Groupthink:

Collective Delusions in Organizations and Markets

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Abstract

This paper investigates collective denial and willful blindness in groups, organizations and markets. Agents with anticipatory preferences, linked through an interaction structure, choose how to interpret and recall public signals about future prospects. Wishful thinking (denial of bad news) is shown to be contagious when it is harmful to others, and self-limiting when it is beneficial. Similarly, with Kreps-Porteus preferences, willful blindness (information avoidance) spreads when it increases the risks borne by others. This general mechanism can generate multiple social cognitions of reality, and in hierarchies it implies that realism and delusion will trickle down from the leaders. The welfare analysis differentiates group morale from groupthink and identifies a fundamental tension in organizations' attitudes toward dissent. Contagious exuberance can also seize asset markets, generating investment frenzies and crashes.

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The Columbia accident is an unfortunate illustration of how NASA's strong cultural bias and its optimistic organizational thinking undermined effective decision-making." (Columbia Accident Investigation Board Final Report, 2003)

"The ability of governments and investors to delude themselves, giving rise to periodic bouts of euphoria that usually end in tears, seems to have remained a constant. (Reinhart and Rogoff, "This Time Is Different: Eight Centuries of Financial Folly", 2009).

1. Introduction

In the aftermath of corporate and public-sector disasters, it often emerges that participants fell prey to a collective form of willful blindness and overconfidence: mounting warning signals were systematically cast aside or met with denial, evidence avoided or selectively reinterpreted, dissenters shunned. Market bubbles and manias exhibit the same pattern of investors acting "color-blind in a sea of red flags", followed by a crash.¹ To shed light on these phenomena, this paper analyzes how distorted beliefs spread through organizations such as firms, bureaucracies and markets.

Janis (1972), studying policy decisions such as the Bay of Pigs invasion, the Cuban missile crisis and the escalation of the Vietnam war, identified in those that ended disastrously a cluster of symptoms for which he coined the term "groupthink". Although later work was critical of his characterization of those episodes, the concept has flourished and spurred a large literature in social and organizational psychology. Defined in Merriam-Webster's dictionary as "a pattern of thought characterized by self-deception, forced manufacture of consent, and conformity to group values and ethics", groupthink was strikingly documented in the official inquiries conducted on the Challenger and Columbia space shuttle disasters. It has also been invoked as a contributing factor in the failures of companies such as Enron and Worldcom, decisions relating to the second Iraq war, and the recent financial crisis. At

¹I borrow here the evocative title of Norris' (2008) account of Merrill Lynch's mortgage securitization debacle. A year later, the Inspector General's Report (2009) on the SEC's failure concerning the Madoff scheme contained over 130 mentions of "red flags".

²The eight symptoms were: (a) illusion of invulnerability; (b) collective rationalization; (c) belief in inherent morality; (d) stereotyped views of out-groups; (e) direct pressure on dissenters; (f) self-censorship; (g) illusion of unanimity; (h) self-appointed mindguards. The model developed here will address (a) to (g).

³On the shuttle accidents, see Rogers Commission (1986) and Columbia Accident Investigation Board (2003). On Enron, see Samuelson (2001), Cohan (2002), Eichenwald (2005) and Pearlstein (2006). On Iraq, see e.g., Hersh (2004), Suskind (2004) and Isikoff and Corn (2007).

the same time, one must keep in mind that the mirror opposite of harmful "groupthink" is valuable "group morale" and therefore ask how the two mechanisms differ, even though both involve the maintenance of collective optimism despite negative signals.

To analyze these issues, I develop a model of (individually rational) collective denial and willful blindness. Agents are engaged in a joint enterprise where their final payoff will be determined by their own action and those of others, all affected by a common productivity shock. To distinguish groupthink from standard mechanisms, there are no complementarities in payoffs, nor any private signals that could give rise to herding or social learning. Each agent derives anticipatory utility from his future prospects, and consequently faces a tradeoff: he can accept the grim implications of negative public signals about the project's value (realism) and act accordingly, or maintain hopeful beliefs by discounting, ignoring or forgetting such data (denial), at the risk of making overoptimistic decisions.

