Stati

Uniform Price Discr. Price (Limit Order Book)

Dynami

Sequential Trade Herding

Asset Pricing under Asymmetric Information Screening Models

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August 17, 2007

Classification of Models

Curti

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A Classification of Market Microstructure Models

- simultaneous submission of demand schedules
 - competitive rational expectation models
 - strategic share auctions
- sequential move models
 - screening models in which the market maker submits a supply schedule first
 - static
 - o uniform price setting
 - ♦ limit order book analysis
 - dynamic sequential trade models with multiple trading rounds
 - strategic market order models where the market maker sets prices ex-post

Static

Uniform Price Discr. Price (Limit Order Book)

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Screening Models à la Glosten

- Uninformed (risk-neutral) market maker sets whole supply schedule
 - market making sector is competitive
 - oligopolistic market making sector
 - market maker is monopolist
- Possibly informed trader submits
 - a single order which is executed at uniform price
 - many little orders in order to "walk along the limit order book" (discriminatory prices)

Book) Contrast

Dynam

Sequential Trade Herding

Uniform Price Setting - Glosten 1989

- Contrast competitive market maker sector with monopolistic market maker (specialist system NYSE).
- Model setup
 - market maker(s) set price (supply) schedule
 - single trader submits order
 - risk-averse with CARA utility function
 - endowment shock of u
 - private signal $S^i = v + \epsilon$
 - two-dimensional screening problem
 Glosten (1989) reduces it to a one-dimensional problem (see later)

Sequential Trade

Uniform Price Setting - Glosten 1989

- Competitive price schedule: $P^{CO} = E[v|x]$
 - Perfect competition
 - ⇒ expected profit for any order size x is ZERO.
 - prevents market makers from effectively screening orders
 - ⇒ leads to instability formally, existence problem for certain parameters (Hellwig JET 1994 shows that this is due to unbounded support of type sapce and it existence problem is different to the one in Rothschild & Stiglitz)
- Monopolistic price schedule:

$$P^{\mathsf{mo}} = \operatorname{arg\,max} E[[P^{\mathsf{mo}}(x^*(\cdot)) - v]x^*(\cdot)],$$

where $x^*(\cdot)$ is the optimal order size.

- principal-agent problem
- principal sets menu of contracts $(x, P^{mo}(x))$
- Cross-subsidization: large profit from small trades small (-ve) profit from large trades
- market with monopolistic setting stays open for larger trade sizes than a market with multiple market markers

D....

Sequential Trade Herding

Discrim. Pricing (Limit Order Book) Glosten 1994 - BRM 2000

 "upper tail" conditional expectations for next marginal order y

$$P^{\mathsf{CO}}(y) = E[v|x \geq y]$$

- trader who buy only a tiny marginal quantity have to pay a higher (ask) price ⇒ small trade spread
- competitive market makers do not know whether trader only buys first marginal unit or continues to buy further units.
- cross-subsidization from small orders to large orders
- limit order book is immune to "cream skimming" of orders by competing exchanges (no advantage of order splitting).

Uniform Price Discr. Price (Limit Order Book)

Contrast

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Sequential Trad

Discrim. Pricing - Biais, Rochet & Martimo Oligopolistic Market Makers

- ullet oligopolistic screening game (special cases $I=1,\ I=\infty$)
- Stage 1: risk-neutral market maker(s) set supply schedule p(x) (limit order book)
- Stage 2: informed trader buy $x = \sum_{i=1}^{I} x^{i}$ shares
 - xⁱ for market maker i
 - transfer to mm i: $t^i(x^i) = \int_0^{x^i} p(q)dq$, $T(x) = \sum_i t^i(x^i)$
 - trader's endowment shock *u*
 - trader's signal S, where $v = S + \varepsilon$. $\varepsilon \sim \mathcal{N}\left(0, \sigma^2\right)$ u and S have bounded support.
 - trader's final wealth $W = v(u+x) \sum_i t^i(x^i)$ (conditional on u, S, wealth W is normally distributed with E[v|S] = S, $Var[v|S] = Var[\varepsilon]$)

