

# Depairing field, onset temperature and the nature of the transition in cuprates

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## Abstract

The depairing (upper critical) field  $H_{c2}$  in hole-doped cuprates has been inferred from magnetization curves  $M$ - $H$  measured by torque magnetometry in fields  $H$  up to 45 T. We discuss the implications of the results for the pair binding energy, onset temperature, fluctuation diamagnetism and the nature of the Meissner transition at  $T_c$ .

*Key words:* Magnetization, Upper Critical Field, Vortex Liquid, Cuprates

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In hole-doped cuprates, the depairing field at which the pair condensate is destroyed (or “upper critical field”  $H_{c2}$ ) has been notoriously difficult to measure. Recently, progress has been achieved using the vortex-Nernst effect [1–3] and high-field torque magnetometry [4,5].

High-field measurements of  $M$  are technically difficult because the large Ginzburg-Landau parameter, small crystal volumes (0.1-0.3 mm<sup>3</sup>) and high field scales of  $H_{c2}$  (50-200 T) all result in a very small sample moment. Fortunately, torque magnetometry is well-suited for this purpose [6]. The crystal is glued to the end of a soft cantilever with its axis  $\mathbf{c}$  at a small angle to  $\mathbf{H}$ . The observed magnetization  $M_{eff} = \Delta\chi H_z + M(T, H_z)$ , where  $M(T, H_z) < 0$  is the magnetization produced by supercurrents ( $\hat{\mathbf{z}} \parallel \mathbf{c}$  and  $T$  is the temperature). The dominant contribution to the paramagnetic background  $\Delta\chi$  comes from the strongly anisotropic orbital (van Vleck) term  $\chi_i^{orb}$ . Its weak  $T$ -linear behavior allows the diamagnetic term  $M$  to be extracted with high resolution [5]. Here we discuss some of our torque measurements

on  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  (LSCO),  $\text{Bi}_2\text{Sr}_{2-y}\text{La}_y\text{CuO}_6$  (Bi 2201) and  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$  (Bi 2212) from the underdoped (UD) to overdoped (OD) regimes.

Figure 1 shows the  $M$ - $H$  curves in optimally-doped (OP) Bi 2212 ( $T_c \sim 86.5$  K) at temperatures 35 to 90 K (left panel), and from 80 to 110 K (right panel). The curves are all fully reversible (pinning effects appear only below 35 K at low fields  $< 1$  T). At the lowest  $T$ , the curve of  $M$  vs.  $H$  is very similar to that in a low- $T_c$  type II superconductor. Above  $H_{c1}$ ,  $|M|$  decreases as  $\log H$  over a very broad field range. A notable feature is the very high  $H_{c2}$ , which we estimate to be 150-200 T by extrapolation. (These values are much larger than inferred from measurements of the resistivity  $\rho$  vs.  $H$ . The “knee” feature in  $\rho$  usually used to fix “ $H_{c2}$ ” actually occurs just above the vortex-solid melting field  $H_m \ll H_{c2}$ .)

As  $T$  nears  $T_c$ , a major difference from BCS superconductors emerges. There,  $H_{c2}(T)$  decreases to zero linearly, viz.  $H_{c2}(T) \sim t$  with  $t = 1 - T/T_c$ . Accordingly, the high-field limit of  $M$  in Fig. 1b should decrease and reach zero at  $T_c$ . Instead, we find that

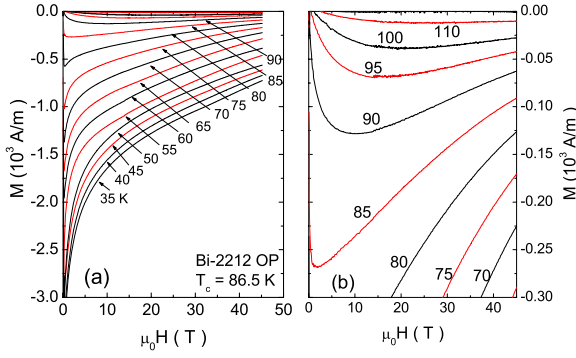


Fig. 1. Magnetization curves  $M$  vs.  $H$  in OP Bi 2212 at  $T = 35$ -90 K (Panel a) and at  $T = 75$ -110 K (b). At low  $T$ ,  $|M| \sim \log H$  initially, but goes to zero at  $H_{c2} = 150$ -200 T. Notably,  $H_{c2}(T)$  shows no tendency towards zero as  $T \rightarrow T_c^-$ . Above  $T_c$  (86.5 K),  $|M|$  remains quite large in fields up to and above 45 T.

it remains high above our maximum field (45 T), even when  $T$  exceeds  $T_c$  (right panel). The diamagnetic signal remains quite large at 45 T up to 110 K.

