-asset should be $p=1$
 - with $p=1$, investors are indifferent between short-term and long-term asset at $t=0$
 - for $p \neq 1$, investors either invest all in short-term asset or all in long-term asset

→ $c_1=1, c_2=R$. Better than autarky

Can this be improved?

|| CASE 3 : BANK ARRANGEMENT

- By forming a bank, optimal insurance can be provided
- Bank offers a deposit contract (c_1^*, c_2^*) which maximizes the agents' ex ante utility

$$\max \lambda u(c_1) + (1 - \lambda)u(c_2)$$

$$\text{s.t. } \lambda c_1 = 1 - x$$

$$(1 - \lambda)c_2 = Rx$$

|| BANK ARRANGEMENT

- From the first order condition

$$\left(\frac{c_1}{c_2}\right) = \left(\frac{1}{R}\right)^{\frac{1}{\gamma}}$$

- Mutual fund arrangement is optimal only if $\gamma=1$ (log utility).
- If $\gamma>1$, smoother consumption: $c_1^*>1, c_2^*<R$

➔ However, possibility of bank run

|| BANK RUN

- There is a bank run equilibrium where even late consumers withdraw early, fearing that others withdraw
- Let y be proportion of late consumers who withdraw. Total withdrawal at date 1 is $\hat{\lambda} = \lambda + (1 - \lambda)y$. Let $L=1$.
- **Sequential servicing constraint!**
- Payoffs

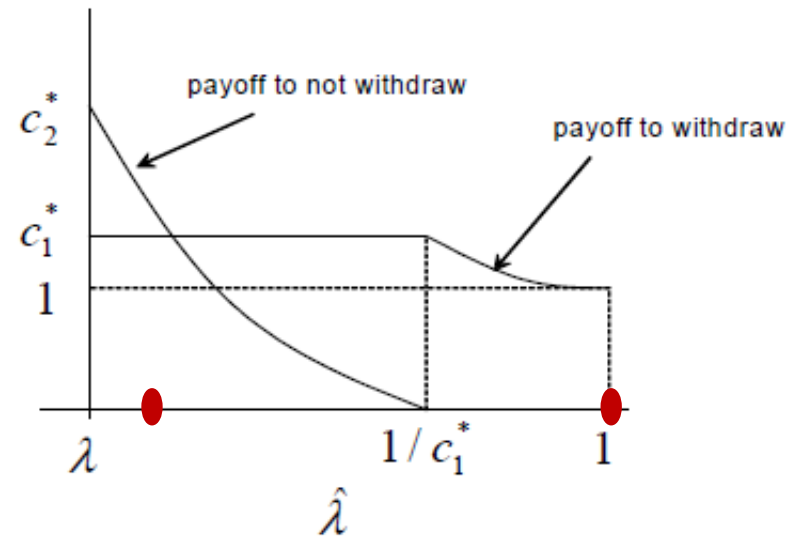


BANK RUN

- Payoffs

	$\hat{\lambda} \leq 1/c_1^*$	$\hat{\lambda} > 1/c_1^*$
Withdraw	c_1^*	$\frac{1}{\hat{\lambda}}$
Not withdraw	$\frac{1 - \hat{\lambda}c_1^*}{1 - \hat{\lambda}}R_2$	0

- Bank run is also Nash equilibrium
- How to prevent run?
 - Suspension of convertibility
 - Deposit insurance



|| CASH IN THE MARKET PRICING-ALLEN AND GALE

- Aggregate risk is introduced $\rightarrow \lambda_L < \lambda_H$
- Uncertainty revealed at $t=1$
- Price of long-asset
 - p_H if $\lambda=\lambda_H$
 - p_L if $\lambda=\lambda_L$
- At $t=0$,
 - aggregate investment in short term project : $1-x$
 - aggregate investment in long term project : x

