# RobustBench: a standardized adversarial robustness benchmark

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#### Abstract

As a research community, we are still lacking a systematic understanding of the progress on adversarial robustness which often makes it hard to identify the most promising ideas in training robust models. A key challenge in benchmarking robustness is that its evaluation is often error-prone leading to robustness overestimation. Our goal is to establish a standardized benchmark of adversarial robustness, which as accurately as possible reflects the robustness of the considered models within a reasonable computational budget. To this end, we start by considering the image classification task and introduce restrictions (possibly loosened in the future) on the allowed models. We evaluate adversarial robustness with AutoAttack [28], an ensemble of white- and black-box attacks, which was recently shown in a large-scale study to improve almost all robustness evaluations compared to the original publications. To prevent overadaptation of new defenses to AutoAttack, we welcome external evaluations based on adaptive attacks [142], especially where AutoAttack flags a potential overestimation of robustness. Our leaderboard, hosted at https://robustbench.github.io/, contains evaluations of 120+ models and aims at reflecting the current state of the art in image classification on a set of well-defined tasks in  $\ell_{\infty}$ - and  $\ell_2$ -threat models and on common corruptions, with possible extensions in the future. Additionally, we open-source the library https://github.com/RobustBench/robustbench that provides unified access to 80+ robust models to facilitate their downstream applications. Finally, based on the collected models, we analyze the impact of robustness on the performance on distribution shifts, calibration, out-of-distribution detection, fairness, privacy leakage, smoothness, and transferability.

### 1 Introduction

Since the finding that state-of-the-art deep learning models are vulnerable to small input perturbations called *adversarial examples* [135], achieving adversarially robust models has become one of the most studied topics in the machine learning community. The main difficulty of robustness evaluation is that it is a computationally hard problem even for simple  $\ell_p$ -bounded perturbations [70] and exact approaches [138] do not scale to large enough models. There are already more than 3000 papers on this topic [16], but it is often unclear which defenses against adversarial examples indeed improve robustness and which only make the typically used attacks overestimate the actual robustness. There is an important line of work on recommendations for how to perform adaptive attacks that are selected specifically for a particular defense [5, 17, 142] which have in turn shown that several

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Rank	Method	Standard accuracy	AutoAttack robust accuracy	Best known robust accuracy	AA eval. potentially unreliable	Extra data	Architecture	🍦 Venue 🍦
1	Fixing Data Augmentatic Improve Adversarial Robu 66.56% robust accuracy is due to the evaluation (AutoAttack + MultiTarg	n to stness original 92.23%	66.58%	66.56%	×		WideResNet-70-16	arXiv, Mar 2021
2	Uncovering the Limits of Ad- Training against Norm-Bou Adversarial Examples 65.87% robust accuracy is due to the evaluation (AutoAttack + MuliTarg	rersarial Inded 91.10% original eted)	65.88%	65.87%	×		WideResNet-70-16	arXiv, Oct 2020
3	Fixing Data Augmentatic Improve Adversarial Robu It uses additional IM synthetic images I 64.58% robust accuracy is due to the evaluation (AutoAttack + MultiTarg	n to stness a training. 88.50% original eted)	64.64%	64.58%	×	×	WideResNet-106- 16	arXiv, Mar 2021

Figure 1: The top-3 entries of our CIFAR-10 leaderboard hosted at https://robustbench.github. io/ for the  $\ell_{\infty}$ -perturbations of radius  $\varepsilon_{\infty} = 8/255$ .

seemingly robust defenses fail to be robust. However, recently Tramèr et al. [142] observe that although several recently published defenses have tried to perform adaptive evaluations, many of them could still be broken by new adaptive attacks. We observe that there are repeating patterns in many of these defenses that prevent standard attacks from succeeding. This motivates us to impose restrictions on the defenses we consider in our proposed benchmark, RobustBench, which aims at standardized adversarial robustness evaluation. Specifically, we rule out (1) classifiers which have zero gradients with respect to the input [13, 53], (2) randomized classifiers [161, 100], and (3) classifiers that use an optimization loop at inference time [118, 84]. Often, non-certified defenses that violate these three restrictions only make gradient-based attacks harder but do not substantially improve robustness [17]. However, we will lift (some of) these constraints if a standardized reliable evaluation method for those defenses becomes available. We start from benchmarking robustness with respect to the  $\ell_{\infty}$ - and  $\ell_2$ -threat models, since they are the most studied settings in the literature. We use the recent AutoAttack [28] as our current standard evaluation which is an ensemble of diverse parameter-free attacks (white- and black-box) that has shown reliable performance over a large set of models that satisfy our restrictions. Moreover, we accept and encourage external evaluations, e.g. with adaptive attacks, to improve our standardized evaluation, especially for the leaderboard entries whose evaluation may be unreliable according to the *flag* that we propose. Additionally, we collect models robust against common image corruptions [58] as these represent another important type of perturbations which should not change the decision of a classifier.

**Contributions.** We make following key contributions with our RobustBench benchmark:

- Leaderboard (https://robustbench.github.io/): a website with the leaderboard (see Fig. 1) based on *more than 120* evaluations where it is possible to track the progress and the current state of the art in adversarial robustness based on a standardized evaluation using AutoAttack *complemented* by (external) adaptive evaluations. The goal is to clearly identify the most successful ideas in training robust models to accelerate the progress in the field.
- Model Zoo (https://github.com/RobustBench/robustbench): a collection of the most robust models that are easy to use for any downstream applications. As an example, we expect that this will foster the development of better adversarial attacks by making it easier to perform evaluations on a large set of *more than 80* models.
- **Analysis**: based on the collected models from the Model Zoo, we provide an analysis of how robustness affects the performance on distribution shifts, calibration, out-of-distribution detection, fairness, privacy leakage, smoothness, and transferability. In particular, we find that robust models are significantly *underconfident* that leads to worse calibration, and that not all robust models have higher privacy leakage than standard models.

#### 2 Background and related work

Adversarial perturbations. Let  $x \in \mathbb{R}^d$  be an input point and  $y \in \{1, \dots, C\}$  be its correct label. For a classifier  $f : \mathbb{R}^d \to \mathbb{R}^C$ , we define a *successful adversarial perturbation* with respect to the perturbation set  $\Delta \subseteq \mathbb{R}^d$  as a vector  $\boldsymbol{\delta} \in \mathbb{R}^d$  such that

$$\underset{c \in \{1,...,C\}}{\operatorname{arg\,max}} f(\boldsymbol{x} + \boldsymbol{\delta})_c \neq y \quad \text{and} \quad \boldsymbol{\delta} \in \Delta,$$
(1)

where typically the perturbation set  $\Delta$  is chosen such that *all* points in  $x + \delta$  have y as their true label. This motivates a typical robustness measure called *robust accuracy*, which is the fraction of datapoints on which the classifier f predicts the correct class for all possible perturbations from the set  $\Delta$ . Computing the exact robust accuracy is in general intractable and, when considering  $\ell_p$ -balls as  $\Delta$ , NP-hard even for single-layer neural networks [70, 149]. In practice, an *upper bound* on the robust accuracy is computed via some *adversarial attacks* which are mostly based on optimizing some differentiable loss (e.g., cross entropy) using local search algorithms like projected gradient descent (PGD) in order to find a successful adversarial perturbation. The tightness of the upper bound depends on the effectiveness of the attack: unsuitable techniques or suboptimal parameters (e.g., the step size and the number of iterations) can make the models appear more robust than they actually are [36, 95], especially in the presence of phenomena like gradient obfuscation [5]. Certified methods [151, 48] instead provide *lower bounds* on robust accuracy which often underestimate robustness significantly, especially if the certification was not part of the training process. Thus, in our benchmark, we do not measure lower bounds and focus only on upper bounds which are typically much tighter [138].

**Threat models.** We focus on the fully white-box setting, i.e. the model f is assumed to be fully known to the attacker. The threat model is defined by the set  $\Delta$  of the allowed perturbations: the most widely studied ones are the  $\ell_p$ -perturbations, i.e.  $\Delta_p = \{\delta \in \mathbb{R}^d, \|\delta\|_p \leq \varepsilon\}$ , particularly for  $p = \infty$  [135, 46, 88]. We rely on thresholds  $\varepsilon$  established in the literature which are chosen such that the true label should stay the same for each in-distribution input within the perturbation set. We note that robustness towards small  $\ell_p$ -perturbations is a necessary but not sufficient notion of robustness which has been criticized in the literature [45]. It is an active area of research to develop threat models which are more aligned with the human perception such as spatial perturbations [42, 39], Wassersteinbounded perturbations [152, 63], perturbations of the image colors [80] or  $\ell_p$ -perturbations in the latent space of a neural network [81, 150]. However, despite the simplicity of the  $\ell_p$ -perturbation model, it has numerous interesting applications that go beyond security considerations [141, 116] and span transfer learning [117, 145], interpretability [143, 71, 38], generalization [158, 174, 9], robustness to unseen perturbations [68, 158, 81, 73], stabilization of GAN training [173]. Thus, improvements in  $\ell_p$ -robustness have the potential to improve many of these downstream applications.

Additionally, we provide leaderboards for *common image corruptions* [58] that try to mimic modifications of the input images which can occur naturally. Unlike  $\ell_p$  adversarial perturbations, they are not imperceptible and evaluation on them is done in the average-case fashion, i.e. there is no attacker who aims at changing the classifier's decision. In this case, the robustness of a model is evaluated as classification accuracy on the corrupted images, averaged over corruption types and severities.