Classification of Models

Static

Uniform Price
Discr. Price
(Limit Order
Book)

Contrast

Dynam

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Sequential Trade Herding 1987-crash

BRM: One Dimensional Screening

- **Stage 2:** (ctd.) "Glosten (1989)-trick"
 - with CARA utility function

$$E[W|u,S] - \frac{\rho}{2}V[W|u,S]$$

$$= (x+u)S - T(x) - \frac{\rho}{2}(x+u)^{2}\underbrace{Var[v|S]}_{=\sigma^{2}}$$

$$= \underbrace{\left(uS - \frac{\rho\sigma^{2}}{2}u^{2}\right)}_{\text{independent of }x} + \underbrace{\left(\underbrace{xS - \rho\sigma^{2}xu}_{\theta_{x}} - \frac{\rho\sigma^{2}}{2}x^{2} - T(x)\right)}_{\theta_{x}}$$

$$= \underbrace{\left(uS - \frac{\rho\sigma^{2}}{2}u^{2}\right)}_{\text{independent of }x} + \underbrace{\left(\underbrace{xS - \rho\sigma^{2}xu}_{\theta_{x}} - \frac{\rho\sigma^{2}}{2}x^{2} - T(x)\right)}_{\theta_{x}}$$

depends on x \Rightarrow Info-Rent

- This reduces it to a one-dimensional screening problem
- function $v(\theta) = E[v|\theta]$ of (one-dimensional) type θ $1 > \dot{v}(\theta) > 0$

Classification of Models

of Model

Uniform Price Discr. Price (Limit Order

Book) Contras

Contras

Dynan

Sequential Trade Herding

BRM: First Best Benchmark

ex-ante

optimal trading mechanism
$$\left\{ \begin{matrix} \text{transfers trading volume} \\ \downarrow \\ \tau\left(\theta\right) \;, \quad x\left(\theta\right) \end{matrix} \right\}$$

$$\max_{\{\tau(\theta), x(\theta)\}} \int_{\underline{\theta}}^{\overline{\theta}} \left(\theta x(\theta) - \frac{\rho \sigma^2}{2} x(\theta)^2 - \tau(\theta) \right) f(\theta) d\theta$$
s.t.
$$\int_{\theta}^{\overline{\theta}} \left(\tau(\theta) - v(\theta) x(\theta) \right) f(\theta) d\theta = \Pi$$

Π determines how surplus is distributed between P and A

$$\Longrightarrow \max \int_{\underline{\theta}}^{\overline{\theta}} (\underbrace{\theta x (\theta) - \frac{\rho \sigma^2}{2} x (\theta)^2 - v (\theta) x (\theta)}_{\text{surplus}} - \Pi) f (\theta) d\theta$$

BRM: First Best Benchmark

for a given $\boldsymbol{\theta}$

$$\theta - \rho \sigma^{2} x(\theta) - v(\theta) = 0$$

$$x^{*}(\theta) = \frac{\theta - v(\theta)}{\rho \sigma^{2}}$$

$$= E[-u|\theta], \text{ since } u = -\frac{\theta - S}{\rho \sigma^{2}}$$

- Assume $x^* (\underline{\theta}) < 0 < x^* (\overline{\theta})$ $\Longrightarrow \exists \theta_0 \text{ s.t. } x^* (\theta_0) = 0$
- almost all θ -types trade (see later that $\forall \theta > \theta_0 \Longrightarrow$ buy $\forall \theta < \theta_0 \Longrightarrow$ sell)

Classification of Models

Statio

Uniform Pric

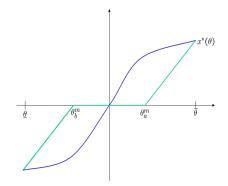
Discr. Price (Limit Order

Book) Contra

Dynam

Sequential Trad Herding 1987-crash

BRM: Monopolistic Screening $x^*(\theta)$ and $x_m(\theta)$



Discr. Price (Limit Order Book)