The key observation is that this tradeoff is shaped by how others deal with bad news, creating cognitive linkages. When an agent benefits from others' overoptimism, his improved prospects make him more accepting of the bad news which they ignore. Conversely, when he is made worse off by others' blindness to adverse signals, the increased loss attached to such news pushes him toward denial, which is then contagious. Thinking styles thus become strategic substitutes or complements, depending on the sign of externalities (not cross-partials) in the interaction payoffs. When interdependence among participants is high enough, this *Mutually Assured Delusion* (MAD) principle can give rise to multiple equilibria with different "social cognitions" of the same reality. The same principle also implies that, in organizations where some agents have a greater impact on others' welfare than the reverse (e.g., managers on workers), strategies of realism or denial will "trickle down" the hierarchy, so that subordinates will in effect take their beliefs from the leader.

The underlying insight is quite general and, in particular, does not depend on the assumptions of anticipatory utility and malleable memory or awareness. To demonstrate this point, I analyze a variant of the model in which both are replaced by Kreps-Porteus (1978) preferences for late resolution of uncertainty. This also serves, importantly, to address collective willful ignorance (ex-ante avoidance of information) in the same way as the benchmark model addresses collective denial (ex-post distortion of beliefs). In line with the MAD principle, I show that if an agent's remaining uninformed about the state of the world leads him to

increase the *risks* borne by others, this pushes them toward also delaying becoming informed; as a result, ignorance becomes contagious and risk spreads through the organization. Conversely, when information avoidance has beneficial hedging spillovers, it is self-dampening.⁴

The model's welfare analysis makes clear what factors distinguish valuable group morale from harmful groupthink, irrespective of anticipatory payoffs, which average out across states of the world. It furthermore explains why organizations and societies find it desirable to set up ex-ante commitment mechanisms protecting and encouraging dissent (constitutional guarantees of free speech, whistle-blower protections, devil's advocates, etc.), even when ex-post everyone would unanimously want to ignore or "kill" the messengers of bad news.

In market interactions, finally, prices typically introduce a substitutability between supply decisions that works against collective belief. Nonetheless, in asset markets with limited liquidity (new types of securities, startup firms, housing), contagious exuberance can again take hold, leading to investment frenzies followed by deep crashes. When signals about fundamentals turn from green to red, each participant who keeps investing contributes to driving the final market-clearing price further down. This makes it ultimately more costly for others to also overinvest, but at the same time magnifies the capital losses that realism would require them to immediately acknowledge on their outstanding positions. In equilibrium the stock effect can dominate the flow effect, so that all prefer to keep believing in strong fundamentals than recognize the warning signals of a looming crash.

In the remainder of this section, I provide empirical evidence on both types of cognitive distortions (ex-ante and ex-post) considered in the model. On the theoretical side, the paper relates to two broad literatures: (i) self-deception, anticipatory preferences and attitudes toward information; (ii) social conformity, herding and bubbles. I defer this discussion to Section 7, where it will be clearer in light of the formal model and analysis.

Asymmetric updating and information avoidance. Besides the vast literature on overconfidence and overoptimism, there is a long-standing body of work more specifically documenting people's tendency to selectively process, interpret and recall data in ways that lead to more favorable beliefs about their own traits or future prospects.⁵ While earlier stud-

⁴Thus, as in the anticipatory-utility version, agents' "patterns of thought" become substitutes or complements in a way that turns entirely on the first derivatives of the payoff structure. The difference is that these externalities now operate on the variance rather than the conditional expectation of agents' utilities.