**Related libraries and benchmarks.** There are many libraries that focus primarily on implementations of popular adversarial attacks such as FoolBox [110], Cleverhans [104], AdverTorch [33], AdvBox [47], ART [98], SecML [92], DeepRobust [85]. Some of them also provide implementations of several basic defenses, but they do not include up-to-date state-of-the-art models. The two challenges [79, 10] hosted at NeurIPS 2017 and 2018 aimed at finding the most robust models for specific attacks, but they had a predefined deadline, so they could capture the best defenses only at the time of the competition. Ling et al. [86] proposed DEEPSEC, a benchmark that tests many combinations of attacks and defenses, but suffers from a few shortcomings as suggested by Carlini [15]: (1) reporting average-case instead of worst-case performance over multiple attacks, (2) evaluating robustness in threat models different from the ones used for training, (3) using excessively large perturbations. Chen and Gu [21] proposed a new *hard-label* black-box attack, RayS, and evaluated it on a range of models which led to a leaderboard (https://github.com/uclaml/RayS). Despite being a state-of-the-art hard-label black-box attack, the robust accuracy in the leaderboard given by RayS still tends to be overestimated even compared to the original evaluations.

Recently, Dong et al. [35] have provided an evaluation of a few defenses (in particular, 3 for  $\ell_{\infty}$ and 2 for  $\ell_2$ -norm on CIFAR-10) against multiple commonly used attacks. However, they did not include some of the best performing defenses [60, 19, 50, 111] and attacks [49, 27], and in a few cases, their evaluation suggests robustness higher than what was reported in the original papers. Moreover, they do not impose any restrictions on the models they accept to the benchmark. RobustML (https://www.robust-ml.org/) aims at collecting robustness claims for defenses together with external evaluations. Their format does not assume running any baseline attack, so it relies entirely on evaluations submitted by the community, which however do not occur often enough. Thus even though RobustML has been a valuable contribution to the community, now it does not provide a comprehensive overview of the recent state of the art in adversarial robustness.

Finally, it has become common practice to test new attacks wrt  $\ell_{\infty}$  on the publicly available models from Madry et al. [88] and Zhang et al. [168], since those represent widely accepted defenses which have stood many thorough evaluations. However, having only two models per dataset (MNIST and CIFAR-10) does not constitute a sufficiently large testbed, and, because of the repetitive evaluations, some attacks may already overfit to those defenses.

What is different in RobustBench. Learning from these previous attempts, RobustBench presents a few different features compared to the aforementioned benchmarks: (1) a baseline worst-case evaluation with an ensemble of *strong*, *standardized* attacks [28] which includes both white- and blackbox attacks, unlike RobustML which is *solely* based on adaptive evaluations, integrated by external evaluations, (2) we add a *flag* in AutoAttack raised when the evaluation might be unreliable, in which case we do additional adaptive evaluations ourselves and encourage the community to contribute, (3) clearly defined threat models that correspond to the ones used during training of submitted models, (4) evaluation of not only standard defenses [88, 168] but also of more recent improvements such as [19, 50, 111]. Moreover, RobustBench is designed as an *open-ended* benchmark that keeps an up-to-date leaderboard, and we welcome contributions of new defenses and evaluations using adaptive attacks. Finally, we open source the Model Zoo for convenient access to the 80+ most robust models from the literature which can be used for downstream tasks and facilitate the development of new standardized attacks.

#### 3 Description of RobustBench

We start by providing a detailed layout of our proposed leaderboards for  $\ell_{\infty}$ ,  $\ell_2$ , and common corruption threat models. Next, we present the Model Zoo, which provides unified access to most networks from our leaderboards.

#### 3.1 Leaderboard

**Restrictions.** We argue that accurate benchmarking adversarial robustness in a standardized way requires some restrictions on the type of considered models. The goal of these restrictions is to prevent submissions of defenses that cause some standard attacks to fail without truly improving robustness. Specifically, we consider only classifiers  $f : \mathbb{R}^d \to \mathbb{R}^C$  that

- have in general *non-zero gradients* with respect to the inputs. Models with zero gradients, e.g., that rely on quantization of inputs [13, 53], make gradient-based methods ineffective thus requiring zeroth-order attacks, which do not perform as well as gradient-based attacks. Alternatively, specific adaptive evaluations, e.g. with Backward Pass Differentiable Approximation [5], can be used which, however, can hardly be standardized. Moreover, we are not aware of existing defenses solely based on having zero gradients for large parts of the input space which would achieve competitive robustness.
- have a *fully deterministic forward pass*. To evaluate defenses with stochastic components, it is a common practice to combine standard gradient-based attacks with Expectation over Transformations [5]. While often effective it might be not sufficient, as shown by Tramèr et al. [142]. Moreover, the classification decision of randomized models may vary over different runs for the same input, hence even the definition of robust accuracy differs from that of deterministic networks. We note that randomization *can* be useful for improving robustness and deriving robustness certificates [82, 25], but it also introduces variance in the gradient estimators (both white- and black-box) making standard attacks much less effective.
- do not have an *optimization loop* in the forward pass. This makes backpropagation through it very difficult or extremely expensive. Usually, such defenses [118, 84] need to be evaluated adaptively with attacks that rely on a combination of hand-crafted losses.

Some of these restrictions were also discussed by [12] for the warm-up phase of their challenge. We refer the reader to Appendix E therein for an illustrative example of a trivial defense that bypasses gradient-based and some of the black-box attacks they consider. We believe that such constraints



Figure 2: Visualization of the robustness and accuracy of 54 CIFAR-10 models from the RobustBench  $\ell_{\infty}$ -leaderboard. Robustness is evaluated using  $\ell_{\infty}$ -perturbations with  $\varepsilon_{\infty} = 8/255$ .

are necessary at the moment since they allow an accurate standardized evaluation which makes the leaderboard meaningful and sustainable. In fact, for defenses not fulfilling the restrictions there is no standard evaluation which is shown to generalize and perform well across techniques, thus one has to resort to time-consuming adaptive attacks specifically tailored for each case. In the design of our benchmark, we thought that it is more important that the robustness evaluation is reliable, rather than being open to all possible defenses with the risk that the robustness is drastically overestimated. As this can lead to a potential bias in our leaderboard, we will lift the restrictions if reliable standardized evaluation methods for these modalities become available in the literature.

**Overall setup.** We set up leaderboards for the  $\ell_{\infty}$ ,  $\ell_2$  and common corruption threat models on CIFAR-10, CIFAR-100 [75], and ImageNet [32] datasets (see Table 1 for details). We use the fixed budgets of  $\varepsilon_{\infty} = 8/255$  and  $\varepsilon_2 = 0.5$  for the  $\ell_{\infty}$  and  $\ell_2$  leaderboards for CIFAR-10 and CIFAR-100. For ImageNet, we use  $\varepsilon_{\infty} = 4/255$  and in App. D, we discuss how we handle that different models use different image resolutions for ImageNet. Most of the models shown in the leaderboards are taken from papers published at top-tier machine learning and computer vision conferences as shown in Fig. 2 (left). For each entry we report the reference to the original paper, standard and robust accuracy under the specific threat model (see the next paragraph for details), network architecture, venue where the paper appeared and possibly notes regarding the model. We also highlight when extra data (often, the dataset introduced by Carmon et al. [19]) is used since it gives a clear advantage for both clean and robust accuracy. If any other attack achieves lower robust accuracy than AutoAttack then we also report it. Moreover, the leaderboard allows to search the entries by their metadata (such as title, architecture, venue) which can be useful to compare different methods that use the same architecture or to search for papers published at some conference.

**Evaluation of defenses.** The evaluation of robust accuracy on common corruptions [58] involves simply computing the average accuracy on corrupted images over different corruption types and severity levels.<sup>1</sup> To evaluate robustness of  $\ell_{\infty}$  and  $\ell_2$  defenses, we currently use AutoAttack [28]. It is an ensemble of four attacks that are run sequentially: a variation of PGD attack with automatically adjusted step sizes, with (1) the cross entropy loss and (2) the difference of logits ratio loss, which is a rescaling-invariant margin-based loss function, (3) the targeted version of the FAB attack [27], which minimizes the  $\ell_p$ -norm of the perturbations, and (4) the black-box Square Attack [4]. Each subsequent attack is run on the points for which an adversarial example has not been found by the preceding attacks. We choose AutoAttack as it includes both black-box and white-box attacks, does not require hyperparameter tuning (in particular, the step size), and consistently improves the results reported in the original papers for almost all the models (see Fig. 2 (middle)). If in the future some new standardized and parameter-free attack is shown to consistently outperform AutoAttack on a wide set of models given a similar computational cost, we will adopt it as standard evaluation. In order to verify the reproducibility of the results, we perform the standardized evaluation independently of the authors of the submitted models. We encourage evaluations of the models in the leaderboard with adaptive or external attacks to reflect the best available upper bound on the true robust accuracy (see a pre-formatted issue template in our repository<sup>2</sup>), in particular in the case where AutoAttack flags that it might not be reliable (see paragraph below). For example, Gowal et al. [50] and Rebuffi et al. [111] evaluate their models with a hybrid of AutoAttack and MultiTargeted attack [49], that in some cases reports slightly lower robust accuracy than AutoAttack alone. We reflect the additional

<sup>&</sup>lt;sup>1</sup>A breakdown over corruptions and severities is also available, e.g. for CIFAR-10 models see: https://github.com/RobustBench/robustbench/blob/master/model\_info/cifar10/corruptions/unaggregated\_results.csv

<sup>&</sup>lt;sup>2</sup>https://github.com/RobustBench/robustbench/issues/new/choose

evaluations in our leaderboard by reporting in a separate column the robust accuracy for the worst case of AutoAttack and all other evaluations. Below we show an example of how one can use our library to easily benchmark a model (either external one or taken from the Model Zoo):

from robustbench.eval import benchmark
clean\_acc, robust\_acc = benchmark(model, dataset='cifar10', threat\_model='Linf')

Moreover, in Appendix E we also show the variability of the robust accuracy given by AutoAttack over random seeds and report its runtime for a few models from different threat models.

