Turbo-MMC: Minimizing the Submodule Capacitor Size in Modular Multilevel Converters with a Matrix Charge Balancer

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Abstract—This paper presents a Turbo-MMC architecture with a Matrix Charge Balancer (MCB) to minimize the size of the submodule capacitors in modular multilevel converter (MMC) based medium voltage motor drives. The MCB manages the energy in all the submodule capacitors of a standard MMC. It balances the low frequency pulsating power among many MMC submodules and can significantly reduce the submodule capacitor size as well as the voltage ripple. We introduced the operation principles of the Turbo-MMC, and systematically investigated the tradeoffs between the capacitor size reduction and the power conversion stress of the MCB. A distributed phase-shift control strategy was adopted to compress the voltage ripple of the submodule capacitors while maintaining high performance for the MMC. Theoretical analysis and detailed design guidelines for the Turbo-MMC architecture are presented. A scaled-down MMC prototype and a 12-Port MCB have been built and tested to verify the effectiveness of the Turbo-MMC concept.

Index Terms—multilevel modular converter, multiport power converter, power decoupling.

I. INTRODUCTION

Modular multilevel converters (MMCs) offer low device voltage rating, high efficiency and excellent harmonic performance [1]. MMC-derived circuit topologies are applicable to a wide range of power conversion applications including high-voltage direct-current (HVDC) systems and medium voltage (MV) motor drives. The submodule capacitors in an MMC are designed to function as voltage sources and buffer the low frequency pulsating power. The peak to peak amplitude of the ripple power is proportional to the amplitude of the load current, and inversely proportional to the output fundamental frequency [2]. In MV variable speed MMC motor drives, the capacitors suffer the highest stress during start-up and low-speed operation. As shown in Fig. 1, the phase current of a motor drive during start-up is much higher than the nominal operation current of the system [3]. The submodule capacitors have to be sized for the highest current and lowest speed to maintain high power factor, low distortion and safety operation. The submodule capacitors usually contribute more than 50% of system volume and weight.

The low frequency components of pulsating power can be removed by injecting high frequency common mode voltage and circulating current to the phase arms of the MMC [2], [4]. In this way only high frequency pulsating power remains so that the voltage variation of submodule capacitors decreases. However, this method limits the modulation ratio of ac voltage and increases current stress for switches and arm inductors.

Existing methods for compensating the power fluctuation in submodule capacitors can be classified into active energy buffers or active energy balance links. In [5], a boost-type active buffer is included in each submodule. The pulsating power in each submodule capacitor is buffered by an active capacitor with large voltage ripple and small capacitance. This method requires a significant number of magnetic components (inductors) and has a theoretical limit in capacitor size reduction. A switched-capacitor-based active energy buffer can eliminate the magnets as needed in each submodule [6]. The voltage ripple also can be reduced by balancing energy between two submodule capacitors through a dual half-bridge (DHB) converters [7], [8] or among three submodule capacitors through a tri-port half-bridge converter [9], leveraging the naturally balanced pulsating power across submodules and phases. The required magnetic components are also fewer than the standalone active energy buffer.

This paper proposes a Matrix Charge Balancer which links all the submodule capacitors together to compensate the pulsating power and significantly reduce the submodule capacitor size with a “Turbo” operation. Fig. 2 shows the principles of the Turbo-MMC in which all MMC submodule capacitors are connected to a half-bridge unit of the matrix charge balancer which can process the low frequency pulsating power. All the half-bridge units are interconnected by a multiwinding transformer. The MCB only operates with the system for a short period of time during the start-up and heavy load operation of the MMC. It is deactivated during light load situation, which is similar to a turbo engine. A distributed phase-shift (DPS) controller regulates the capacitor voltage of each submodule by changing the phase shift of each half-bridge port. Time domain multiplexing can be applied to
control the power flow. The Turbo-MMC architecture is highly modular and can be implemented in MMC systems with a large number of series stacked submodules.