Sequential Trade

under Adverse Selection

- social planner must elicit information
- Revelation Principle Any allocation that can be achieved with non-linear schedules T(x) can also be achieved with a truthful direct mechanism $\{\tau(\cdot), x(\cdot)\}.$

BRM: Implementable Allocation

Incentive compatibility

$$\theta \in \arg\max_{\widehat{\theta}} \left(\theta x \left(\widehat{\theta}\right) - \frac{\rho \sigma^2}{2} x \left(\widehat{\theta}\right)^2 - \tau \left(\widehat{\theta}\right)\right)$$

$$\Longrightarrow U\left(\theta\right) = \max_{\widehat{\theta}} \left(\underbrace{\theta x\left(\widehat{\theta}\right) - \frac{\rho\sigma^2}{2} x\left(\widehat{\theta}\right)^2 - \tau\left(\widehat{\theta}\right)}_{\text{informational rent}}\right)$$

 $\{\tau(\cdot), x(\cdot)\}\$ transfers and allocation



Classification of Models

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Uniform Price Discr. Price (Limit Order Book)

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Sequential Trade Herding

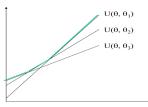
BRM: Dual (Mirrlees) Approach

 $\{U(\cdot),x(\cdot)\}$ informational rent (see Fudenberg & Tirole Ch. 7)

Lemma 1:

A pair $\{U(\cdot), x(\cdot)\}$ is implementable iff $U(\cdot)$ is convex on $[\underline{\theta}, \overline{\theta}]$, and for a.e. θ , $U(\theta) = x(\theta)$, $\frac{dU(\theta, \widehat{\theta}(\theta))}{d\theta} = \frac{\partial U}{\partial \theta} = x(\theta).$

envelope theorem



Classification of Models

Uniform Price Discr. Price (Limit Order Book)

Contras

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BRM: Monopolistic Screening

m.m.(principal) gets $\int_{\underline{\theta}}^{\overline{\theta}} \tau(x(\theta)) - v(\theta)x(\theta)$ replacing τ from information rent $U(\theta) = \theta x(\theta) - \frac{\rho \sigma^2}{2} x^2(\theta) - \tau(x(\theta))$, the m.m.'s objective becomes

$$\max_{\{U(\cdot),x(\cdot)\}} \int_{\underline{\theta}}^{\overline{\theta}} \{ [\theta - v(\theta)]x(\theta) - \frac{\rho\sigma^2}{2} [x(\theta)]^2 - U(\theta) \} f(\theta) d\theta$$

subject to

$$\text{IC} \quad \left\{ \begin{array}{c} U\left(\cdot\right) \text{ is convex on } \left[\underline{\theta},\overline{\theta}\right] \\ \dot{U}\left(\theta\right) = x\left(\theta\right) \quad \forall \theta \text{ (almost everywhere)} \end{array} \right.$$

ex-post PC $U(\theta) \ge 0$ **ex-post** participation constraints

(ex-post: since traders decide after knowing θ whether to participate)

Discr. Price (Limit Order Book)

Sequential Trade Herding

BRM: Monopolistic Screening Dual Approach

(replace $x(\theta)$ with $U(\theta)$)

$$\max_{U(\cdot)} B_m \left(U(\cdot), \dot{U}(\cdot) \right)$$

$$:= \int_{\underline{\theta}}^{\overline{\theta}} \left(\left[\theta - v\left(\theta \right) \right] \dot{U}\left(\theta \right) - \frac{\rho \sigma^2}{2} \dot{U}\left(\theta \right)^2 - U\left(\theta \right) \right) f\left(\theta \right) d\theta$$