Identifying potential need for adaptive attacks. Although AutoAttack provides an accurate estimation of robustness for most models that satisfy the restrictions mentioned above, there might still be corner cases when AutoAttack overestimates robustness of a model that satisfies the restrictions. Carlini et al. [17] suggest that one indicator of possible overestimation of robustness is when black-box attacks are more effective than white-box ones. We noticed that this is the case for the model from Xiao et al. [156] where the black-box Square Attack [4] improves by more than 10% the robust accuracy given by the previous white-box attacks in AutoAttack. We run a simple adaptive attack: Square Attack with multiple random restarts (30 instead of 1) decreases the robust accuracy from the 18.50% of AutoAttack to 7.40%. We note that AutoAttack did not fail completely for this model and correctly revealed a lower level of robustness than reported (52.4%), although the exact robust accuracy was overestimated. Based on this case, we integrate a *flag* in AutoAttack: a warning is output whenever Square Attack reduces of more than 0.2% the robust accuracy compared to the white-box gradient-based attacks in AutoAttack. In this case, AutoAttack evaluation might be not fully reliable and adaptive attacks might be necessary, so we flag the corresponding entries in the leaderboard (currently, only the model of Xiao et al. [156]). Moreover, for the sake of convenience, we also integrate in AutoAttack flags that automatically inform the user if the restrictions are violated.<sup>3</sup>

Adding new defenses. We believe that the leaderboard is only useful if it reflects the latest advances in the field, so it needs to be constantly updated with new defenses. We intend to include evaluations of new techniques and we welcome contributions from the community which help to keep the benchmark up-to-date. We require new entries to (1) satisfy the three restrictions stated above, (2) to be accompanied by a publicly available paper (e.g., an arXiv preprint) describing the technique used to achieve the reported results, and (3) share the model checkpoints (not necessarily publicly). We also allow *temporarily* adding entries without providing checkpoints given that the authors evaluate their models with AutoAttack. However, we will mark such evaluations as *unverified*, and to encourage reproducibility, we reserve the right to remove an entry later on if the corresponding model checkpoint is not provided. It is possible to add a new defense to the leaderboard and (optionally) the Model Zoo by opening an issue with a predefined template in our repository https://github.com/RobustBench/robustbench, where more details about new additions can be found.

#### 3.2 Model Zoo

We collect the checkpoints of many networks from the leaderboard in a single repository hosted at https://github.com/RobustBench/robustbench after obtaining the permission of the authors (see Appendix B for the information on the licenses). The goal of this repository, the Model Zoo, is to make the usage of robust models as simple as possible to facilitate various downstream applications and analyses of general trends in the field. In fact, even when the checkpoints of the proposed method are made available by the authors, it is often time-consuming and not straightforward to integrate them in the same framework because of many factors such as small variations in the architectures, custom input normalizations, etc. For simplicity of implementation, at the moment we include only models implemented in PyTorch [105]. Below we illustrate how a model can be automatically downloaded and loaded via its identifier and threat model within two lines of code:

from robustbench.utils import load\_model
model = load\_model(model\_name='Ding2020MMA', dataset='cifar10', threat\_model='L2')

At the moment, all models (see Table 1 and Appendix G for details) are variations of ResNet [55] and WideResNet architectures [164] of different depth and width. However, we note that the benchmark and Model Zoo are not restricted only to residual or convolutional networks, and we are ready to

<sup>&</sup>lt;sup>3</sup>See https://github.com/fra31/auto-attack/blob/master/flags\_doc.md for details

	CIF	AR-10	CIFA	AR-100	ImageNet		
Threat model	Model Zoo	Leaderboard	Model Zoo	Leaderboard	Model Zoo	Leaderboard	
$\ell_{\infty}$	39	63	14	14	5	6	
$\ell_2$	17	18	-	-	-	-	
Common corruptions [58]	7	15	2	4	5	7	

Table 1: The total number of models in the Model Zoo and leaderboards per dataset and threat model.

add any other architecture. We include the most robust models, e.g. those from Rebuffi et al. [111], but there are also defenses which pursue additional goals alongside adversarial robustness at the fixed threshold we use: e.g., Sehwag et al. [122] consider networks which are robust and compact, Wong et al. [153] focus on computationally efficient adversarial training, Ding et al. [34] aim at input-adaptive robustness as opposed to robustness within a single  $\ell_p$ -radius. All these factors have to be taken into account when comparing different techniques, as they have a strong influence on the final performance. Thus, we highlight these factors in the footnotes below each paper's title.

A testbed for new attacks. Another important use case of the Model Zoo is to simplify comparisons between different adversarial attacks on a wide range of models. First, the leaderboard already serves as a strong baseline for new attacks. Second, as mentioned above, new attacks are often evaluated on the models from Madry et al. [88] and Zhang et al. [168], but this may not provide a representative picture of their effectiveness. For example, currently the difference in robust accuracy between the first and second-best attacks in the CIFAR-10 leaderboard of Madry et al. [88] is only 0.03%, and between the second and third is 0.04%. Thus, we believe that a more thorough comparison should involve multiple models to prevent overfitting of the attack to one or two standard robust defenses.

## 4 Analysis

With unified access to multiple models from the Model Zoo, one can easily compute various performance metrics to see general trends. We analyze various aspects of robust classifiers, mostly for  $\ell_{\infty}$ -robust models on CIFAR-10. Results for other threat models and datasets can be found in App. F.

**Progress on adversarial defenses.** In Fig. 2, we plot a breakdown over conferences, the amount of robustness overestimation reported in the original papers, and we also visualize the robustness-accuracy trade-off for the  $\ell_{\infty}$ -models from the Model Zoo. First, we observe that for multiple *published* defenses, the reported robust accuracy is highly overestimated. We also find that the use of extra data is able to alleviate the robustness-accuracy trade-off as suggested in previous works [108]. However, so far all models with high robustness to perturbations of  $\ell_{\infty}$ -norm up to  $\varepsilon = 8/255$  still suffer from noticeable degradation in clean accuracy compared to standardly trained models. Finally, it is interesting to note that the best entries of the  $\ell_p$ -leaderboards are still variants of PGD adversarial training [88, 168] but with various enhancements (extra data, early stopping, weight averaging).

**Performance across various distribution shifts.** We test the performance of the models from the Model Zoo on different distribution shifts ranging from common image corruptions (CIFAR-10-C, [58]) to dataset resampling bias (CIFAR-10.1, [112]) and image source shift (CINIC-10, [31]). For each of these datasets, we measure standard accuracy, and Fig. 3 shows that improvement in robust accuracy (which often comes with an improvement in standard accuracy) on CIFAR-10 correlates with an improvement in standard accuracy across distributional shifts. On CIFAR-10-C, robust models (particularly with respect to the  $\ell_2$ -norm) tend to give a significant improvement which agrees with the findings in [43]. Concurrently with our work, Taori et al. [137] study the robustness to different distribution shifts of many models trained on ImageNet, including some  $\ell_p$ -robust models. Our conclusions qualitatively agree with theirs, and we hope that our collected set of models will help to provide a more complete picture. Moreover, we measure robust accuracy, in the same threat model used on CIFAR-10, using AutoAttack [28] (see Fig. 10 in Appendix F), in order to see how  $\ell_p$  adversarial robustness generalizes across the datasets representing different distributions shifts, and observe a clear positive correlation between robust accuracy on CIFAR-10 and its variations.

**Calibration.** A classifier is *calibrated* if its predicted probabilities correctly reflect the actual accuracy [52]. In the context of adversarial training, calibration was considered in Hendrycks et al. [61] who focus on improving accuracy on common corruptions and in Augustin et al. [7] who focus mostly on



Figure 3: Standard accuracy of classifiers trained against  $\ell_{\infty}$  (left),  $\ell_2$  (middle), and common corruption (right) threat model respectively, from our Model Zoo on various distribution shifts.

preventing overconfident predictions on out-of-distribution inputs. We instead focus on *in-distribution* calibration, and in Fig. 4 plot the expected calibration error (ECE) without and with temperature rescaling [54] to minimize the ECE (which is a simple but effective post-hoc calibration method, see Appendix F for details) together with the optimal temperature for a large set of  $\ell_{\infty}$  models. We observe that most of the  $\ell_{\infty}$  robust models are significantly *underconfident* since the optimal calibration temperature is less than one for most models. The only two models in Fig. 4 which are *overconfident* are the standard model and the model of Ding et al. [34] that aims to maximize the margin. We see that temperature rescaling is even more important for robust models since without any rescaling the ECE is as high as 70% for the model of Pang et al. [101] (and 21% on average) compared to 4% for the standard model. Temperature rescaling significantly reduces the ECE gap between robust and standard models but it does not fix the problem completely which suggests that it is worth incorporating calibration techniques also during training of robust models. For  $\ell_2$  robust models, the models can be on the contrary *more calibrated* by default, although the improvement vanishes if temperature rescaling is applied (see Appendix F).



Figure 4: Expected calibration error (ECE) before (left) and after (middle) temperature rescaling, and the optimal rescaling temperature (right) for the  $\ell_{\infty}$ -robust models.