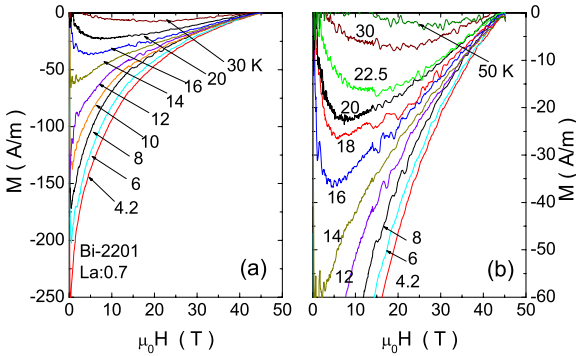


Fig. 2. Magnetization curves  $M$  vs.  $H$  in UD Bi 2201 shown for  $T = 4.2$ -30 K (Panel a), and in expanded scale (Panel b). At each  $T$ , the field at which  $|M| \rightarrow 0$  is taken to be  $H_{c2}(T)$ . The convergence of all curves implies that  $H_{c2}(T)$  is independent of  $T$  to our resolution. Above  $T_c \sim 14$  K,  $M$  remains sizeable and strongly  $H$  dependent.

This key feature – seen in all the hole-doped cuprates studied – is most apparent in single-layer UD Bi 2201, where complete suppression of diamagnetism is attainable below 45 T. Figure 2 shows the  $M$ - $H$  curves in a crystal with  $T_c \sim 14$  K. Hysteretic behavior is not observed down to 4 K. In comparison with OP Bi 2212, the magnitude  $|M|$  in weak  $H$  and low  $T$  is quite a bit smaller (250 A/m compared with 4000 A/m), but it displays the same  $\log H$  de-

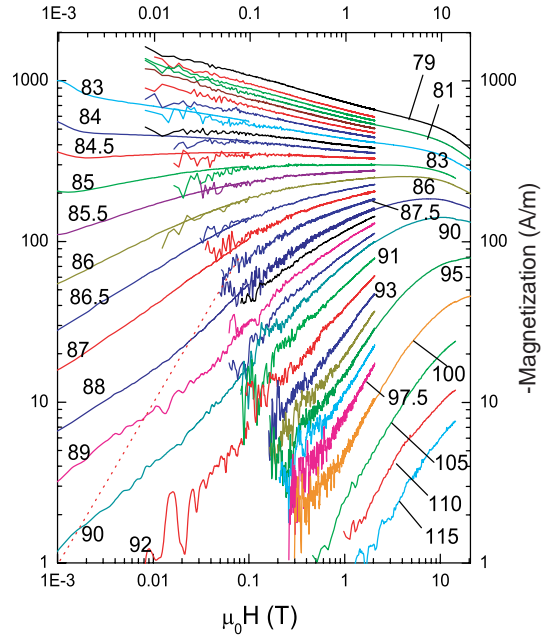


Fig. 3. The field dependence of  $M(T, H)$  in OP Bi 2212 from  $H = 10$  Oe to 20 T at  $T = 79$ -115 K. The log-log plot shows that, as  $H \rightarrow 0$ ,  $M(H)$  follows the fractional power-law  $M \sim H^{1/\delta}$ . The plot combines SQUID results (10 to 1000 Oe) and torque magnetometry results (500 Oe to 2 T). Torque results up to 20 T are also shown at selected  $T$ . Linear response  $M \sim H$  at 87 K would appear as the dashed line (from Ref. [4]).

pendence in  $H < 20$  T. At high fields,  $M$  approaches zero at the field  $H_{c2}(0) \sim 43$  T. In Panel b, we show that  $H_{c2}(T)$  remains nominally  $T$ -independent even above  $T_c$ . In the interval around  $T_c$ , the  $M$ - $H$  curves display the same pattern as shown for OP Bi 2212. Significant diamagnetism remains at  $T$  up to 30 K.

The diamagnetic signal  $M$  above  $T_c$  is robust to fields of 45 T and considerably larger in magnitude than “fluctuating diamagnetism” in low- $T_c$  superconductors [9]. We discuss why the fluctuations are distinctly non-Gaussian. In BCS superconductors, a key feature is the linear decrease to zero of the  $T$ -dependent critical field  $H_{c2}(T)$  as  $T \rightarrow T_c^-$ . This feature dictates the behavior of fluctuations above  $T_c$  in Gaussian GL treatments. In particular,  $t$  enters in  $M(t, h)$  as the ratio  $|t|/h$ . Consequently, above  $T_c$ , the field dependence of  $M$  is dictated by the field scale  $H_{c2}(0)t$ , which is the “mirror image” of  $H_{c2}(T)$ , vanishing linearly in  $|t|$  as  $T \rightarrow T_c$  from above. Accordingly,  $M$  measured in low- $T_c$  superconductors are nicely scaled when plotted in terms of the “Prange” variable  $x = [\frac{dH_{c2}}{dT}]_c (T - T_c) / H \sim 1.4|t|/h$  [9].