PRICE OF LONG ASSET AT T=1

- If $\lambda = \lambda_L$, enough “late consumers” (liquidity) to absorb selling from “early consumers”
 - $p_L = R$, since
 - if $p_L > R$ even late diers will sell long-term asset and
 - if $p_L > R$ excessive demand for long asset once L is realized.
- If $\lambda = \lambda_H$, too many sellers (“early consumers”) but not enough liquidity (“late consumers”)
 - Supply of asset = $\lambda_H x$
 - Supply of cash = $(1 - \lambda_H)(1 - x)$
 - Market clearing, “cash in the market pricing”
→ $p_H = (1 - \lambda_H)(1 - x) / (\lambda_H x)$. Note that $p_H < p_L$

|| MATURITY RAT RACE

- A financial institution can borrow
 - from multiple creditors
 - at different maturities
- **Negative externality causes excessively short-term financing:**
 - shorter maturity claims dilute value of longer maturity claims
- Externality arises
 - for any maturity structure
 - particularly during times of high volatility (crises)

Successively unravels all long-term financing:

→ *A Maturity Rat Race*

MODEL SETUP: CREDIT MARKETS

- Risk-neutral, competitive lenders
- All promised interest rates
 - are endogenous
 - depend aggregate maturity structure
- Debt contracts specifies maturity and face value:
 - can match project maturity: $D_{0,T}$
 - or shorter maturity $D_{0,t}$, then rollover $D_{t,t+\tau}$ etc.
 - lenders make uncoordinated rollover decisions
- Maturing debt has equal priority in default:
 - proportional to face value

|| MODEL SETUP: CREDIT MARKETS (2)

- Financial institution deals bilaterally with multiple creditors:
 - simultaneously offer debt contracts to creditors
 - cannot commit to aggregate maturity structure
 - can commit to aggregate amount raised
- An equilibrium maturity structure must satisfy **two conditions**:
 1. **Break even**: all creditors must break even
 2. **No deviation**: no incentive to change one creditor's maturity

INTUITION BEHIND THE DEVIATION

- Rollover face value $D_{t,T}$ (promised interest rate)
 - is endogenous
 - adjusts to interim information

Interim Signal	$D_{t,T}$	default	no default
Negative	high	LT creditors lose	no effect
Positive	low	LT creditors gain	no effect

- Since default more likely after negative signals:
 - On average LT creditors lose

|| A SIMPLE EXAMPLE WITH ONE ROLL OVER DATE

- For now: focus on only one possible rollover date, $t < T$
- α is fraction of 'short-term' debt with maturity t
- Outline of thought experiment:
 - Conjecture an equilibrium in which all debt has maturity T
 - Calculate break-even face values
 - At break-even interest rate, is there an incentive to deviate?

|| A SIMPLE EXAMPLE WITH ONE ROLL OVER DATE

- θ (investment payoff at T) only takes two values:
 - θ^H with probability p
 - θ^L with probability $1 - p$
- $p \sim$ uniform on $[0; 1]$, realized at t .
- If all financing has maturity T:

$$\frac{1}{2}\theta^L + \frac{1}{2}D_{0,T} = 1, \quad D_{0,T} = 2 - \theta^L$$

- Break-even condition for first t-rollover creditor:

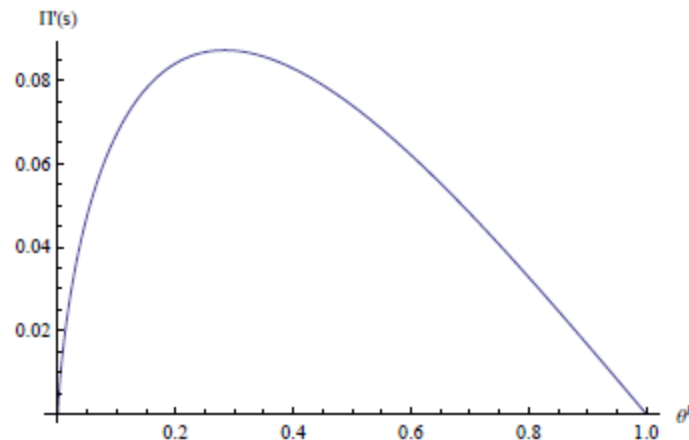
$$(1 - p) \frac{D_{t,T}}{2 - \theta^L} \theta^L + p D_{t,T} = \underbrace{D_{0,t}}_{=1}, \quad D_{t,T} = \frac{2 - \theta^L}{2p(1 - \theta^L) + \theta^L}$$

|| A SIMPLE EXAMPLE WITH ONE ROLL OVER DATE

- Deviation payoff from all long-term financing by

$$\begin{aligned}\frac{\partial \Pi}{\partial \alpha} &= \int_0^1 p [D_{0,T} - D_{t,T}(p)] dp \\ &= \frac{1}{2} D_{0,T} - \int_0^1 p D_{t,T}(p) dp > 0?\end{aligned}$$

- Deviation from $\alpha=0$?



|| GENERAL ONE-STEP DEVIATION

- Same argument for any maturity structure that involves some amount of long term financing with maturity T .