**Out-of-distribution detection.** Ideally, a classifier should exhibit high uncertainty in its predictions when evaluated on *out-of-distribution* (OOD) inputs. One of the most straightforward ways to extract this uncertainty information is to use some threshold on the predicted confidence where OOD inputs are expected to have low confidence from the model [59]. An emerging line of research aims at developing OOD detection methods in conjunction with adversarial robustness [57, 120, 7]. In particular, Song et al. [132] demonstrated that adversarial training [88] leads to degradation in the robustness against OOD data. We further test this observation on all  $\ell_{\infty}$ -models trained on CIFAR-10 from the Model Zoo on three OOD datasets: CIFAR-100 [75], SVHN [97], and Describable Textures Dataset [24]. We use the area under the ROC curve (AUROC) to measure the success in the detection of OOD data, and show the results in Fig. 5. With  $\ell_{\infty}$  robust models, we find that compared to standard training, various robust training methods indeed lead to degradation of the OOD detection quality. While extra data in standard training can improve robustness against OOD inputs, it fails to provide similar improvements with robust training. We further find that  $\ell_2$  robust models have in general comparable OOD detection performance to standard models (see Fig. 12 in Appendix), while the model of Augustin et al. [7] achieves even better performance since their approach explicitly optimizes both robust accuracy and worst-case OOD detection performance.

**Fairness in robustness.** Recent works [8, 160] have noticed that robust training [88, 168] can lead to models whose performance varies significantly across subgroups, e.g. defined by classes. We will refer to this performance difference as *fairness*, and here we study the influence of robust training



Figure 5: Visualization of the OOD detection quality (higher AUROC is better) for the  $\ell_{\infty}$ -robust models trained on CIFAR-10 on three OOD datasets: CIFAR-100 (**left**), SVHN (**middle**), Describable Textures (**right**). We detect OOD inputs based on the maximum predicted confidence [59].

methods on fairness. In Fig. 6 we show the breakdown of standard and robust accuracy for the  $\ell_{\infty}$  robust models, where one can see how the achieved robustness largely varies over classes. While in general the classwise standard and robust accuracy correlate well, the class "deer" in  $\ell_{\infty}$ -threat model suffers a significant degradation, unlike what happens for  $\ell_2$  (see Appendix F), which might indicate that the features of such class are particularly sensitive to  $\ell_{\infty}$ -bounded attacks. Moreover, we measure fairness with the relative standard deviation (RSD), defined as the standard deviation divided over the average, of robust accuracy over classes for which lower values mean more uniform distribution and higher robustness. We observe that better robust accuracy generally leads to lower RSD values which implies that the disparity among classes is reduced. (with a strong linear trend): improving the robustness of the models has then the effect of reducing the disparities among classes. However, some training techniques like MART [148] can noticeably increase the RSD and thus *increase the disparity* compared to other methods which achieve similar robustness (around 57%).



Figure 6: Fairness of  $\ell_{\infty}$ -robust models. Left: classwise standard (dotted lines) and robust (solid) accuracy. Right: relative standard deviation (RSD) of robust accuracy over classes vs its average.

**Privacy leakage.** Deep neural networks are prone to memorizing training data [127, 18]. Recent work has highlighted that robust training exacerbates this problem [131]. We benchmark privacy leakage of training data across robust networks (Fig. 7). We calculate membership inference accuracy using output confidence of adversarial images from the training and test sets (see Appendix F for more details). It measures how accurately we can infer whether a sample was present in the training dataset. Our analysis reveals mixed trends. First, our results show that not all robust models have a significantly higher privacy leakage than a standard model. We find that the inference accuracy across robust models has a large variation, where some models even have lower privacy leakage than a standard model, and there is no strong correlation with robust accuracy. In contrast, it is largely determined by the generalization gap, as using the classifier confidence does not lead to a much higher inference accuracy than the baseline determined by the generalization gap (as shown in Fig. 7 (right)). Thus one can expect lower privacy leakage in robust networks as previous work explicitly aimed to reduce the generalization gap in robust training e.g. via early stopping [113, 168, 50].

**Extra experiments.** In Appendix F, we show extra experiments related to the points analyzed above and describe some of the implementation details. Also, we study how adversarial perturbations transfer between different models. We find that adversarial examples strongly transfer from robust to robust, non-robust to robust, and non-robust to non-robust networks. However, we observe poor transferability of adversarial examples from robust to non-robust networks. Finally, since prior works [56, 162] connected higher smoothness with better robustness, we analyze the smoothness of the



Figure 7: Privacy leakage of  $\ell_{\infty}$ -robust models. We measure privacy leakage of training data in robust networks and compare it with robust accuracy (left) and generalization gap (right).

models both at intermediate and output layers. This confirms that, for a fixed architecture, standard training yields classifiers that are significantly less smooth than robust ones. This study of properties of networks illustrates another useful aspect of our Model Zoo.

#### 5 Outlook

Conclusions. We believe that a *standardized* benchmark with clearly defined threat models, restrictions on submitted models, and tight upper bounds on robust accuracy is useful to show which ideas in training robust models are the most successful. While AutoAttack is for most models very reliable and accurate and allows a standardized comparison, we ensure by flagging potentially unreliable evaluations and doing additional adaptive attacks that the benchmark reflects the best possible robustness assessment with limited resources as the exact robustness evaluation is computationally infeasible. We remark that recent works have already referred to our leaderboards [74, 163, 89, 136, 159], in particular as reflecting the current state of the art [111, 83, 103], and used the networks of our Model Zoo to test new adversarial attacks [92, 115, 41, 119], evaluate test-time defenses [146] or perceptual distances derived from them [67], explore further properties of robust models [134, 172]. Additionally, we have shown that unified access to a *large* and *up-to-date* set of robust models can be useful to analyze multiple aspects related to robustness. First, one can easily analyze the progress of adversarial defenses over time including the amount of robustness overestimation and the robustness-accuracy tradeoff. Second, one can conveniently study the impact of robustness on other performance metrics such as accuracy under distribution shifts, calibration, out-of-distribution detection, fairness, privacy leakage, smoothness, and transferability. Overall, we think that the community has to develop a better understanding of how different types of robustness affect other aspects of the model performance and RobustBench can help to achieve this goal. Finally, we note that a good performance on our benchmark does not guarantee the safety of the benchmarked model in a real-world deployment since  $\ell_p$ - and corruption robustness may not be sufficiently representative of all realistic threat models.

**Future plans.** Our intention in the future is to keep the current leaderboards up-to-date (see the maintenance plan in Appendix C) and add new leaderboards for other datasets and other threat models which become widely accepted in the community. We see as potential candidates (1) sparse perturbations, e.g. bounded by  $\ell_0$ ,  $\ell_1$ -norm or adversarial patches [11, 26, 93, 29], (2) multiple  $\ell_p$ -norm perturbations [140, 90], (3) adversarially optimized common corruptions [68, 69], (4) a broad set of perturbations unseen during training [81]. Another possible direction is the development of a standardized evaluation of recent defenses based on some form of test-time adaptation [126, 146], which do not fulfill the third restriction (no optimization loop). Finally, although the benchmark currently focuses on image classification, we think that its structure and principles should apply to other tasks (e.g., image segmentation [157], image retrieval [139]) and domains (e.g., natural language processing [2], malware detection [51]) where adversarial robustness can be of interest. Since this direction requires more domain-specific expertise, we welcome contributions from different communities to expand RobustBench.

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## A Broader impact

We note that the restrictions we impose on the defenses allowed in our benchmark could lead to a potential bias of the community which discourages research in certain directions. It is certainly not our goal to discourage research in directions which violate restrictions of the benchmark. However, without these restrictions a reliable evaluation of adversarial robustness is not feasible and a reliable evaluation of adversarial robustness in order to identify true advances in the field is key for further progress. Thus we think that these restrictions are unavoidable for a benchmark but we are working on relaxing the restrictions as much as possible.

Additionally, in motivating higher robustness against adversarial examples, our work may leave an unwanted side effect on tasks where adversarial attacks can actually be used for beneficial purposes [76, 125, 109]. However, this is true for any paper that aims at improving adversarial robustness (either directly or indirectly via, e.g., a standardized benchmark).

On the positive side, in our work, we do not only perform a standardized benchmarking of adversarial robustness but also analyze multiple other properties of robust models such as calibration, privacy leakage, fairness, etc. In our opinion, such analyses are important since they allow us to assess the broader impact of improving robustness on other crucial performance metrics of neural networks.

Finally, we note that a good performance on our benchmark does not guarantee the safety of the benchmarked model in a real-world deployment which is likely to require more domain-specific threat models.  $\ell_p$ -bounded adversarial attacks can be a realistic threat model in applications where it is possible to input an image directly in a digital format [141, 116]. However, attacks in-the-wild [78, 40] are usually much more involved and differ considerably from the presented simple  $\ell_p$ -perturbations. Moreover, the common corruptions we used for evaluation from Hendrycks and Dietterich [58] are artificially generated, and thus may differ from the corruptions encountered in the real world. Taking this into account, we suggest to always think critically about the robustness requirements that are necessary for a particular application at hand.