⁵See, e.g., Mischel et al. [1976] and Thompson et al. [1992] on the differential recall of favorable and

ies relied on self-reports rather than incentivized choices, several recent papers offer rigorous confirmations of a differential response to good and bad news. Eil and Rao (2010) and Möbius et al. (2010) provide subjects with several rounds of objective data on their IQ rankings; the first paper uses physical attractiveness as well. They also elicit, using incentive-compatible scoring rules, subjects' prior and posterior beliefs about their rank. Eil and Rao find that, compared with Bayes' rule, subjects systematically underrespond to negative news and are much closer to proper updating for positive news. Möbius et al. similarly find significant underupdating in response to bad news; subjects also update less than fully in response to good news, but the gap with Bayes' rule is significantly smaller. In both studies, a significant fraction of subjects also display information aversion, paying money to avoid learning their exact IQ or beauty score after the last round.⁶

Mijovic-Prelec and Prelec (2010) demonstrate costly self-deception about the likelihood of an exogenous binary event: although incentivized for accuracy, subjects reverse their predictions as a function of their stakes in the outcome. Similarly, Mayraz (2011) finds that subjects assigned to be buyers or sellers at some future price make (incentivized) predictions about it that vary systematically with their monetary stakes in its being high or low. These results establish the role of the anticipatory motive in belief distortion and show that the latter responds to incentives, as will be the case in the model.

In the field, Choi and Lou (2010) find evidence of self-serving, asymmetric updating by mutual fund managers. Using a large panel of actively managed funds, they measure a manager's confidence in his stock-picking ability or private signal quality by the deviation, attributable to his active trades, between his portfolio weights and the relevant market index. Following confirming signals (positive realized excess returns over the year), fund managers trade more actively, thereby exhibiting increased self-confidence. Following disconfirming ones (negative realized excess returns) there is no equivalent decrease—in fact, zero adjustment cannot be rejected. Furthermore, this selective updating leads to subopti-

unfavorable, information, and Kunda [1987] on the biased processing of self-relevant data.

⁶In contrast, no updating bias or information avoidance occurs when rank is randomly assigned. For self-relevant information, both findings of underadjustment to bad news and a lesser underadjustment (possibly none) to good news accord very well with the awareness-management model of Bénabou and Tirole (2002), which corresponds to equation (6) below (see also footnote 18).

⁷Using FMRI to identify the neural correlates of self-deception, Hedden et al. (2008) furthermore show that self-deceivers (as identified by their more systematic prediction reversals) exhibit distinctive activity patterns in the regions of the brain associated to reward processing and to attentional and cognitive control.

mal investments, as positive past excess returns are found to negatively predict subsequent risk-adjusted fund performance. Individual investors also display a good-news / bad news asymmetry, both in the recall of their portfolios' past returns (Goetzman and Peles (1997)) and in informational decisions, where far more go online to look up the value of their portfolios on days when the market is up than when it is down (Karlsson et al. (2009)).

The avoidance of decision-relevant information for fear of learning of a bad outcome is extensively documented in the medical sphere, where significant fractions of people avoid checkups, refuse to take tests for HIV infection or genetic predispositions to certain cancers, even when anonymity is ensured and in countries with universal health insurance and strict anti-discrimination regulations. This body of evidence and its relationship to anticipatory anxiety are reviewed in Caplin and Leahy (2001) and Caplin and Eliaz (2003).

Organizational and market blindness. These individual propensities to cognitive distortion naturally raise the question of equilibrium: what environments will make such behaviors socially contagious or self-limiting, and with what welfare implications? Surprisingly, this question has never been considered, even in the large literature on informational attitudes that followed Kreps and Porteus (1978). Yet the issue is not only theoretically interesting, but also potentially important to make sense of notions such as "optimistic organizational thinking" and "governments and investors deluding themselves".

While there is yet no formal study of motivated cognition at the level of a firm or market, a number of in-depth case studies and official investigation reports provide supporting evidence for the idea. I summarize in online Appendix D several "patterns of denial" –including again actively avoiding information ex-ante and changing standards of evidence ex-post– that recurstrikingly from NASA to the FED, SEC and Fannie Mae, from Enron to investment banks, AIG and individual investors.⁸ The historical studies of financial crises by Mckay (1980), Kindleberger and Aliber (2005), Shiller (2005) and Reinhart and Rogoff (2009) provide many similar examples, from which their conclusions of contagious "delusions", "manias", "irrational exuberance" and "financial folly" are derived.⁹

⁸Another point made there is the insufficiency of moral hazard as the sole explanation. Instead, self-serving rationalizations ("ethical fading", e.g., Tenbrunsel, and Messick (2004), Bazerman and Tenbrunsel (2011)) and overoptimistic hubris are key enablers of most corporate misconduct and financial fraud (see also Huseman and Driver (1979), Sims (1992), Anand et al. (2005) and Schrand and Zechman (2008)).