The remainder of this paper is organized as follows: Section II reviews the principles of pulsating power and voltage ripple in MMCs. Section III presents the principles of the Matrix Charge Balancer together with the MMC systems. Section IV presents the simulation results of the Turbo-MMC. Experimental results of a prototype Turbo-MMC is summarized in Section V. Finally, Section VI concludes the paper.

II. PULSATING POWER AND VOLTAGE RIPPLE IN MMCs

The 3φ MMC topology in Fig. 2 has two arm inductors \( L_{arm} \) and \( 2N \) submodules in each phase arm. The high frequency current and voltage ripples are neglected and switching cycle average is applied to simplify the following analysis. The arm current of Phase \( A, B, C \) with balanced load is:

\[
\begin{align*}
i_{ux} &= \frac{I_{dc}}{3} + i_{zx}, \quad i_{lx} = \frac{I_{dc}}{3} + i_{zx}
\end{align*}
\]

Here \( i_{ux} \) and \( i_{lx} \) are the upper arm current and lower arm's current respectively. \( I_{dc} \) is the dc input current, \( i_{zx} \) is the ac circulating current and \( i_{ox} \) is the ac output current of the specific phase. With Phase-Shift Carriers SPWM control [1], the input voltage of submodules \( v_{ux} \) and \( v_{lx} \) are:

\[
\begin{align*}
v_{ux} &= \frac{1}{2N} \left( \frac{V_{dc}}{2} - v_{ox} \right), \quad v_{lx} = \frac{1}{2N} \left( \frac{V_{dc}}{2} + v_{ox} \right)
\end{align*}
\]

The ac circulating current is calculated by solving:

\[
\frac{di_{zx}}{dt} = \frac{V_{dc}}{2L_{arm}} - \frac{R_{arm}I_{dc}}{3L_{arm}} - \frac{N(v_{ux} + v_{lx})}{2L_{arm}} - \frac{R_{arm}i_{zx}}{L_{arm}}.
\]

Here \( V_{dc} \) is the dc input voltage and \( v_{ox} \) is the phase voltage, \( R_{arm} \) is the equivalent resistance of phase arm. Obviously the ac circulating current is caused by the fluctuation of the submodule voltage. The submodule power of upper arm and lower arms are:

\[
p_{ux} = v_{ux}i_{ux}, \quad p_{lx} = v_{lx}i_{lx}.
\]

Substituting (1) and (2) into (4) yields:

\[
p_{ux}(t) = \frac{V_o I_o}{2N} \left( \frac{2}{M} \sin(2\pi ft - \varphi) - M \cos \varphi \sin 2\pi ft + \cos(4\pi ft - \varphi) \right) + \frac{\sqrt{2}V_{ox} i_{za}}{N} \left( \frac{1}{M} - \sin(2\pi ft - \varphi) \right),
\]

\[
p_{lx}(t) = \frac{V_o I_o}{2N} \left( M \cos \varphi \sin 2\pi ft - \frac{2}{M} \sin(2\pi ft - \varphi) \right) + \cos(4\pi ft - \varphi) + \frac{\sqrt{2}V_{ox} i_{za}}{N} \left( \frac{1}{M} + \sin(2\pi ft - \varphi) \right),
\]

Here \( I_o \) and \( V_o \) are the RMS values of the output current and phase voltage, \( f \) is the fundamental frequency, \( M \) is the voltage amplitude modulation ratio, and \( \varphi \) is the power factor angle. The pulsating power results in voltage ripple on submodule capacitors. For a given submodule capacitance \( C_{sm} \), the peak-to-peak voltage ripple is:

\[
\Delta V_{pp} = \frac{N}{2C_{sm} V_{dc}} \int_{0}^{\frac{T}{2}} |p_{gx}(t)| \, dt.
\]

The energy buffered by one submodule capacitor in a fundamental output current cycle is:

\[
E_{gx} = \frac{1}{2} \int_{0}^{\frac{T}{2}} |p_{gx}(t)| \, dt.
\]
The purpose of adding a matrix charge balancer to the MMC system is to balance the pulsating power among many submodules, leveraging the fact that the pulsating power in the upper arms and lower arms of the three phases are naturally interleaved. The matrix charge balancer only operate at low frequency and during the startup to significantly reduce the design constraints for the submodule capacitors in a MMC without sacrificing the system efficiency in normal operation.