# **B** Licenses

The code used for benchmarking is released under MIT license. The code of AutoAttack [28] that our benchmark relies on has been released under the MIT license as well. The classifiers in the Model Zoo are added according to the permission given by the authors with the license they choose: most of the models have MIT license, other have more restrictive ones such as Attribution-NonCommercial-ShareAlike 4.0 International, Apache License 2.0, BSD 3-Clause License. The details can be found at https://github.com/RobustBench/robustbench/blob/master/LICENSE. The CIFAR-10 and CIFAR-100 datasets [75] are obtained via the PyTorch loaders [105], while CIFAR-10-C and CIFAR-100-C [58], with the common corruptions, are downloaded from the official release (see https://zenodo.org/record/2535967#.YLYf9agzaUk and https://zenodo.org/record/3555552#.YLYeJagzaUk). The validation set of ImageNet is not hosted or downloaded by our provided evaluation code, but it needs to be downloaded in advance directly by the user.

# C Maintenance plan

Here we discuss the main aspects of maintaining RobustBench and the costs associated with it:

- Hosting the website (https://robustbench.github.io/): we host our leaderboard using GitHub pages<sup>4</sup> which is a free service.
- Hosting the library (https://github.com/RobustBench/robustbench): the code of our library is hosted on GitHub<sup>5</sup> which offers the basic features that we need to maintain the library for free.

<sup>&</sup>lt;sup>4</sup>https://pages.github.com/ <sup>5</sup>https://github.com/

- Hosting the models: to ensure the availability of the models from the Model Zoo, we host them in our own cloud storage on Google Drive<sup>6</sup>. At the moment, they take around 24 GB of space which fits into the 100 GB storage plan that costs 2 USD per month.
- **Running evaluations**: we run all evaluations on the GPU servers that are available to our research groups which incurs no extra costs.

Moreover, as we mention in the outlook (Sec. 5), we also plan to expand the benchmark to new datasets and threat models which can slightly increase the required maintenance costs since we may need to upgrade the storage plan. We also expect the benchmark to be community-driven and to encourage this we have provided instructions<sup>7</sup> on how to submit new entries to the leaderboard and to the Model Zoo.

### **D** Details of the ImageNet leaderboards

Extending the benchmark to ImageNet presents some challenges compared to CIFAR-10 and CIFAR-100. First, the ImageNet validation set (usually used as the test set) contains 50'000 images which makes it infeasible to run expensive evaluations on it. Thus, we define a fixed subset (5'000 randomly sampled images in our case) for faster evaluation, whose image IDs we make available in the Model Zoo. Second, it is not obvious how to handle the fact that different models may use different preprocessing techniques (e.g., different resolution, cropping, etc) which makes the search space for an attack *not fully comparable* across defenses. For this, we decide to allow models with different preprocessing steps and input resolution, considering them yet another design choice similarly to the choice of the network architecture which also has a large influence on the final results. Since in the  $\ell_{\infty}$ -threat model the constraints are componentwise independent, we use the same threshold  $\varepsilon_{\infty} = 4/255$  for every classifier, regardless of the input dimensionality which is used after preprocessing.

## E Reproducibility and runtime

Here we discuss the main aspects of the reproducibility of the benchmark.

First of all, the code to run the benchmark on a given model is available in our repository, and an example of how to run it is given in the README file. The installation instructions are also provided in the README file and the requirements will be installed automatically.

To satisfy other points from the reproducibility checklist<sup>8</sup> which are applicable to our benchmark, we also discuss next the variability of the robust accuracy over random seeds and the average runtime of the benchmark. Evaluation of the accuracy on common corruptions [58] is deterministic if we do not take into account non-deterministic operations on computational accelerators such as GPUs<sup>9</sup> which, however, do not affect the resulting accuracy. On the other hand, robustness evaluation using AutoAttack has an element of randomness since it relies on random initialization of the starting points and also on the randomness in the update of the Square Attack [4]. To show the effect of randomness on the robust accuracy given by AutoAttack, we repeat evaluation over four random seeds on four models available in the Model Zoo from different threat models covering all datasets considered. In Table 2, we report the average robust accuracy with its standard deviation and observe that different seeds lead to very similar results. Moreover, we indicate the runtime of each evaluation, which is largely influenced by the size of the model, the computing infrastructure (every run uses a single Tesla V100 GPU), and the dataset. Moreover, less robust models require less time for evaluation which is due to the fact that AutoAttack does not further attack a point if an adversarial example is already found by some preceding attack in the ensemble.

Additionally, as mentioned above, for ImageNet we have randomly sampled and fixed 5000 images from the validation set. We provide the IDs of those images and code to load them in our repository. Note that we use the same set of images for  $\ell_p$ -robustness and for common corruptions, in which case for every point 15 types of corruptions at 5 severity levels are applied, consistently with the other datasets.

<sup>&</sup>lt;sup>6</sup>https://www.google.com/drive/

<sup>&</sup>lt;sup>7</sup>https://github.com/RobustBench/robustbench#adding-a-new-model

<sup>&</sup>lt;sup>8</sup>https://www.cs.mcgill.ca/~jpineau/ReproducibilityChecklist.pdf

<sup>&</sup>lt;sup>9</sup>https://pytorch.org/docs/stable/notes/randomness.html

Finally, when we extended the benchmark to ImageNet, we noticed that different versions of PyTorch and torchvision may lead to small differences in the standard accuracy (up to 0.16% on 5000 points for the same model). We suspect this is due to minor variations in the implementation of the preprocessing functions (such as resizing). Thus, we fix in the requirements torch==1.7.1 and torchvision==0.8.2 to ensure reproducibility. Note that the overall *ranking* and level of robustness of the defenses should not be influenced by using different versions of these libraries. We have not noticed similar issues for the other datasets.

Table 2: Statistics about the standardized evaluation with AutoAttack when repeated for four random seeds. We can see that the robust accuracy has very small fluctuations. We also report the runtime for the different models which is much smaller for less robust models.

Dataset	Leaderboard	Paper	Architecture	Clean acc.	Robust acc.	Time
CIFAR-10	$\ell_{\infty}$	Gowal et al. [50]	WRN-28-10	89.48%	$62.82\% \pm 0.016$	11.8 h
CIFAR-10	$\ell_2$	Rebuffi et al. [111]	WRN-28-10	91.79%	$78.80\% \pm 0.000$	15.1 h
CIFAR-100	$\ell_{\infty}$	Wu et al. [155]	WRN-34-10	60.38%	$28.84\% \pm 0.018$	6.6 h
ImageNet	$\ell_{\infty}$	Salman et al. [117]	ResNet-18	52.92%	$25.31\% \pm 0.010$	1.6 h

#### **F** Additional analysis

In this section, we show more results on different datasets and/or threat models and discuss some implementation details related to the analysis from Sec. 4. We also additionally analyze the *smoothness* and *transferability* properties of the models from the Model Zoo.

**Progress on adversarial defenses.** As done in the main part for the  $\ell_{\infty}$ -robust models on CIFAR-10, we show here the same statistics but for  $\ell_2$ -robust models on CIFAR-10 in Fig. 8 and for  $\ell_{\infty}$ -robust models on CIFAR-100 in Fig. 9. We observe a few differences compared to the  $\ell_{\infty}$ -robust models on CIFAR-10 reported in Fig. 2. First of all, the amount of robustness overestimation is not large and in particular there are no models that have *zero* robust accuracy. Second, we can see that the best  $\ell_2$ -robust models on CIFAR-10 has even higher standard accuracy than a standard model (95.74% vs 94.78%) while having a significantly higher robust accuracy. Finally, we note that the progress on the  $\ell_{\infty}$ -threat model on CIFAR-100 is more recent and there are only a few published papers that report adversarial robustness on this dataset.



Figure 8: Visualization of the robustness and accuracy of 13 CIFAR-10 models from the RobustBench  $\ell_2$ -leaderboard. Robustness is evaluated using  $\ell_2$ -perturbations with  $\varepsilon_2 = 0.5$ .

**Robustness across distribution shifts.** We measure robust accuracy on various distribution shifts using four dataset, namely CIFAR-10, CINIC-10, CIFAR-10.1, and CIFAR-10-C. In particular, we compute the robust accuracy in the same threat model as for the original CIFAR-10 dataset, and report the results in Fig. 10. Interestingly, one can observe that  $\ell_p$  adversarial robustness is maintained under the distribution shifts, and it highly correlates with the robustness on the dataset the models were trained on (i.e. CIFAR-10).

**Calibration.** We compute the expected calibration error (ECE) using the code of [52]. We use their default settings to compute the calibration error which includes, in particular, binning of the probability range onto 15 equally-sized bins. However, we use our own implementation of the temperature rescaling algorithm which is close to that of [7]. Since optimization of the ECE over the



Figure 9: Visualization of the robustness and accuracy of 12 CIFAR-100 models from the RobustBench  $\ell_{\infty}$ -leaderboard. Robustness is evaluated using  $\ell_{\infty}$ -perturbations with  $\varepsilon_{\infty} = 8/255$ .



Figure 10: Robust accuracy of the robust classifiers, trained against  $\ell_{\infty}$  and  $\ell_2$  threat model, respectively, from our Model Zoo on various distribution shifts. The data points with 0% robust accuracy correspond to a standardly trained model.

softmax temperature is a simple *one-dimensional* optimization problem, we can solve it efficiently using a grid search. Moreover, the advantage of performing a grid search is that we can optimize directly the metric of interest, i.e. ECE, instead of the cross-entropy loss as in [52] who had to rely on a differentiable loss since they used LBFGS [87] to optimize the temperature. We perform a grid search over the interval  $t \in [0.001, 1.0]$  with a grid step 0.001 and we test both t and 1/t temperatures. Moreover, we check that for all models the optimal temperature t is situated not at the boundary of the grid.