⁹In standard models of herding and cascades, by contrast, investors are cool-headed, rational information processors who follow others only when warranted by optimal inference (see Section 6 for further discussion).

For the financial crisis of 2008, there is specific evidence of collective overoptimism by the groups who had the most at stake in ever-rising housing prices (consistently with the model), and against standard views of moral hazard or herding. Cheng et al. (2012) show that mid-level managers in the mortgage securitization business (insiders) were more likely to buy a house at the peak of the bubble, and slower to divest as prices started falling, than either real estate lawyers or financial analysts covering non-housing companies (outsiders). Foote et al. (2012) document how banks and dealers issuing mortgage-backed securities kept a lot of it on their books, resulting in huge losses; also as in the model, their analysts understood fairly well how the assets would fare under different housing-price scenarios but assigned very low probabilities to adverse ones, even after prices started falling nationwide.

Section 2 presents the benchmark model and propositions on collective realism and denial. Section 3 examines welfare and the treatment of dissent. Section 4 deals with asset-market manias and crashes. Section 5 uses risk preferences to study the contagion of ex-ante attitudes toward information (also a contribution of independent interest). Section 6 discusses the model's relations to other theories, and Section 7 concludes. Key proofs are gathered in Appendix A, extensions and more technical proofs in online Appendices B and C respectively.

2. Groupthink in teams and organizations

2.1. Benchmark model

• Technology. A group of risk-neutral agents, $i \in \{1,...n\}$, are engaged in a joint project (team, firm, military unit) or other activities generating spillovers; see Figure 1. At t = 1, each chooses effort $e^i = 0$ or 1, with cost ce^i , c > 0. At t = 2, he will reap expected utility

(1)
$$U_2^i \equiv \theta \left[\alpha e^i + (1 - \alpha)e^{-i} \right],$$

where $e^{-i} \equiv \frac{1}{n-1} \sum_{j \neq i} e^j$ is the average effort of others and $1 - \alpha \in [0, 1 - 1/n]$ the degree of interdependence, reflecting the joint nature of the enterprise.¹⁰ Depending on α , the choice of e^i ranges from a pure private good (or bad) to a pure public one. This payoff structure

¹⁰ Another source is the presence of cross-interests or interests or social preferences: altruism, family or kinship ties, social identity, etc. Thus, (1) is equivalent to $U_2^i \equiv \beta \theta e^i + (1-\beta)U_2^{-i}$ with $1-\alpha \equiv (1-\beta)(n-1)/(n-\beta)$. Altruistic concerns are explicitly studied in online Appendix B.

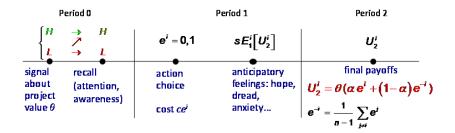


Figure 1: Timeline

is maximally simple: all agents play symmetric roles, there is a fixed value to inaction e = 0, normalized to 0, and no interdependence of any kind between effort decisions. These assumptions serve only to highlight the key mechanism, and are all relaxed later on.