As noted above,  $H_{c2}(T)$  does not vanish linearly

in  $|t|$  in hole-doped cuprates [3–5]. This invalidates the Gaussian approach which depends on series expansion in terms of the order parameter and its derivative. Above  $T_c$ , the  $M$ - $H$  curves in Bi 2212 are also qualitatively different from low- $T_c$  superconductors. Instead of linear response, the  $M$ - $H$  curves are strongly nonlinear even in low  $H$ . Figure 3 shows in log-log scale the variation of  $M$  over a broad range of  $H$  (10 G to 30 T) at  $T = 79$ -115 K. As emphasized in Fig. 4a, the  $M$ - $H$  curves display strong curvature at temperatures near  $T_c = 87$  K. In weak  $H$ ,  $M(H)$  fits well to the power law

$$|M| \sim H^{1/\delta}, \quad (1)$$

with a strongly  $T$  dependent exponent  $\delta(T)$ . Between  $T_c$  and 105 K,  $\delta(T)$  decreases from  $\sim 10$  to 1 (Fig. 4b). The vanishing of  $\delta(T)$  defines the temperature  $T_s$  slightly below  $T_c$  at which  $M$  is *independent* of  $H$  up to a few T (this feature – dubbed the separatrix [4] – has been known for a long time).

These anomalous magnetization patterns are incompatible with Gaussian fluctuations, but consistent with the phase-disordering scenario [7] in which, above  $T_c$ , the condensate amplitude is large, but phase rigidity and long-range phase coherence are lost. Near  $T_c$ , the  $M$ - $H$  curves are strikingly similar to those calculated for a 2D superconductor near its Kosterlitz Thouless (KT) transition [8]. As discussed later, the appropriate comparison is with the 3DXY model with very large anisotropy.

The  $M$ - $H$  curves in Figs. 1-3 together imply the following physical picture (see Ref. [4]). On cooling from 300 K, the system first crosses the pseudogap temperature  $T^*$ . The pseudogap affects primarily the spin degrees of freedom, especially the relaxation rate  $1/T_1T$  in NMR and the bulk susceptibility. Evidence for Cooper charge pairing appears only at  $T_{onset} = 0.5$ - $0.7 T^*$ . Below  $T_{onset}$  (the “Nernst” region), both the Nernst signal and diamagnetism increase steeply to merge smoothly with the corresponding signals below  $T_c$ . Within each  $\text{CuO}_2$  layer, the pair condensate is robust with a very large pair-binding energy. However, because of thermal generation of mobile 2D vortices, phase coherence is confined to a length scale given by the phase correlation length  $\xi_\phi$  [4]. The “hot 2D vortex liquid”, nonetheless, displays a fairly large diamagnetic response.

It is instructive to contrast cuprates from a percolative system (e.g. granular Al) in which superconducting islands are gradually phase coupled by the proximity effect as  $T$  decreases. In high-quality crystals of the cuprates, the zero-field transition is

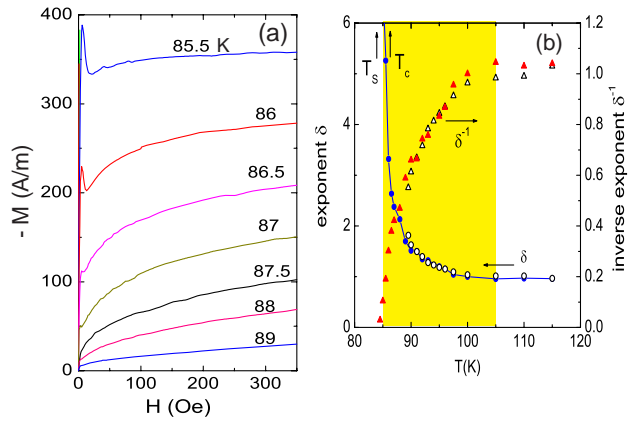


Fig. 4. (Panel a) The weak-field  $M$ - $H$  curves near  $T_c$  ( $= 87$  K) in OP Bi 2212. The power-law variation with fractional exponent is evident in all curves shown. Below  $T_c$ , full flux expulsion occurs for  $H < H_{c1}$  (visible as a spike). The curve at 85.5 K is very close to the separatrix temperature  $T_s$ . Panel (b) displays the  $T$  dependence of the exponent  $\delta(T)$  (circles) for 2 crystals of OP Bi 2212. The reciprocal  $\delta(T)^{-1}$  is plotted as solid and open triangles for the 2 samples. As  $T \rightarrow T_s^+$ ,  $\delta(T)^{-1}$  decreases smoothly to 0. In the shaded region where  $\delta > 1$  (from  $T_s$  to 105 K), linear magnetic response is absent even at 10 Oe (adapted from Ref. [4]).

invariably very sharp. At  $T_c$ , full flux expulsion appears [4]. The resistive transition is also abrupt, in contrast to the long tail seen in granular Al.