We show additional calibration results for  $\ell_2$ -robust models in Fig. 11. The overall trend of the ECE is the same as for  $\ell_{\infty}$ -robust models: most of the  $\ell_2$  models are underconfident (since the optimal temperature is less than one) and lead to worse calibration before and after temperature rescaling. The main difference compared to the  $\ell_{\infty}$  threat model is that among the  $\ell_2$  models there are two models that are *better-calibrated*: one before (Engstrom et al. [37] with 1.41% ECE vs 3.71% ECE of the standard model) and one after (Gowal et al. [50] with 1.00% ECE vs 1.11% ECE of the standard model) temperature rescaling. Moreover, we can see that similarly to the  $\ell_{\infty}$  case, the only overconfident models are either the standard one or models that maximize the margin instead of using norm-bounded perturbations, i.e. Ding et al. [34] and Rony et al. [114].



Figure 11: Expected calibration error (ECE) before (**left**) and after (**middle**) temperature rescaling, and the optimal rescaling temperature (**right**) for the  $\ell_2$ -robust models.

**Out-of-distribution detection.** Fig. 12 complements Fig. 5 and shows the ability of  $\ell_2$ -robust models trained on CIFAR-10 to distinguish inputs from other datasets (CIFAR-100, SVHN, Describable Textures). We find that  $\ell_2$  robust models have in general comparable OOD detection performance to standardly trained models, while the model by Augustin et al. [7] achieves even better perfor-

mance since their approach explicitly optimizes both robust accuracy and worst-case OOD detection performance.



Figure 12: Visualization of the quality of OOD detection (higher AUROC is better) for the  $\ell_2$ -robust models on three different OOD datasets: CIFAR-100 (left), SVHN (middle), Describable Textures (right).

**Fairness in robustness.** We report the results about fairness for robust models in the  $\ell_2$ -threat model in Fig. 13, similarly to what done for  $\ell_{\infty}$  above. We see that the difference in robustness among classes is similar to what observed for the  $\ell_{\infty}$  models. Also, the RSD of robustness over classes decreases, which indicates that the disparity among subgroups is reduced, as the average robust accuracy improves. To compute the robustness for the experiments about fairness we used APGD on the targeted DLR loss [28] with 3 target classes and 20 iterations each on the whole test set. Note that even with this smaller budget we achieve results very close to that of the full evaluation, with an average difference smaller than 0.5%.



Figure 13: Left: classwise standard (dotted lines) and robust (solid) accuracy of  $\ell_2$ -robust models. Right: relative standard deviation (RSD) of robust accuracy over classes vs its average.

**Privacy leakage.** We use membership inference accuracy, referred to as inference accuracy, as a measure of the leakage of training data details from pre-trained neural networks. It measures how successfully we can identify whether a particular sample was present in the training set. We closely follow the methodology described in Song and Mittal [130] to calculate inference accuracy. In particular, we measure the confidence in the correct class for each input image with a pre-trained classifier. We measure the confidence for both training and test set images and calculate the maximum classification accuracy between train and test images based on the confidence values. We refer to this accuracy as *inference accuracy using confidence*. We also follow the recommendation from Song et al. [131] where they show that adversarial examples are more successful in estimating inference accuracy on robust networks. In our experiments, we also find that using adversarial examples leads to higher inference accuracy than benign images (Figure 14). We also find that robust networks in the  $\ell_{\infty}$  threat model.

A key reason behind privacy leakage through membership inference is that deep neural networks often end up overfitting on the training data. One standard metric to measure overfitting is the generalization gap between train and test set. Naturally, this difference in the accuracy on the train and test set is the baseline of inference accuracy. We refer to it as *inference accuracy using label* and report it in Figure 15. We consider both benign and adversarial images. When using benign images, we find confidence information does lead to higher inference accuracy than using only labels. However, with adversarial examples, which achieve higher inference accuracy than benign images, we find that inference accuracy based on confidence information closely follows the inference accuracy calculate from labels.



Figure 14: Comparing privacy leakage of different networks. We compare membership inference accuracy from benign and adversarial images across both  $\ell_{\infty}$  and  $\ell_2$  threat model.



Figure 15: **Comparing privacy leakage with different output statistics.** We measure privacy leakage using membership inference accuracy, i.e., classification success between train and test set. We measure it using two baselines 1) based on correct prediction i.e., using predicted class label and 2) based on classification confidence in correct class. We also measure it using both benign and adversarial images.

**Smoothness.** Previous work [162] has shown that smoothness of a model, together with enough separation between the classes of the dataset for which it is trained, is necessary to achieve both natural and robust accuracy. They use local Lipschitzness as a measure for model smoothness, and observe empirically that robust models are more smoother than models trained in a standard way. Our Model Zoo enables us to check this fact empirically on a wider range of robust models, trained with a more diverse set of techniques, in particular with and without extra training data. Moreover, as we have access to the model internals, we can also compute local Lipschitzness of the model up to arbitrary layers, to see how smoothness changes between layers.

We compute local Lipschitzness using projected gradient descent (PGD) on the following optimization problem:

$$L = \frac{1}{N} \sum_{i=1}^{N} \max_{\substack{x_1: \|x_1 - x_i\|_{\infty} \le \varepsilon \\ x_2: \|x_2 - x_i\|_{\infty} \le \varepsilon}} \frac{\|f(x_1) - f(x_2)\|_1}{\|x_1 - x_2\|_{\infty}},$$
(2)

where  $x_i$  represents each sample around which we compute local Lipschitzness, N is the number of samples across which we average (N = 256 in all our experiments), and f represents the function whose Lipschitz constant we compute. As mentioned above, this function can be either the full model, or the model up to an arbitrary intermediate layer.

Since the models can have similar smoothness behavior, but at a different scale, we also consider normalizing the models outputs. One such normalization we use is given by the projection of the model outputs on the unit  $\ell_2$  ball. This normalization aims at capturing the angular change of the output, instead of taking in consideration also its magnitude. We compute the "angular" version of the Lipschitz constant as

$$L = \frac{1}{N} \sum_{i=1}^{N} \max_{\substack{x_1: \|x_1 - x_i\|_{\infty} \le \varepsilon, \\ x_2: \|x_2 - x_i\|_{\infty} \le \varepsilon}} \frac{\left\| \frac{f(x_1)}{\|f(x_1)\|_2} - \frac{f(x_2)}{\|f(x_2)\|_2} \right\|_1}{\|x_1 - x_2\|_{\infty}}.$$
(3)

For both variations of Lipschitzness, we compute it with  $\varepsilon = 8/255$ , running the PDG-like procedure for 50 steps, with a step size of  $\varepsilon/5$ .



Figure 16: Lipschitzness. Computation of the local Lipschitz constant of the WRN-28-10  $\ell_{\infty}$ -robust models in our Model Zoo with  $\varepsilon = 8/255$ . The color coding of the models is the same across both figures. For the correspondence between model IDs (shown in the legend) and papers that introduced them, see Appendix G.



Figure 17: Lipschitzness vs Robustness. Local Lipschitz constant of the output layer vs. robust accuracy of a subset of the  $\ell_{\infty}$ -robust models in our Model Zoo.

In Fig. 16 we compute the layerwise Lipschitzness for all  $\ell_{\infty}$  models trained on CIFAR-10 from the Model Zoo that have the WRN-28-10 architecture. We observe that the standard model is the least smooth at all the layers, and that all the robustly trained models are smoother. Moreover, we can notice that in Fig. 16a there are two models in the middle ground: these are the models by Gowal et al. [50] and Rebuffi et al. [111], which are the most robust ones, up to the last layer, the smoothest. Nonetheless, in the middle layers, they are the second and third least smooth, according to the unnormalized local Lipschitzness. This can be due to the different activation function used in these models (Swish vs ReLU). For this reason, we also compute "angular" Lipschitzness according to Eq. 3. Indeed, in Fig. 16b, all the robust models are in the same order of magnitude at all layers.

Finally, we also show the Lipschitz constants of the output layer for a larger set of  $\ell_{\infty}$  models from the Model Zoo that are not restricted to the same architecture. We plot the Lipschitz constant vs. the robust accuracy for these models in Fig 17. We see that there is a clear relationship between robust accuracy and Lipschitzness, hence confirming the findings of Yang et al. [162].

**Transferability.** We generate adversarial examples for a network, referred to as source network, and measure robust accuracy of every other network, referred to as target network, from the model zoo on them. We also include additional non-robust models<sup>10</sup>, to name a few, VGG19, ResNet18, and DenseNet121, in our analysis. We consider both ten step PGD attack and FGSM attack to generate adversarial examples as two transferability baselines commonly used in the literature. For both attacks, we use the cross-entropy loss, and for the PGD attack we use ten iterations and step size  $\varepsilon/4$ .

We present our results in Figure 18, 19 where the correspondence between model IDs and papers that introduced them can be found in Appendix G. We find that transferability to each robust target network follows a similar trend where adversarial examples transfer equally well from another robust

<sup>&</sup>lt;sup>10</sup>We train then for 200 epochs and achieve 93-95% clean accuracy for all networks on the CIFAR-10 dataset.

networks. Though slight worse than robust network, adversarial example from non-robust network also transfer equally well to robust networks. We observe a strong transferability among non-robust networks with adversarial examples generated from PGD attacks. Adversarial examples generated using the FGSM attack also transfer successfully. However, they achieve lower robust accuracy on the target network. Intriguingly, we observe the weakest transferability from a robust to a non-robust network. This observation holds for all robust source networks across both FGSM and PGD-attack in both  $\ell_{\infty}$  and  $\ell_2$  threat model.