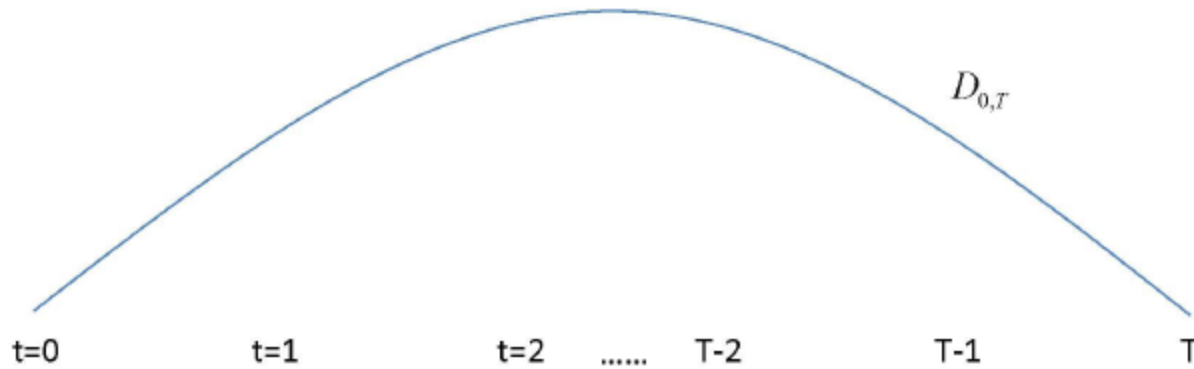
Proposition

One-step Deviation. *Under a regularity condition on $F(\cdot)$, in any conjectured equilibrium maturity structure with some amount of long-term financing ($\alpha \in [0; 1)$), the financial institution has an incentive to increase the amount of short-term financing by switching one additional creditor from maturity T to the shorter maturity $t < T$, since $\frac{\partial \Pi}{\partial \alpha} > 0$. As a result, the maturity structure of the financial institution shortens to time- t financing.*

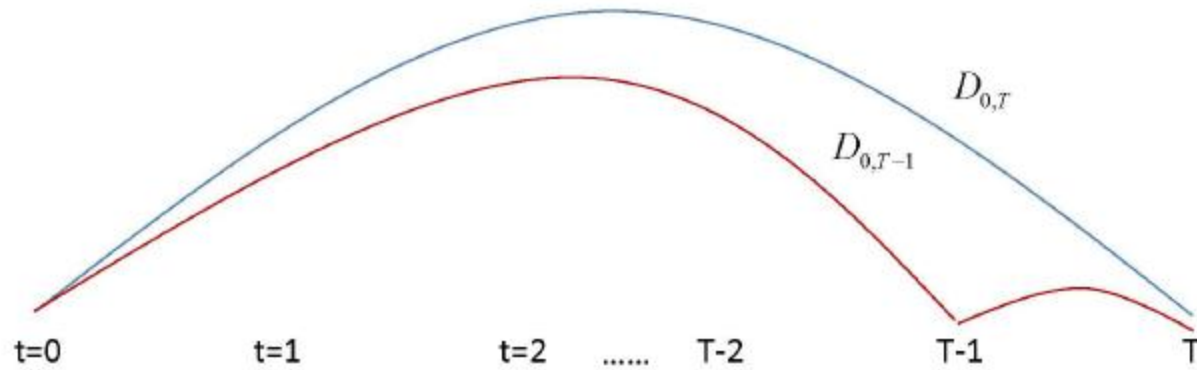
|| MANY ROLLOVER DATES: THE MATURITY RACE

- Up to now: focus on one potential rollover date
Assume everyone has maturity of length T
Show that there is a deviation to shorten maturity to t
 - This extends to multiple rollover dates
Assume all creditors roll over for the first time at some time $\tau < T$
By same argument as before, there is an incentive to deviate
- *Successive unraveling of maturity structure*