III. PRINCIPLES OF THE MATRIX CHARGE BALANCER

Fig. 5 illustrates the key operation principles of the Turbo-MMC architecture with a multiport-ac-coupled matrix charge balancer. The Turbo balancer interface with all capacitors, and can freely transfer the pulsating power among multiple capacitors. The Turbo-MMC offers three ways of balancing the pulsating power: 1) balance power vertically among submodules within one phase (red); 2) balance power horizontally among three phases (blue); and 3) balance power as a matrix across submodules and phases (green). The residual pulsating power of the three balancing modes are defined as the average power processed by all involved submodules:

\[
p_v = \frac{p_{ua} + p_{tc}}{2} = \frac{V_o I_o}{2N} \cos(4\pi ft - \phi) + \frac{\sqrt{2}V_o i_{za}}{NM},
\]

\[
p_{h1} = \sum_{x=a,b,c} \frac{p_{ux}}{3} = \frac{\sqrt{2}V_o}{3N} \left( \frac{3}{2} i_{za} + \frac{3}{2} i_{zb} + \frac{3}{2} i_{zc} \right) - \frac{i_{za} - \frac{i_{zb}}{2} - \frac{i_{zc}}{2}}{2} \sin(2\pi ft - \phi) + \frac{i_{za} + i_{zb} + i_{zc}}{M}.
\]

\[
p_{h2} = \sum_{x=a,b,c} \frac{p_{tx}}{3} = \frac{\sqrt{2}V_o}{3N} \left( \frac{3}{2} i_{za} + \frac{3}{2} i_{zb} + \frac{3}{2} i_{zc} \right) + \frac{i_{za} - \frac{i_{zb}}{2} - \frac{i_{zc}}{2}}{2} \sin(2\pi ft - \phi) + \frac{i_{za} + i_{zb} + i_{zc}}{M}.
\]

\[
p_m = \sum_{x=a,b,c} \frac{p_{ux}}{6} + \sum_{x=a,b,c} \frac{p_{tx}}{6} = \frac{\sqrt{2}V_o}{3N} \left( i_{za} + i_{zb} + i_{zc} \right).
\]  

(9)

If only vertical balancing strategy is used (energy is transferred from upper arms to lower arms), the residual pulsating power of vertical balancing \(p_v\) contains both double-fundamental frequency power fluctuation and ac circulating current. If horizontal balancing is used, the double-fundamental frequency power fluctuation caused by the ac

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**TABLE I**

**Circuit Parameters of an Example Turbo-MMC Motor Drive with the Matrix Charge Balancer.**

<table>
<thead>
<tr>
<th>(V_{dc})</th>
<th>(P_o)</th>
<th>(M)</th>
<th>(N)</th>
<th>(f_{mmc})</th>
<th>(f_{mab})</th>
</tr>
</thead>
<tbody>
<tr>
<td>700 V</td>
<td>6 kW</td>
<td>0.89</td>
<td>2</td>
<td>10 kHz</td>
<td>100 kHz</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>(L_o)</th>
<th>(C_{sm})</th>
<th>(L_{arm})</th>
<th>(R_{arm})</th>
<th>(L_b)</th>
<th>(C_b)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 mH</td>
<td>1 mF</td>
<td>4 mH</td>
<td>50 mΩ</td>
<td>5 μH</td>
<td>0.1 mF</td>
</tr>
</tbody>
</table>

Here \(y\) represents the position of phase arm (\(U\): upper arm; \(L\): lower arm). Fig. 3 illustrates the calculated voltage ripple and pulsating power of one submodule is calculated and plotted in Fig. 4. The system is controlled with SPWM without capacitor charge balancing. The frequency of ac circulating current is twice of the fundamental frequency. In this specific case, the peak instantaneous power in each submodule (ac with circulating current) is 125% of the output power of one phase. The total energy buffered in all submodule capacitors is 88% of the overall output energy in this case. If the ac circulating current is zero, 50% of energy needs to be buffered. The ac circulating current in each phase increases the power stress of submodule switches and passive components. It can be reduced by larger submodule capacitors, larger arm inductors and closed-loop control [10].
output is eliminated. Matrix balancing is a combination of vertical balancing and horizontal balancing, and can fully eliminate the double-fundamental frequency power fluctuation. The ac circulating current can also be reduced by balancing the pulsating power among many submodules.