## **G** Leaderboards

We here report the details of all the models included in the various leaderboards, for the  $\ell_{\infty}$ -,  $\ell_2$ -threat models and common corruptions. In particular, we show for each model the clean accuracy, robust accuracy (either on adversarial attacks or corrupted images), whether additional data is used for training, the architecture used, the venue at which it appeared and, if available, the identifier in the Model Zoo (which is also used in some of the experiments in Sec. F).



Target network (Adversarial examples are evaluated on it)

Figure 18: Measuring transferability of adversarial examples ( $\ell_{\infty}$ ,  $\epsilon = 8/255$ ). We use a ten step PGD attack in top figure and FGSM attack in bottom figure. Lower robust accuracy implies better transferability. 26



Figure 19: Measuring transferability of adversarial examples ( $\ell_2$ ,  $\epsilon = 0.5$ ). We use a ten step PGD attack in top figure and FGSM attack in bottom figure. Lower robust accuracy implies better transferability.

Table 3: Leaderboard for the  $\ell_{\infty}$ -threat model, CIFAR-10.

	Model	Clean	Robust	Extra data	Architecture	Venue	Model Zoo ID
1	Rebuffi et al. [111]	92.23	66.56	Y	WRN-70-16	arXiv, Mar 2021	Rebuffi2021Fixing 70 16 cutmix extra
2	Gowal et al. [50]	91.10	65.87	Y	WRN-70-16	arXiv, Oct 2020	Gowal2020Uncovering 70 16 extra
3	Rebuffi et al. [111]	88.50	64.58	N	WRN-106-16	arXiv, Mar 2021	Rebuffi2021Fixing 106 16 cutmix ddpm
4	Rebuffi et al. [111]	88.54	64.20	N	WRN-70-16	arXiv, Mar 2021	Rebuffi2021Fixing_70_16_cutmix_ddpm
5	Rade and Moosavi-Dezfooli [107]	91.47	62.83	Y	WRN-34-10	OpenReview, Jun 2021	Rade2021Helper_extra
6	Gowal et al. [50]	89.48	62.76	Y	WRN-28-10	arXiv, Oct 2020	Gowal2020Uncovering_28_10_extra
7	Rade and Moosavi-Dezfooli [107]	88.16	60.97	N	WRN-28-10	OpenReview, Jun 2021	Rade2021Helper_ddpm
8	Rebuffi et al. [111]	87.33	60.73	N	WRN-28-10	arXiv, Mar 2021	Rebuffi2021Fixing_28_10_cutmix_ddpm
9	Wu et al. [154]	87.67	60.65	Y	WRN-34-15	arXiv, Oct 2020	N/A
10	Sridhar et al. [133]	86.53	60.41	Y	WRN-34-15	arXiv, Jun 2021	Sridhar2021Robust_34_15
11	Wu et al. [155]	88.25	60.04	Y	WRN-28-10	NeurIPS 2020	Wu2020Adversarial_extra
12	Sridhar et al. [133]	89.46	59.66	Y	WRN-28-10	arXiv, Jun 2021	Sridhar2021Robust
13	Zhang et al. [171]	89.36	59.64	Y	WRN-28-10	ICLR 2021	Zhang2020Geometry
14	Carmon et al. [19]	89.69	59.53	Y	WRN-28-10	NeurIPS 2019	Carmon2019Unlabeled
15	Sehwag et al. [123]	85.85	59.09	N	WRN-34-10	arXiv, Apr 2021	Sehwag2021Proxy
16	Rade and Moosavi-Dezfooli [107]	89.02	57.67	Y	PreActRN-18	OpenReview, Jun 2021	Rade2021Helper_R18_extra
17	Gowal et al. [50]	85.29	57.14	N	WRN-70-16	arXiv, Oct 2020	Gowal2020Uncovering_/0_16
18	Sehwag et al. [121]	88.98	57.14	Y	WRN-28-10	NeurIPS 2020	Sehwag2020Hydra
19	Rade and Moosavi-Dezfool [107]	80.80	57.09	IN N	PTEACIKIN-18	OpenKeview, Jun 2021	Causi2020Lineauring 24, 20
20	Cowaret al. [30]	83.04	56.62	IN	WKIN-34-20	arAiv, Oct 2020	Babuff2020Uncovering_34_20
21	Wenn et al. [111]	85.55	56.00	IN N	WDN 28 10	ICL D 2020	Wag = 2020 January in a
22	What al [155]	87.30	56.17	I	WRIN-28-10 WRN 24-10	NeurIDS 2020	Wu2020A dvarcarial
23	Wu ct al. [155]	86.46	56.02	v	WRN-34-10	NeurIPS 2020	WU2020Adversariar
24	Hendrycks et al. [60]	87.11	54.02	v	WRN 28 10	ICML 2019	Hendrycks2010Using
26	Sebwag et al [123]	8/ 38	54.43	N	PN 18	arXiv Apr 2021	Sehwag2021Provy P18
20	Pang et al [102]	86.43	54.39	N	WRN-34-20	ICLR 2021	N/A
28	Pang et al [101]	85.14	53.74	N	WRN-34-20	NeurIPS 2020	Pang2020Boosting
29	Cui et al [30]	88 70	53 57	N	WRN-34-20	ICCV 2021	Cui2020Learnable 34 20
30	Zhang et al. [170]	84.52	53.51	N	WRN-34-10	ICML 2020	Zhang2020Attacks
31	Rice et al. [113]	85.34	53.42	N	WRN-34-20	ICML 2020	Rice2020Overfitting
32	Huang et al. [64]	83.48	53.34	N	WRN-34-10	NeurIPS 2020	Huang2020Self
33	Zhang et al. [168]	84.92	53.08	N	WRN-34-10	ICML 2019	Zhang2019Theoretically
34	Cui et al. [30]	88.22	52.86	N	WRN-34-10	ICCV 2021	Cui2020Learnable_34_10
35	Qin et al. [106]	86.28	52.84	N	WRN-40-8	NeurIPS 2019	N/A
36	Chen et al. [23]	86.04	51.56	N	RN-50	CVPR 2020	Chen2020Adversarial
37	Chen et al. [22]	85.32	51.12	N	WRN-34-10	arXiv, Oct 2020	Chen2020Efficient
38	Sitawarin et al. [129]	86.84	50.72	N	WRN-34-10	arXiv, Mar 2020	Sitawarin2020Improving
39	Engstrom et al. [37]	87.03	49.25	N	RN-50	GitHub, Oct 2019	Engstrom2019Robustness
40	Singh et al. [128]	87.80	49.12	N	WRN-34-10	IJCAI 2019	N/A
41	Mao et al. [91]	86.21	47.41	N	WRN-34-10	NeurIPS 2019	N/A
42	Zhang et al. [165]	87.20	44.83	N	WRN-34-10	NeurIPS 2019	Zhang2019You
43	Madry et al. [88]	87.14	44.04	N	WRN-34-10	ICLR 2018	N/A
44	Andriushchenko and Flammarion [3]	79.84	43.93	N	PreActRN-18	NeurIPS 2020	Andriushchenko2020Understanding
45	Pang et al. [99]	80.89	43.48	N	RN-32	ICLR 2020	N/A
46	Wong et al. [153]	83.34	43.21	N	PreActRN-18	ICLR 2020	Wong2020Fast
47	Shafahi et al. [124]	86.11	41.47	N	WRN-34-10	NeurIPS 2019	N/A
48	Ding et al. [34]	84.36	41.44	N	WRN-28-4	ICLR 2020	Ding2020MMA
49	Kundu et al. [77]	87.32	40.41	N	RN-18	ASP-DAC 2021	N/A
50	Atzmon et al. [6]	81.30	40.22	N	RN-18	NeurIPS 2019	N/A
51	Moosavi-Deztooli et al. [94]	83.11	38.50	N	KN-18	CVPR 2019	N/A N/A
52	Zhang and Wang [166]	89.98	30.04	IN N	WRN-28-10	Neurips 2019	N/A N/A
55	Znang and Xu [167]	90.25	30.45	IN N	WKN-28-10	OpenKeview, Sep 2019	N/A N/A
55	Jang et al. [03] Kim and Wang [72]	/6.91	34.95	IN	WDN 24 10	OpenPaview Sep 2010	IN/A N/A
55 56	Theng et al. [160]	91.51	32.64	IN N	5 laver CNN	ICLP 2020	IN/A N/A
57	Wang and Zhang [147]	44.75	20.35	N	WDN 28 10	ICCV 2010	N/A N/A
58	Viao et al [156]	70.29	29.55	N	DenseNet 121	ICL P 2019	N/A N/A
50	Jin and Rinard [66]	90.84	1.35	N	RN-18	arXiv Mar 2020	N/A N/A
60	Mustafa et al [96]	89.16	0.28	N	RN-110	ICCV 2019	N/A
61	Chan et al. [20]	93 70	0.26	N	WRN_34_10	ICLR 2020	N/A N/A
62	Standard	94 78	0.0	N	WRN-28-10	N/A	N/A
63	Alfarra et al. [1]	91.03	0.00	N	WRN-28-10	arXiv, Jun 2020	N/A

Table 4: Leaderboard for the  $\ell_2$ -threat model, CIFAR-10.