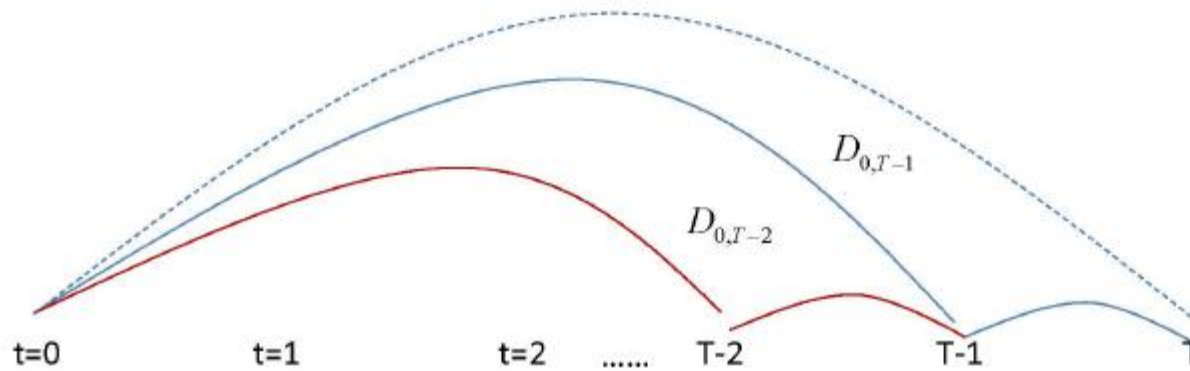
THE MATURITY RISK PREMIUM: SUCCESSIVE UNRAVELING



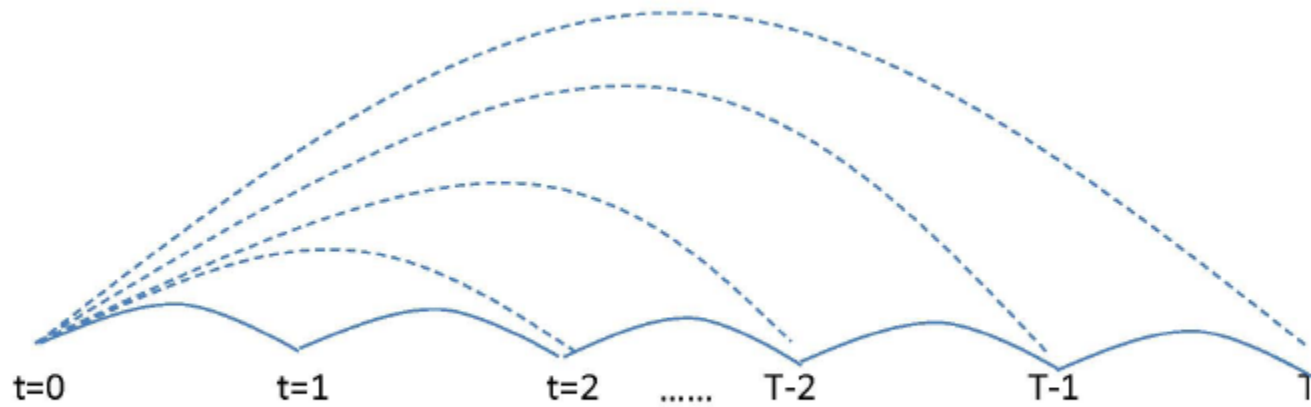
THE MATURITY RACE: SUCCESSIVE UNRAVELING



THE MATURITY RACE: SUCCESSIVE UNRAVELING



THE MATURITY RACE: SUCCESSIVE UNRAVELING



|| RAT RACE STRONGEST DURING CRISES

- Rat race stronger when more information is released at interim dates
 - ability to adjust financing terms becomes more valuable
- *Volatile environments, such as crises, facilitate rat race*
- Explains drastic shortening of unsecured credit markets in crisis
 - e.g. commercial paper during fall of 2008