The productivity of the venture is a priori uncertain. At t=0, everyone observes a common signal that is either good or bad news: $\sigma=H,L$, with probabilities q and 1-q respectively. The project's expected value is $\theta=\theta_H$ in the good-news state H and $\theta=\theta_L$ in the bad-news state L, with $\Delta\theta\equiv\theta_H-\theta_L>0$ and $\theta_H>0$ without loss of generality. Depending on the context, θ can represent the value of a firm's product or business plan, the state of the market, the suitability of a political or military strategy, or the quality of a leader. Given (1), θ defines the expected social value of a choice $e^j=1$, relative to what the alternative course of action would yield. Thus, for $\theta_L\geq0$ each agent would prefer that others always choose $e^j=1$, whereas for $\theta_L<0$ he would like them to pursue the "appropriate" course of action for the organization, choosing $e^j=1$ in state H and $e^j=0$ in state L. Description of the context of the state H and H and

• Preferences. The payoffs received during period 1 include the cost of effort, $-ce^i$, but also the anticipatory utility experienced from thinking about one's future prospects, $sE_1^i[U_2^i]$, where $s \geq 0$ (for "savoring" or "susceptibility") parametrizes the well-documented psychological and health effects of hopefulness, dread and similar emotions. ¹³

At the start of period 1, agent i chooses effort to maximize the expected present value of payoffs, discounted at rate $\delta \in (0,1]$:

¹¹Note that θ_{σ} is only the *expected* value of the project conditional on σ , so a low (high) signal need not preclude a high (low) final realization of payoffs.

¹²It is thus not the sign of θ_L per se that is relevant, but how θ_L compares to the (social) return to taking the alternative action e = 0 in state L. The latter's normalization to zero is relaxed in Section 2.4.

¹³The parameter s also increases with the duration of uncertainty (period 1), while the discount factor δ in (2) correspondingly decreases as the "final reckoning" is further postponed. The linear specification $sE_1^i[U_2^i]$ avoids building in either information-loving or information aversion (which will be studied in Section 5).

(2)
$$U_1^i = -ce^i + sE_1^i [U_2^i] + \delta E_1^i [U_2^i].$$

Given (1), his effort is determined solely by his beliefs about $\theta : e^i = 1$ if $(s + \delta)\alpha E_1^i[\theta] > c$, independently of what any one else may be doing. I shall assume that

(3)
$$\theta_L < \frac{c}{(s+\delta)\alpha} < \frac{c}{\delta\alpha} < q\theta_H + (1-q)\theta_L.$$

An agent acting on his sole prior will thus choose $e^i = 1$, whereas one who knows for sure that the state is L will abstain. Actual beliefs at t = 1 will depend on the news received at t = 0 and how objectively or subjectively the agent processes them, as described below. In doing so, he aims to maximize the discounted utility of all payoffs

(4)
$$U_0^i = -M^i + \delta E_0^i \left[-ce^i + sE_1^i \left[U_2^i \right] \right] + \delta^2 E_0^i \left[U_2^i \right],$$

where E_t^i denotes expectations at t=0,1 and M^i the date-0 costs of his cognitive strategy.

The main behavioral implications of these preferences arise from the tradeoff between accurate and hopeful beliefs embodied in (4). To the extent that his cognitive "technology" allows it, an agent will update in a distorted manner (underadjusting to bad news as in Rao and Eil (2010) and Möbius et al. (2010)), and consequently invest even after seeing data showing that he should not. In short, he will engage in wishful thinking.¹⁴

- Information and beliefs. To represent agents' "patterns of thought", I use an extended version of the selective-recall technology in Bénabou and Tirole (2002). Upon observing the signal $\sigma = H, L$ at t = 0, each agent chooses (consciously or not) how much attention to pay to the news, how to interpret it, whether to "keep it in mind" or "not think about it", etc. Formally, he can:
- (a) Accept the facts realistically, truthfully encoding $\hat{\sigma}^i = \sigma$ into memory or awareness (his date-1 information set).
- (b) Engage in denial, censoring or rationalization, encoding $\hat{\sigma}^i = H$ instead of $\sigma = L$, or $\hat{\sigma}^i = L$ instead of $\sigma = H$. In addition to impacting later decisions, this may entail an

¹⁴Namely, "the attribution of reality to what one wishes to be true or the tenuous justification of what one wants to believe" (Merriam Webster), and "the formation of beliefs and making decisions according to what might be pleasing to imagine instead of by appealing to evidence, rationality or reality" (Wikipedia).

immediate cost $m \ge 0.15$

(c) When indifferent between these two courses of actions, use a mixed strategy. 16

This simple informational structure captures a broad range of situations. The perfect correlation between agents' signals could be relaxed, but serves to make clear that the model has nothing to do with herding or cascades, where privately informed agents make inferences from each other's behavior. The prior distribution (q, 1 - q) could be conditional on an earlier positive signal, such as the appearance of a new technology or market opportunity that warranted some initial investments, including the formation of the group itself.