Fig. 6 compares the remaining pulsating power of one submodule capacitor in an example MMC with 1) vertical power balancing; 2) horizontal power balancing; and 3) matrix power balancing. Matrix power balancing can significantly reduce the peak residual pulsating power. The percentage of energy buffered are calculated based on Eq. (8) and compared in Fig. 7. In the example MMC without pulsating power balancing, over 88% of the energy the MMC processed needs to be buffered by the submodule capacitors. In the example MMC with vertical power balancing, this percentage is reduced to 75%. In the example MMC with horizontal power balancing, the percentage of the energy that needs to be buffered is 19.6%. In the example MMC with matrix power balancing, the percentage of the energy that needs to be buffered is less than 1%. Matrix power balancing can almost completely eliminate the pulsating power in the submodule capacitors at the cost of increased power processing stress in the charge balancer. The more energy processed by the matrix charge balancer, the more capacitor size reduction can be achieved.

The smaller submodule capacitor voltage ripple further reduces the ac circulating current in each arm. Balancing the pulsating power not only reduces the submodule capacitor size but also allows smaller arm inductors. However, completely eliminating the submodule capacitor or pursuing zero voltage ripple pushes the power conversion stress to the matrix charge balancer and reduces the system efficiency. The best way to design a Turbo-MMC architecture is to activate the MCB only if needed (i.e., similar to a Turbocharge engine, only operate the matrix charge balancer during the startup when the pulsating power is high), and size the capacitors based on the normal operation to reduce the system volume. Use a MMC with parameters listed in Table I as an example, we investigate the tradeoff between the voltage ripple reduction (which is equivalent to the capacitor size reduction) and the power conversion stress in the Turbo operation with theoretical derivation, SPICE simulations and experiments.

IV. MATRIX CHARGE BALANCER

A. Topology and Operation Principles

The matrix charge balancer can be implemented as a multi-active-bridge (MAB) converter as shown in Fig. 8. The MAB converter has many dc-ac inverter units and a multi-winding transformer. By controlling the phase shift of the dc-ac converters, and applying time-domain multiplexing in the dc-ac converters, the matrix charge balancer can route energy from one port to another port, and from multiple input ports to multiple output ports. Other isolated multi-input-multi-output (MIMO) topologies, such as multi-winding flyback and multiport series resonant converter, are also applicable. Implementing the MCB as a MAB converter offers many advantages including high efficiency, high power density, and small magnetic component size. There is only one “dc-ac-dc” power conversion process between two arbitrary ports.
B. Power Flow Control Method

The MAB converter delivers power among many submodule capacitors for matrix power balancing. The goal of control the power flow in the MAB converter is to regulate the submodule capacitor voltages. As shown in Fig. 9, the MAB converter with single magnetic core can be modeled as a cantilever model [11] driven by multiple square wave voltage sources. All windings have identical number of turns $N_w$. In a symmetric multi-winding transformer, the equivalent branch inductance $L_{ij}$ between Port #i and Port #j is [12]:

$$L_{ij} = \frac{6N \cdot L_b}{N_w^2}. \quad (10)$$

Here $L_b$ is the link inductance of each branch. $6N$ is the total number of submodules for a N-level 3φ MMC. The average power feed into the multiwinding transformer from Port #i in one switching cycle is:

$$P_i = \frac{V_i}{2\pi f_mab N_w} \sum_{j \neq i} \frac{V_j}{L_{ij}} (\Phi_j - \Phi_i) \left(1 - \frac{|\Phi_j - \Phi_i|}{\pi}\right). \quad (11)$$

$V_i, V_j$ are the dc voltage of Port #i and Port #j, which is one half of the submodule capacitor voltage $0.5V_{dc}/N$. $\Phi_i, \Phi_j$ are the phase-shift angles of Port #i and Port #j.