s.t.
$$U(\cdot)$$
 convex $U(\theta) \ge 0$

Temporarily ignore convexity constraint and check ex-post. (Sufficient condition: $U(\cdot)$ is convex if

$$\forall \theta > \theta_0 \quad \frac{d}{d\theta} \left(\frac{1 - F(\theta)}{f(\theta)} \right) < 0$$

$$\forall \theta < \theta_0 \quad \frac{d}{d\theta} \left(\frac{F(\theta)}{f(\theta)} \right) > 0$$
(18)

$$\forall \theta < \theta_0 \quad \frac{d}{d\theta} \left(\frac{F(\theta)}{f(\theta)} \right) > 0$$
 (19)

BRM: Monopolistic Screening

$$\mathcal{L}\left(U,\dot{U}\right) = B_{m}\left(U,\dot{U}\right) + \int_{\underline{\theta}}^{\overline{\theta}} U(\theta) \qquad d\Lambda(\theta)$$

 ∞ many Lagrange multipliers different from type to type (ex-post constraint)

By complementary slackness condition, support of Λ be constrained in $(U_m)^{-1}(0)$, $(\theta$ -types which get zero info ret) view $\Lambda(\theta)$ as c.d.f., i.e., \exists a measure Λ

$$\Lambda(\theta) = \int_{\underline{\theta}}^{\theta} \frac{d\Lambda(s)}{\int_{\theta}^{\overline{\theta}} d\Lambda(s)} \qquad \text{(slight abuse of notation)}$$

BRM: Monopolistic Screening

Aside: Integrating by parts

$$\int_{\underline{\theta}}^{\overline{\theta}} U(\theta) d \left[\Lambda(\theta) - F(\theta) \right] = -\int_{\underline{\theta}}^{\overline{\theta}} \dot{U}(\theta) (\Lambda(\theta) - F(\theta)) d\theta + U(\overline{\theta})$$

Consequently, $\max \mathcal{L}\left(U,\dot{U}\right) =$

$$= \int_{\underline{\theta}}^{\overline{\theta}} \left(\left(\theta - v(\theta) + \frac{F(\theta) - \Lambda(\theta)}{f(\theta)} \right) \dot{U}(\theta) - \frac{\rho \sigma^2}{2} \dot{U}(\theta)^2 \right) f(\theta) d\theta + U(\overline{\theta}) (\Lambda(\theta) - 1)$$

max only if $\Lambda\left(heta
ight) = 1$ (since $U\left(\overline{ heta}
ight)$ is arbitrary)

pointwise maximization over $\dot{U}(\theta)$

$$\forall \theta \in \left[\underline{\theta}, \overline{\theta}\right], \ x_{m}(\theta) = \underbrace{\frac{\theta - v(\theta)}{\rho \sigma^{2}}}_{x^{*}(\theta)} + \frac{F(\theta) - \Lambda(\theta)}{f(\theta) \rho \sigma^{2}}$$

BRM: Monopolistic Screening

Complementary slackness condition $(d\Lambda = 0 \text{ for some } \theta)$

$$\forall \theta \in [\underline{\theta}, \theta_b^m] \quad \Lambda(\theta) = 0$$

$$\forall \theta \in [\theta_a^m, \overline{\theta}] \quad \Lambda(\theta) = 1$$

 \implies given (18) & (19), $U(\cdot)$ is convex and

Proposition 2

 $\exists \theta_a^m > \theta_0$ and $\theta_b^m < \theta$ s.t.