Intuition suggests that it is only in state L that an agent may censor his signal: given (1) and the utility from anticipation, he would never want to substitute bad news for good ones.¹⁷ Verifying in Appendix C that such is indeed the case as long as m > 0, no matter how small, I focus here on cognitive decisions in state L and denote

(5)
$$\lambda^i \equiv \Pr\left[\hat{\sigma}^i = L | \sigma = L\right]$$

the awareness strategy of agent i. Later on I will consider payoffs structures more general than (1), under which either state may be censored.

While people can selectively process information, their latitude to self-deceive is generally not unconstrained. At t = 1, agent i no longer has direct access to the original signal, but if he is aware of his tendency to discount bad news he will take it into account. Thus, when

 $^{^{15}}$ This can involve material resources (eliminating evidence, avoiding certain people, searching for and rehearsing desirable signals) or mental ones (stress from repression, cognitive dissonance, guilt). As explained below, any arbitrarily small m > 0 suffices to rule out uninteresting equilibria in which there is signal distortion in both states ("inefficient encoding"). Beyond this, all the paper's key results apply equally with m = 0, though non-zero costs are more realistic, particularly for the welfare analysis.

 $^{^{16}}$ Agents thus do not commit in advance to a (state-contingent) mixture of realism and denial, but respond optimally to the news they receive. It seems unlikely that someone could constrain a priori how he will interpret or recall different signals, particularly in a social context where he may be exposed to others' response to the news. Such commitment is more plausible at the organizational level, and this is analyzed in Section 3. For a sophisticated Bayesian, cognitive commitment (when feasible) would be equivalent to coarsening the signal structure $\sigma = H, L$; such ex-ante informational choices are studied in Section 5.

¹⁷An agent who likes pleasant surprises and dislikes disappointments, on the other hand, may want to. Such preferences correspond (maintaining linearity) to $s = -\delta s'$, 0 < s' < 1, so that the last two terms in (4) become $\delta^2 E_0^i \left[U_2^i - s' E_1^i \left[U_2^i\right]\right]$. All results could be transposed to the case s < 0, leading to a (less empirically relevant) model of collective "defensive pessimism". Focusing on $s \ge 0$ means that anticipatory concerns dominate disappointment-aversion ones; such is the case, for instance, when the "waiting" period 1 is long enough. The potential social or evolutionary value of anticipatory concerns is discussed in Section 3.

 $\hat{\sigma}^i = L$ he knows for sure that the state is L, but when $\hat{\sigma}^i = H$ his posterior belief is only

(6)
$$\Pr\left[\sigma = H \mid \hat{\sigma}^i = H, \lambda^i\right] = \frac{q}{q + (1 - q)\chi(1 - \lambda^i)} \equiv r(\lambda^i),$$

where λ^i is his equilibrium rate of realism (awareness of bad news) and $\chi \in [0, 1]$ parametrizes cognitive sophistication. I shall focus on the benchmark case of rational Bayesians ($\chi = 1$), but the analysis goes through for any χ , including full naiveté ($\chi = 0$).¹⁸

To analyze the equilibria of this game, I proceed in three steps. First, I fix everyone but agent i's awareness strategy at some arbitrary $\lambda^{-i} \in [0,1]$ and look for his "best response" λ^{i} . Second, I identify the general principle that governs whether individual cognitions are strategic substitutes (the more others delude themselves, the better informed I want to be) or complements (the more others delude themselves, the less I also want to face the truth). Finally, I derive conditions under which groupthink arises in its most striking form, where both collective realism and collective denial constitute self-sustaining social cognitions.