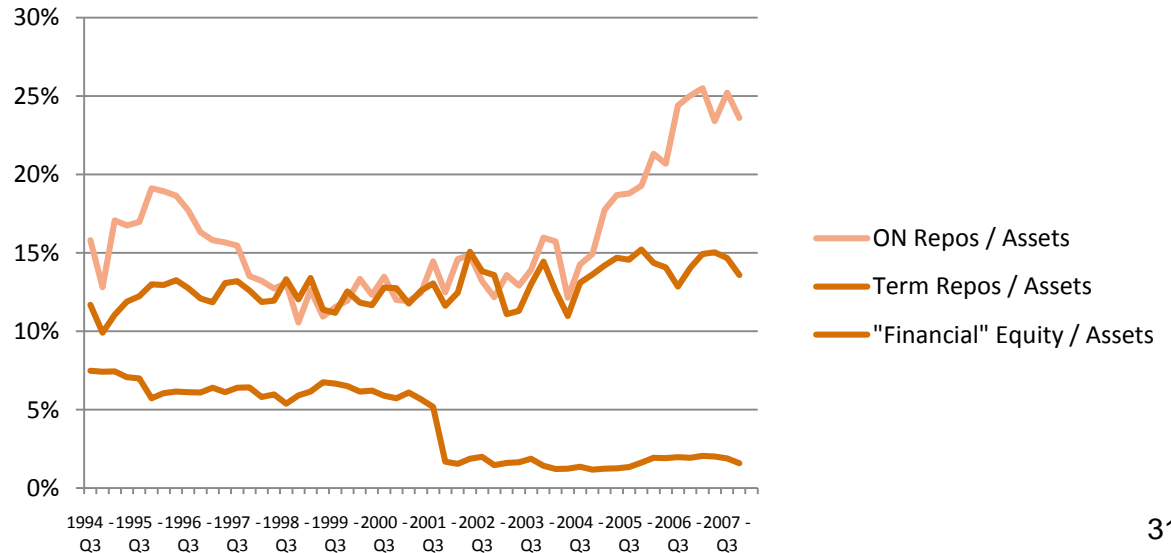
1.2 SHORTENING MATURITY: I-BANKS

Investment banks' main financing in 2007

- Repos 1150.9bn
- Security credit (subject to Reg T)
 - Margin accounts from HH or non-profit 853.5bn
 - From banks 335.7bn
- "Financial" equity 49.3bn

Increase in repo is due to overnight repos!

Repos as a Fraction of Broker/Dealers' Assets



1.3 WHY STRUCTURED PRODUCTS?

■ Good reasons

- Credit risk transfer risk who can best bear it
 - Banks: hold equity tranche to ensure monitoring
 - Pension funds: hold AAA rated assets due to restriction by their charter
 - Hedge funds: focus on more risky pieces
 - *Problem:* risks stayed mostly within banking system
banks held leveraged AAA assets – tail risk

■ Bad reasons - supply

- **Regulatory Arbitrage** – Outmaneuver Basel I (SIVs)
 - esp. reputational liquidity enhancements
- **Rating Arbitrage**
 - Transfer assets to SIV and issue AAA rated papers
 - instead of issuing A- minus rated papers
 - + banks' own rating was unaffected by this practice
 - ++ buy back AAA has lower capital charge (Basel II)

• ...

1.3 WHY STRUCTURED PRODUCTS?

- Bad reasons - demand
 - Naiveté – Reliance on
 - past low correlation among regional housing markets
 - ★ Overestimates value of top tranches
 - ★ explains why even investment banks held many mortgage products on their books
 - rating agencies - rating structured products is different
 - ★ Quant-skills are needed instead of cash flow skills
 - ★ **Rating at the edge** – AAA tranche just made it to be AAA
 - Trick your own fund investors – own firm (in case of UBS)
 - “Enhance” portfolio returns e.g. leveraged AAA positions – extreme tail risk
 - ★ searching for yield (mean)
 - ★ track record building (skewness: picking up nickels before the steamroller)
 - Attraction of illiquidity (no price exists) (fraction of “level 3 assets” went up a lot)
+ difficulty to value CDOs (correlation risk)
 - ★ “mark-to-model”: Mark “up”, but not “down”
 - ★ smooth volatility, increase Sharpe ratio, lower β , increase α
 - Implicit (hidden) leverage

1.4 CONSEQUENCES OF

“ORIGINATE AND DISTRIBUTE BANKING MODEL”

- Banks focus only on “**pipeline/warehouse risk**”
- Deterioration of lending standards
 - **Housing Frenzy**
 - **Private equity bonanza** – “going private trend”
LBO acquisition spree