- (i) for all $\theta \in [\underline{\theta}, \theta_b^m)$, $x_m(\theta) = x^*(\theta) + \frac{F(\theta)}{\rho \sigma^2 f(\theta)}$
- (ii) for all $\theta \in [\theta_b^m, \theta_a^m]$, $x_m(\theta) = 0$ (no info rent)

(iii) for all
$$\theta \in (\theta_a^m, \overline{\theta}]$$
, $x_m(\theta) = x^*(\theta) - \frac{1 - F(\theta)}{\rho \sigma^2 f(\theta)}$

Classification of Models

Static

Uniform Price

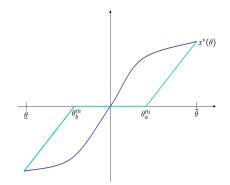
Discr. Price (Limit Order Book)

Contra

Dynam

Sequential Trade Herding 1987-crash

BRM: Monopolistic Screening $x^*(\theta)$ and $x_m(\theta)$



Discr. Price (Limit Order

Book)

BRM: Monopolistic Screening Price Schedule

for $\theta > \theta_2^m$ we know

(1)
$$\theta \geq \theta_a^m U(\theta) = 0 + \int_{\theta_a^m}^{\theta} \dot{U}'(s) ds = \int_{\theta_a^m}^{\theta} x(s) ds$$

(2)
$$U(\theta) = \theta x_m(\theta) - \frac{\rho \sigma^2 x_m(\theta)^2}{2} - T(x(\theta))$$
(1)=(2)
$$T(x(\theta)) = \theta x_m(\theta) - \frac{\rho \sigma^2 x_m(\theta)^2}{2} - \int_{\theta_m^2}^{\theta} x(s) ds$$

(1)=(2)
$$T(x(\theta)) = \theta x_m(\theta) - \frac{\rho \sigma^2 x_m(\theta)^2}{2} - \int_{\theta_a^m}^{\theta} x(s) ds$$

Differentiate w.r.t. θ

$$\frac{\partial T}{\partial x}\frac{\partial x}{\partial \theta} = x_m(\theta) + \theta \frac{\partial x}{\partial \theta} - \rho \sigma^2 x_m(\theta) \frac{\partial x_m}{\partial \theta} - x_m(\theta)$$

$$\frac{\partial T}{\partial x} = \theta - \rho \sigma^2 x_m(\theta)$$

We have

$$x_{m}(\theta) = \underbrace{x^{*}(\theta)}_{\frac{\theta - v(\theta)}{\sigma^{2}}} + \frac{F(\theta)}{\rho \sigma^{2} f(\theta)}$$

Book) Contras

Dynam

Sequential Trad Herding 1987-crash

BRM: Monopolistic Screening Price Schedule

$$\implies \frac{\partial T}{\partial x} = \theta - \theta + v(\theta) - \frac{F(\theta)}{f(\theta)}$$

$$t_m(x) = \frac{\partial T}{\partial x} = v(\theta) - \frac{F(\theta)}{f(\theta)}$$

for $\theta < \theta_b^m$ similar steps

$$\frac{\partial T}{\partial x} = v(\theta) + \frac{1 - F(\theta)}{f(\theta)}$$

Note that

$$t_m\left(x=0^+\right)=\theta_a^m>\theta_b^m=t_m\left(x=0^-\right)$$

"small trade spread" → ⟨₹⟩ ⟨₹⟩ ⟨₹⟩ ⟨₹⟩ ⟨₹⟩

Asset Pricing under Asym. Information

Screening Models

Classification of Models

Static

Uniform Price

Discr. Price (Limit Order Book)

Contras

Dynamic

Sequential Trade Herding 1987-crash

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BRM: Oligopolistic Screening

Limit Order Book vs. Uniform Pricing Röell (1998)

- Model setup
 - order size of trader is exogenous
 - is double exponentially distributed $f(x) = \frac{1}{2}ae^{-a|x|}$
 - conditional expectations
 - $E[\cdot|x \ge y] \Rightarrow$ linear schedule in limit order book
 - $E[v|x] = v_0 + \gamma x$ assumed \Rightarrow linear uniform price schedule
- $p^u(x) = v_0 + \frac{l-1}{l-2}\gamma x$ versus $p^d(x) = v_0 + \frac{l}{l-1}\frac{\gamma}{a} + \gamma x$

Contrast

Sequential Trade Herding 1987-crash

Limit Order Book vs. Uniform Pricing Röell (1998)

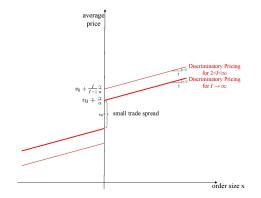


Figure: Limit Order Book.