2.2. Best-response awareness

Following bad news, agents who remain aware that $\theta = \theta_L$ do not exert effort, while those who managed to ignore or rationalize away the signal have posterior $r(\lambda^j) \geq q$ and choose $e^j = 1$. Responding as a realist to a signal $\sigma = L$ thus leads for agent i to intertemporal expected utility (R is for "realism")

(7)
$$U_{0,R}^{i} = \delta(\delta + s) \left[\alpha \cdot 0 + (1 - \alpha)(1 - \lambda^{-i}) \right] \theta_{L},$$

reflecting his knowledge that only the fraction $1 - \lambda^{-i}$ of other agents who are in denial will exert effort. If he censors, on the other hand, he will assign probabilities $r(\lambda^i)$ to the state being H, in which case everyone exerts effort with productivity θ_H , and $1 - r(\lambda^i)$ to it being

¹⁸The paper's positive results become only stronger with $\chi < 1$, as self-deception is more effective. In the welfare analysis, an extra term is simply added to the criterion computed with $\chi = 1$; see footnote 33. Note also that (6) generates both empirical findings discussed in footnote 6, for any $\lambda^i < 1$ and $\chi < q/(1-q)$.

¹⁹ With imperfect recall, each agent's problem is itself a game of strategic information transmission between his date-0 and date-1 "selves". Condition (3) and m > 0 will rule out any multiplicity of intrapersonal equilibria, simplifying the analysis and making clear that the groupthink phenomenon is one of *collectively* sustained cognitions. With many identical agents, the focus on symmetric group equilibria (implicit in equating all λ^i 's to a common λ^{-i}) is without loss of generality. On asymmetric equilibria, see Section 2.4.

really L, in which case only the other optimists like him are working and their output is $(1 - \lambda^{-i})\theta_L$. Hence (D is for "denial"):

(8)
$$U_{0,D}^{i} = -m + \delta \left(-c + \delta \left[\alpha + (1 - \alpha)(1 - \lambda^{-i}) \right] \theta_{L} \right) + \delta s \left(r(\lambda^{i})\theta_{H} + \left(1 - r(\lambda^{i}) \right) \left[\alpha + (1 - \alpha)(1 - \lambda^{-i}) \right] \theta_{L} \right).$$

Agent i's incentive to deny reality, given that a fraction $1 - \lambda^{-i}$ of others do so, is thus:

(9)
$$U_{0,D}^{i} - U_{0,R}^{i} = -m - \delta \left[c - (\delta + s) \alpha \theta_{L} \right] + \delta s r(\lambda^{i}) \left[(1 - \alpha) \lambda^{-i} \theta_{L} + \Delta \theta \right].$$

The second term is the net loss from mistakenly choosing $e^i = 1$ due to overoptimistic beliefs.²⁰ The third term is the gain in anticipatory utility, proportional to s and the posterior belief $r(\lambda^i)$ that the state is H, which has two effects. First, the agent raises his estimate of the fraction choosing e = 1, from $1 - \lambda^{-i}$ to 1; at the true productivity θ_L , this contributes $(1 - \alpha)\lambda^{-i}\theta_L$ to his expected welfare. Second, he believes the project's value to be θ_H rather than θ_L , so that when everyone chooses e = 1 his welfare is higher by $\Delta \theta = \theta_H - \theta_L$.