Two features seem to be crucial. The first is the pre-emption of the 2D KT transition in individual layers by the 3D transition caused by interlayer coupling, as occurs in layered magnets [10]. Below  $T_{onset} \sim 130$  K, the in-plane  $\xi_\phi$  (inferred from the susceptibility  $\chi = M/H$ ) grows as in the KT transition [4]. Below 105 K, however,  $M$  becomes increasingly non-linear (Fig. 4a). The increase in  $\delta(T)$  reflects rapid upward renormalization of the interlayer coupling strength. In the interval between  $T_c$  and 105 K, the fractional power-law implies that  $\chi$  can approach -1 in the limit  $H \rightarrow 0$ . However, this London rigidity is fragile and easily suppressed by field. At  $T_c$  ( $\sim 2$  K above  $T_s$ ), the Meissner state appears [4]. As apparent in Fig. 4a, full flux expulsion occurs below the lower critical field  $H_{c1}(T)$ , seen as sharp spikes in Fig. 4a. Significantly, the 3D Meissner state is observed at fields  $H < H_{c1}$ , yet at higher  $H$  ( $>$  a few T), the  $M$ - $H$  profiles revert to the 2D pattern seen high above  $T_c$ . This field-induced crossover from 3D to 2D behavior – with its intrinsic non-monotonicity – is very different from low- $T_c$  superconductors.

The second feature is the termination of the melt-

ing curve  $H_m(T)$  at  $T_c$ . Far from being accidental, we believe this is intrinsic to the nature of the transition. Within the vortex-solid state, spontaneously created vortices are ineffectual in destroying phase coherence because they are not able to diffuse. Hence,  $T_c$  cannot lie below the high- $T$  termination of  $H_m(T)$ . On the other hand,  $T_c$  cannot lie above the termination point. This would correspond to a strictly 2D transition that is incompatible with the observed full Meissner effect. These 2 features distinguish the cuprate transition from that in granular Al.

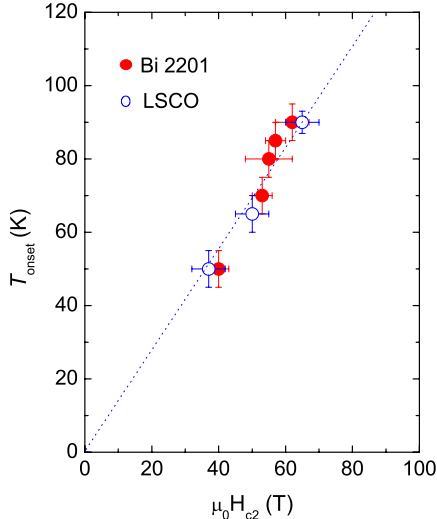


Fig. 5. Plot of  $T_{onset}$  vs.  $H_{c2}(0)$  in the single-layer cuprates Bi 2201 and LSCO. Both quantities are inferred from the  $M$  vs.  $H$  curves measured by high-field torque magnetometry. The broken line is Eq. 2 with  $g \simeq 2.1$ .

Lastly, we discuss an interesting relation between  $H_{c2}$  and  $T_{onset}$ . Measurements on several Bi 2201 and LSCO crystals from UD to OD regime reveal that  $H_{c2}(0)$  and  $T_{onset}$  (measured from both the Nernst signal and magnetization) scale together as shown in Fig. 5. Within the experimental uncertainties,  $T_{onset}$  is linear in  $H_{c2}(0)$ . Expressing  $H_{c2}(0)$  as a Zeeman energy, viz.

$$k_B T_{onset} = g \mu_B H_{c2}(0), \quad (2)$$

we find that the  $g$ -factor  $g \simeq 2.1$  ( $\mu_B$  is the Bohr magneton). The data in Fig. 5 are restricted to Bi 2201 and LSCO. As noted in Fig. 1,  $H_{c2}(0)$  in OP Bi 2212 is much larger given its  $T_{onset}$  ( $\sim 130$  K). Figure 5 ties together the energy scale implied by  $T_{onset}$

and the pair binding energy at low  $T$  for Bi 2201 and LSCO. The linear fit with  $g \sim 2.1$  suggests that the Pauli limit may be relevant to the high-field de-pairing process. The implication of this relationship is currently being explored.

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