Contrast

Sequential Trade Herding 1987-crash

Limit Order Book vs. Uniform Pricing Röell (1998)

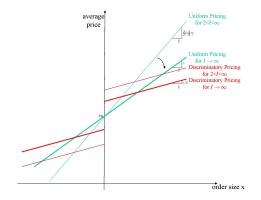


Figure: Limit Order Book and Uniform Pricing.

of Models

Static

Uniform Price Discr. Price (Limit Order Book)

Dynamic

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A Classification of Market Microstructure Models

- simultaneous submission of demand schedules
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of Models

Static Uniform Pri

Discr. Price (Limit Order Book)

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Sequential Trade Models à la Glosten & Milgrom (1985)

• order size is restricted to $x \in \{-1, +1\}$

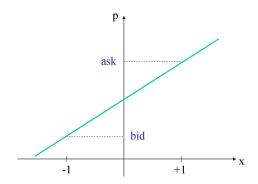


Figure: Bid-Ask Spread.

Classification of Models

Statio

Uniform Price Discr. Price (Limit Order Book)

Dynam

Sequential Trade Herding

Sequential Trade Models à la Glosten & Milgrom (1985)

- Monopolistic Market Maker Copeland & Galai (1983)
 - bid-ask spread is partially due to monopoly power partially due to adverse selection
 - difficult to handle in multi-period setting
- Competitive Market Makers Glosten & Milgrom (1985)
 - bid-ask spread is only due to adverse selection
 - multi-period setting

Classification of Models

Uniform Price Discr. Price (Limit Order

Contrast

Dynamic

Sequential Trade Herding 1987-crash

Glosten & Milgrom (1985)

Model Setup

- value of the stock \underline{v} and \overline{v}
- ullet with probability lpha an informed trader shows up
- ullet with probability (1-lpha) an uninformed trader shows up
- all traders are chosen from a pool of a continuum of traders, i.e., the probability that they will trade a second time is zero (rule out strategic considerations as in Kyle's)
- informed traders know true $\widetilde{v} \to \text{buys if } v > a \text{ sells if } v < b.$
- uninformed traders buy with probability μ and sell with probability 1μ .
- Note: Traders can only buy or sell 1 unit (No-Trade is also not allowed!)

Classification of Models

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Glosten & Milgrom (1985)

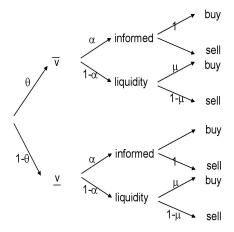


Figure: Tree.

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Sequential Trade Herding

Glosten & Milgrom (1985) Calculating Bid-Ask Spread

Buy order

$$\begin{array}{rcl} \mathsf{P}\left(\overline{\nu}\right) & = & \theta \\ \mathsf{P}\left(\mathsf{buy}|\overline{\nu}\right) & = & \alpha + (1-\alpha)\,\mu \\ \mathsf{P}\left(\mathsf{buy}|\underline{\nu}\right) & = & (1-\alpha)\,\mu \end{array}$$

Bayes' Rule

$$\begin{array}{ll} \mathsf{P}\left(\overline{\nu}|\mathsf{buy}\right) & = & \frac{\left(\alpha + \left(1 - \alpha\right)\mu\right)\theta}{\left(\alpha + \left(1 - \alpha\right)\mu\right)\theta + \left(1 - \alpha\right)\mu\left(1 - \theta\right)} \\ \mathsf{P}\left(\underline{\nu}|\mathsf{buy}\right) & = & 1 - \mathsf{P}\left(\overline{\nu}|\mathsf{buy}\right) \end{array}$$