A distributed phase-shift (DPS) controller (as shown in Fig. 11) is designed to control the power flow and regulate the voltage of each submodule capacitor. The DPS block comprises functional blocks such as voltage sensing, error calculation, PI controller and phase-delay module. A global synchronize clock is needed by the DPS block as the absolute phase-shift reference. This DPS controller implementation is highly modular and is applicable to large-scale MMC systems with a large number of submodules.

A hysteresis voltage control strategy is implemented in each DPS controller (Fig. 10). The DPS sets an upper threshold $\Delta V_{pp}/2$, a lower threshold $-\Delta V_{pp}/2$ and a hysteresis $\Delta V_h$ for the capacitor voltage, if a capacitor voltage reaches the upper threshold, the MAB converter moves energy away from this capacitor until the voltage ripple drops below $\Delta V_{pp}/2 - \Delta V_h$; if a capacitor voltage reaches the lower threshold, the MAB converter moves energy into this capacitor until the voltage ripple goes above $-\Delta V_{pp}/2 + \Delta V_h$. The matrix power balancing requires exchanging power among all the submodules so that a global enable signal is used to wake up all the half-bridge ports of the MAB converter when any submodule voltage triggers the ripple threshold. Other power flow control strategies, such as ranking the voltage level of all the submodule capacitors and only operate a portion of the ports during a part of the fundamental frequency cycle, are also applicable and are beyond the scope of this paper. Other power flow control methods for MAB converters, such as the Newton-Raphson method based methods as presented in [12], and the time-domain multiplexing method as presented in [13], are also attractive options and are beyond the scope of this paper.
C. Turbo Operation and Voltage Ripple Reduction

The pulsating power buffered by the submodule capacitors can almost be completely eliminated by the matrix power balancing, which reduces the device stresses and improves the power quality. On the other hand, processing the pulsating power induces additional loss. For a given submodule design with capacitance $C_{sm}$, the peak to peak voltage ripple amplitude on the capacitor is a function of the energy buffered by the submodule in Phase $x$ Arm $y$ ($E_{yx}$):

$$
\Delta V_{pp} = \frac{N}{C_{sm} V_{dc}} E_{yx}.
$$

V. SPICE SIMULATIONS

Fig. 12 shows a SPICE simulation platform for the Turbo-MMC built in PLECS. Each upper arm and lower arm has two submodules. The carrier frequency of the MMC is 10 kHz and switching frequency of the Turbo balancer is 100 kHz. Other parameters of the MMC system are listed in Table I. Fig. 18 shows the simulation waveforms of voltage ripple on submodule capacitors with different peak to peak ripple threshold. The peak to peak voltage ripple of the submodule capacitors without matrix charge balancing (Turbo mode OFF) is 25 V with a DC offset of 350 V (Fig. 18a). Fig. 18b and Fig. 18c show the voltage ripple of the submodule capacitors under Turbo operation. In Fig. 18b, the Turbo operation reduces the peak to peak amplitude of voltage ripple to 12.5 V. In Fig. 18c, the Turbo balancer processes all pulsating power aiming to compress the voltage ripple to zero. The peak to peak voltage ripple is below 1 V (350 V dc offset).

If the MAB converter is controlled in a way to reduce the voltage ripple by $K\%$, the energy that needs to be processed by the MAB converter is $K\%$ of the energy which is processed by this specific submodule. Fig. 13 shows the energy processed by this submodule in Phase $x$ Arm $y$. SPICE simulation results verified the theoretical analysis.
The parameters of the prototype are listed in Table II. The converter with 4 modules in each phase and a 12 Port capacit. The prototype includes a low power three-phase MMC tested to verify the matrix pulsating power balancing con-
and the capacitor voltage ripple almost reduces to zero.