	Model	Clean	Robust	Extra data	Architecture	Venue	Model Zoo ID
1	Rebuffi et al. [111]	95.74	82.32	Y	WRN-70-16	arXiv, Mar 2021	Rebuffi2021Fixing_70_16_cutmix_extra
2	Gowal et al. [50]	94.74	80.53	Y	WRN-70-16	arXiv, Oct 2020	Gowal2020Uncovering_extra
3	Rebuffi et al. [111]	92.41	80.42	N	WRN-70-16	arXiv, Mar 2021	Rebuffi2021Fixing_70_16_cutmix_ddpm
4	Rebuffi et al. [111]	91.79	78.80	N	WRN-28-10	arXiv, Mar 2021	Rebuffi2021Fixing_28_10_cutmix_ddpm
5	Augustin et al. [7]	93.96	78.79	Y	WRN-34-10	ECCV 2020	Augustin2020Adversarial_34_10_extra
6	Augustin et al. [7]	92.23	76.25	Y	WRN-34-10	ECCV 2020	Augustin2020Adversarial_34_10
7	Rade and Moosavi-Dezfooli [107]	90.57	76.15	N	PreActRN-18	OpenReview, Jun 2021	Rade2021Helper_R18_ddpm
8	Sehwag et al. [123]	90.31	76.12	N	WRN-34-10	arXiv, Apr 2021	Sehwag2021Proxy
9	Rebuffi et al. [111]	90.33	75.86	N	PreActRN-18	arXiv, Mar 2021	Rebuffi2021Fixing_R18_cutmix_ddpm
10	Gowal et al. [50]	90.90	74.50	N	WRN-70-16	arXiv, Oct 2020	Gowal2020Uncovering
11	Wu et al. [155]	88.51	73.66	N	WRN-34-10	NeurIPS 2020	Wu2020Adversarial
12	Sehwag et al. [123]	89.52	73.39	N	RN-18	arXiv, Apr 2021	Sehwag2021Proxy_R18
13	Augustin et al. [7]	91.08	72.91	Y	RN-50	ECCV 2020	Augustin2020Adversarial
14	Engstrom et al. [37]	90.83	69.24	N	RN-50	GitHub, Sep 2019	Engstrom2019Robustness
15	Rice et al. [113]	88.67	67.68	N	PreActRN-18	ICML 2020	Rice2020Overfitting
16	Rony et al. [114]	89.05	66.44	N	WRN-28-10	CVPR 2019	Rony2019Decoupling
17	Ding et al. [34]	88.02	66.09	N	WRN-28-4	ICLR 2020	Ding2020MMA
18	Standard	94.78	0.0	Ν	WRN-28-10	N/A	Standard

Table 5: Leaderboard for common corruptions, CIFAR-10.

	Model	Clean	Corr.	Extra data	Architecture	Venue	Model Zoo ID
1	Calian et al. [14]	94.93	92.17	Y	RN-50	arXiv, Apr 2021	N/A
2	Kireev et al. [73]	94.75	89.60	N	RN-18	arXiv, Mar 2021	Kireev2021Effectiveness_RLATAugMix
3	Hendrycks et al. [61]	95.83	89.09	N	ResNeXt29_32x4d	ICLR 2020	Hendrycks2020AugMix_ResNeXt
4	Hendrycks et al. [61]	95.08	88.82	N	WRN-40-2	ICLR 2020	Hendrycks2020AugMix_WRN
5	Kireev et al. [73]	94.77	88.53	N	PreActRN-18	arXiv, Mar 2021	Kireev2021Effectiveness_RLATAugMixNoJSD
6	Rebuffi et al. [111]	92.23	88.23	Y	WRN-70-16	arXiv, Mar 2021	Rebuffi2021Fixing_70_16_cutmix_extra_L2
7	Gowal et al. [50]	94.74	87.68	Y	WRN-70-16	arXiv, Oct 2020	N/A
8	Kireev et al. [73]	94.97	86.60	N	PreActRN-18	arXiv, Mar 2021	Kireev2021Effectiveness_AugMixNoJSD
9	Kireev et al. [73]	93.24	85.04	N	PreActRN-18	arXiv, Mar 2021	Kireev2021Effectiveness_Gauss50percent
10	Gowal et al. [50]	90.90	84.90	N	WRN-70-16	arXiv, Oct 2020	N/A
11	Kireev et al. [73]	93.10	84.10	N	PreActRN-18	arXiv, Mar 2021	Kireev2021Effectiveness_RLAT
12	Rebuffi et al. [111]	92.23	82.82	Y	WRN-70-16	arXiv, Mar 2021	Rebuffi2021Fixing_70_16_cutmix_extra_Linf
13	Gowal et al. [50]	91.10	81.84	Y	WRN-70-16	arXiv, Oct 2020	N/A
14	Gowal et al. [50]	85.29	76.37	N	WRN-70-16	arXiv, Oct 2020	N/A
15	Standard	94.78	73.46	Ν	WRN-28-10	N/A	Standard

Table 6: Leaderboard for the  $\ell_\infty\text{-threat model},$  CIFAR-100.

	Model	Clean	Robust	Extra data	Architecture	Venue	Model Zoo ID
1	Gowal et al. [50]	69.15	36.88	Y	WRN-70-16	arXiv, Oct 2020	Gowal2020Uncovering_extra
2	Rebuffi et al. [111]	63.56	34.64	Ν	WRN-70-16	arXiv, Mar 2021	Rebuffi2021Fixing_70_16_cutmix_ddpm
3	Rebuffi et al. [111]	62.41	32.06	N	WRN-28-10	arXiv, Mar 2021	Rebuffi2021Fixing_28_10_cutmix_ddpm
4	Cui et al. [30]	62.55	30.20	Ν	WRN-34-20	ICCV 2021	Cui2020Learnable_34_20_LBGAT6
5	Gowal et al. [50]	60.86	30.03	N	WRN-70-16	arXiv, Oct 2020	Gowal2020Uncovering
6	Cui et al. [30]	60.64	29.33	Ν	WRN-34-10	ICCV 2021	Cui2020Learnable_34_10_LBGAT6
7	Rade and Moosavi-Dezfooli [107]	61.50	28.88	N	PreActRN-18	OpenReview, Jun 2021	Rade2021Helper_R18_ddpm
8	Wu et al. [155]	60.38	28.86	N	WRN-34-10	NeurIPS 2020	Wu2020Adversarial
9	Rebuffi et al. [111]	56.87	28.50	N	PreActRN-18	arXiv, Mar 2021	Rebuffi2021Fixing_R18_ddpm
10	Hendrycks et al. [60]	59.23	28.42	Y	WRN-28-10	ICML 2019	Hendrycks2019Using
11	Cui et al. [30]	70.25	27.16	Ν	WRN-34-10	ICCV 2021	Cui2020Learnable_34_10_LBGAT0
12	Chen et al. [22]	62.15	26.94	Ν	WRN-34-10	arXiv, Oct 2020	Chen2020Efficient
13	Sitawarin et al. [129]	62.82	24.57	N	WRN-34-10	ICML 2020	Sitawarin2020Improving
14	Rice et al. [113]	53.83	18.95	Ν	PreActRN-18	ICML 2020	Rice2020Overfitting

Table 7: Leaderboard for common corruptions, CIFAR-100.

	Model	Clean	Corr.	Extra data	Architecture	Venue	Model Zoo ID
1	Hendrycks et al. [61]	78.90	65.14	Ν	ResNeXt29_32x4d	ICLR 2020	Hendrycks2020AugMix_ResNeXt
2	Hendrycks et al. [61]	76.28	64.11	Ν	WRN-40-2	ICLR 2020	Hendrycks2020AugMix_WRN
3	Gowal et al. [50]	69.15	56.00	Y	WRN-70-16	arXiv, Oct 2020	Gowal2020Uncovering_extra_Linf
4	Gowal et al. [50]	60.86	49.46	Ν	WRN-70-16	arXiv, Oct 2020	Gowal2020Uncovering_Linf

Table 8: Leaderboard for the  $\ell_{\infty}$ -threat model, ImageNet.

	Model	Clean	Robust	Extra data	Architecture	Venue	Model Zoo ID
1	Salman et al. [117]	68.46	38.14	Ν	WRN-50-2	NeurIPS 2020	Salman2020Do_50_2
2	Salman et al. [117]	64.02	34.96	Ν	RN-50	NeurIPS 2020	Salman2020Do_R50
3	Engstrom et al. [37]	62.56	29.22	Ν	RN-50	GitHub, Oct 2019	Engstrom2019Robustness
4	Wong et al. [153]	55.62	26.24	Ν	RN-18	ICLR 2020	Wong2020Fast
5	Salman et al. [117]	52.92	25.32	Ν	RN-50	NeurIPS 2020	Salman2020Do_R18
6	Standard_R50	76.52	0.0	Ν	RN-50	N/A	Standard_R50

Table 9: Leaderboard for common corruptions, ImageNet.

	Model	Clean	Corr.	Extra data	Architecture	Venue	Model Zoo ID
1	Hendrycks et al. [62]	76.88	51.61	Ν	RN-50	ICCV 2021	Hendrycks2020Many
2	Hendrycks et al. [61]	76.98	46.91	Ν	RN-50	ICLR 2020	Hendrycks2020AugMix
3	Geirhos et al. [44]	74.88	44.48	Ν	RN-50	ICLR 2019	Geirhos2018_SIN_IN
4	Geirhos et al. [44]	77.44	40.77	Ν	RN-50	ICLR 2019	Geirhos2018_SIN_IN_IN
5	Standard_R50	76.52	38.12	Ν	RN-50	N/A	Standard_R50
6	Geirhos et al. [44]	60.24	37.95	Ν	RN-50	ICLR 2019	Geirhos2018_SIN
7	Salman et al. [117]	68.46	34.60	Ν	WRN-50-2	NeurIPS 2020	Salman2020Do_50_2_Linf