Dynam

Sequential Trade Herding

Glosten & Milgrom (1985) Calculating Bid-Ask Spread

• Sell order $P(\overline{v}|sell) =$

$$= \frac{(1-\alpha)(1-\mu)\theta}{(1-\alpha)(1-\mu)\theta + [\alpha + (1-\alpha)(1-\mu)](1-\theta)}$$

$$P\left(\overline{\nu}|\mathsf{buy}\right) > P\left(\overline{\nu}\right) > P\left(\overline{\nu}|\mathsf{sell}\right)$$

$$P\left(\underline{\nu}|\mathsf{buy}\right) < P\left(\underline{\nu}\right) < P\left(\underline{\nu}|\mathsf{sell}\right)$$

 Market Maker makes zero expected profit (potential Bertrand competition)

$$b = bid = E[v|sell] = \overline{v}P(\overline{v}|sell) + \underline{v}P(\underline{v}|sell)$$

$$a = ask = E[v|buy] = \overline{v}P(\overline{v}|buy) + \underline{v}P(\underline{v}|buy)$$

Dynam

Sequential Trade Herding

Remarks to Glosten & Milgrom (1985)

- quotes are regret free
- **3** $(a-b) \rightarrow \text{gain from liquidity traders} = \text{loss to insider}$
- **4** bid-ask spread (a b) increases with α
- **6** over time price converge to true value
- 6 prices follow a martingale $E_t \left[p_{t+1} | I_t^l \right] = p_t$ (changes in prices are uncorrelated)
- Simple setting price at t depends only on # buy orders # sell orders (sequence of trades does not matter)
- **13** mid point of bid ask spread $\frac{a+b}{2}$ is <u>not</u> current market maker's expectation.

Sequential Trade

Extensions

- Easley and O'Hara (1987)
 - 'small and large' order size
 - noise traders submit randomly a small or a large sized order
 - informed traders always prefer large order size (if bid and ask is the same for both order sizes)
 - m.m. will set larger spread for large orders
 - Separating equilibrium
 - Informed traders' order size is 2
 - Uninformed traders' order size is 1 and 2 (exogenously given)
 - \Rightarrow Spread for small orders = 0
 - Pooling equilibrium
 - Informed traders' order size is 1 and 2
 - Uninformed traders' order size is 1 and 2 exogenously given)
 - ⇒ Larger spread for larger orders

of Models

Static Uniform Price Discr. Price

Discr. Price (Limit Order Book) Contrast

Dynam

Sequential Trade Herding 1987-crash

- "event uncertainty" (also in Easley & O'Hara (1992))
 - ullet with prob γ info is like in Glosten & Milgrom
 - with prob $(1-\gamma)$ no news event occurs (nobody receives a signal)
- No-Trade \rightarrow signals that nothing has occurred! \Rightarrow quotes will pull towards $\frac{1}{2}$ updating
 - whether event has occurred AND
 - 2 about true value of the stock
- transaction price is still a Martingale but no longer Markov!

Statio

Uniform Price Discr. Price (Limit Order Book) Contrast

Dynam

Sequential Trade

Herding 1987-crash

Herding - Avery & Zemsky (1998)

- Relates Glosten-Milgrom model to herding models (BHW 1992)
- Price adjustment eliminates herding and informational cascades if market maker learns at the same speed as other informed traders.
- Herding can still arise in a more general setting with event uncertainty and a more complicated information structure which guarantees that the market maker learns at a slower speed compared to other traders.

Classification of Models

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Uniform Price Discr. Price (Limit Order Book)

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Sequential Trade Herding 1987-crash

1987-Crash Jacklin, Kleiden & Pfleiderer (1992)

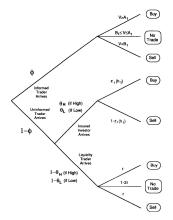


Figure: Underestimating portfolio insurance traders θ .