1) From 0 to 0.3, the system starts with low frequency (10 Hz) and delivers 1200 W to the load. When starting the motor, low frequency operation causes high fluctuation on the submodule capacitor voltage. The MAB converter is activated to perform Turbo operation from 0 to 0.3; 2) The Turbo operation is turned OFF while the ac fundamental frequency remains 10 Hz from 0.3 to 0.6. The capacitor voltage ripple significantly increases; 3) From 0.6 to 0.9, the system frequency steps up to 50 Hz and the capacitor voltage ripple reduces; 4) From 0.9 to 1.2, the system output power steps up to full load (6000 W) and the capacitor voltage ripple increases; 5) From 1.2 to 1.5, the Turbo mode is turned ON, and the capacitor voltage ripple almost reduces to zero.

VI. EXPERIMENTAL VERIFICATION
A scaled down Turbo-MMC prototype has been built and tested to verify the matrix pulsating power balancing concept. The prototype includes a low power three-phase MMC converter with 4 modules in each phase and a 12 Port ac-coupled dc-dc converter as the Matrix Charge Balancer. The parameters of the prototype are listed in Table II. The submodule circuits of the MMC converter and the half-bridge ports of MAC converter are implemented with the same half-bridge module. Fig. 17 shows a picture of the prototype. The switching frequency of the MMC is 50 kHz, and the switching frequency of the MAC converter is 200 kHz. Fig. 18 shows the operation waveforms of the prototype with and without Turbo operation. With Turbo operation, the capacitator voltage ripple is very small. Without the Turbo operation, the voltage ripple increases by almost 8 times. The high voltage ripple also saturated the arm inductors with very high current spikes.

VII. CONCLUSIONS
This paper presents a Turbo-MMC architecture to reduce the submodule capacitor size in MMC motor drives. We analyzed the pulsating power and the voltage ripple in MMC submodule capacitors and developed a matrix charge balancer to process the pulsating power. The matrix charge balancer can eliminate the pulsating power in the submodule capacitors and significantly reduce the capacitor size. The Turbo mode should be turned on when the capacitor pulsating power is high (e.g., during system startup, low speed, and heavy load operation) and kept off in nominal operation to maintain high efficiency. The effectiveness of the Turbo-MMC concept is verified by SPICE simulations and experimental results.

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REFERENCES
Simulated capacitor voltage ripple ($v_{cua}, v_{cla}$) of the Turbo-MMC in five operating modes: (1) 0.0s – 0.3s, low frequency (10 Hz) startup with Turbo mode ON, 20% load (1200 W); (2) 0.3s – 0.6s, light load operation with Turbo mode OFF; (3) 0.6s – 0.9s, output frequency increased to 50Hz with Turbo mode OFF; (4) 0.9s – 1.2s, output load steps up to 100% (6000 W); (5) 1.2s – 1.5s, high frequency heavy load operation with Turbo mode ON.

![Fig. 16. Simulated capacitor voltage ripple (v_{cua}, v_{cla}) of the Turbo-MMC in five operating modes: (1) 0.0s – 0.3s, low frequency (10 Hz) startup with Turbo mode ON, 20% load (1200 W); (2) 0.3s – 0.6s, light load operation with Turbo mode OFF; (3) 0.6s – 0.9s, output frequency increased to 50Hz with Turbo mode OFF; (4) 0.9s – 1.2s, output load steps up to 100% (6000 W); (5) 1.2s – 1.5s, high frequency heavy load operation with Turbo mode ON.](image)

Fig. 17. Picture of the prototype Turbo-MMC with 12 submodules and a 12-port MAB converter.

![Fig. 17. Picture of the prototype Turbo-MMC with 12 submodules and a 12-port MAB converter.](image)

Fig. 18. Measured waveforms of the prototype Turbo-MMC with Output fundamental frequency of 50 Hz. High voltage ripple even causes arm inductor saturation without Turbo operation.

![Fig. 18. Measured waveforms of the prototype Turbo-MMC with Output fundamental frequency of 50 Hz. High voltage ripple even causes arm inductor saturation without Turbo operation.](image)