Let $\Psi(\lambda^i, s|\lambda^{-i})$ denote the right-hand side of (9), representing agent *i*'s net incentive for denial. Since it is increasing in his "habitual" degree of realism λ^i , there is a unique fixed point (personal equilibrium), which characterizes the optimal awareness strategy:

(a) $\lambda^i = 1$ if $\Psi(1, s | \lambda^{-i}) \leq 0$. By (9), and noting that $\alpha \theta_L + \Delta \theta + (1 - \alpha) \lambda^{-i} \theta_L \geq \min \{\Delta \theta, \theta_H\} > 0$, this means

(10)
$$s \leq \frac{m/\delta + c - \delta\alpha\theta_L}{\alpha\theta_L + \Delta\theta + (1 - \alpha)\lambda^{-i}\theta_L} \equiv \underline{s}(\lambda^{-i}).$$

(b) $\lambda^{i} = 0$ if $\Psi(0, s | \lambda^{-i}) \geq 0$. By (9), and noting that $\alpha \theta_{L} + q \left[\Delta \theta + (1 - \alpha) \lambda^{-i} \theta_{L} \right] \geq \min \left\{ q \Delta \theta, q \theta_{H} + (1 - q) \theta_{L} \right\} > \min \left\{ q \Delta \theta, c / (s + \delta) \right\} > 0$, this means

(11)
$$s \ge \frac{m/\delta + c - \delta \alpha \theta_L}{\alpha \theta_L + q \left[\Delta \theta + (1 - \alpha) \lambda^{-i} \theta_L\right]} \equiv \bar{s}(\lambda^{-i}).$$

Moreover, $\underline{s}(\lambda^{-i}) < \overline{s}(\lambda^{-i})$, since $\Delta \theta + (1 - \alpha)\lambda^{-i}\theta_L \ge \Delta \theta + (1 - \alpha)\lambda^{-i}\min\{\theta_L, 0\} \ge \Delta \theta + \min\{\theta_L, 0\} = \min\{\theta_H, \Delta \theta\} > 0$.

²⁰Due to the linearity of agents' payoffs it is independent of the actions (and therefore the beliefs) of others, but this is relaxed in Appendix B, which extends the results to nonseparable payoffs; see also Section 4.

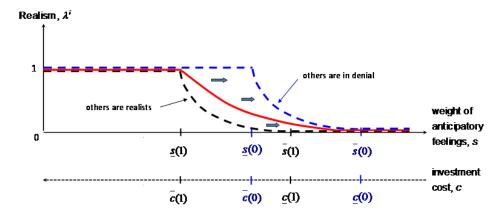


Figure 2: Group Morale ($\theta_L > 0$). The dashed lines give agent *i*'s optimal awareness λ^i when others are realists ($\lambda^j = 1$) or deniers ($\lambda^j = 0$); arrows indicate the shift between the two. The solid line defines the social equilibrium.

(c) $\lambda^i \in (0,1)$ is the unique solution to $\Psi(\lambda^i, s | \lambda^{-i}) = 0$ for $\Psi(0, s | \lambda^{-i}) < 0 < \Psi(1, s | \lambda^{-i})$, which corresponds to $\underline{s}(\lambda^{-i}) < s < \overline{s}(\lambda^{-i})$.

This best response to how others think is illustrated by the dashed curves in Figures 2-3, as a function of either s or c, which have opposite effects. Variations in s provide more transparent intuitions (e.g., s = 0 is the classical benchmark), whereas variations in c are directly observable and experimentally manipulable. All results are therefore stated in a dual form that covers both approaches.

Lemma 1. (Optimal awareness) For any cognitive strategy λ^{-i} used by other agents, there is a unique optimal awareness rate λ^{i} for agent i:

- (i) $\lambda^i = 1$ for s up to a lower threshold $\underline{s}(\lambda^{-i}) > 0$, λ^i is strictly decreasing in s between $\underline{s}(\lambda^{-i})$ and an upper threshold $\overline{s}(\lambda^{-i}) > \underline{s}(\lambda^{-i})$, and $\lambda^i = 0$ for s above $\overline{s}(\lambda^{-i})$.
- (ii) Similarly, $\lambda^i = 0$ for c below a threshold $\underline{c}(\lambda^{-i})$, λ^i is strictly increasing in c between $\underline{c}(\lambda^{-i})$ and a threshold $\overline{c}(\lambda^{-i}) > \underline{c}(\lambda^{-i})$, and $\lambda^i = 0$ for c above $\underline{c}(\lambda^{-i})$.

As one would expect, the more important anticipatory feelings are to an agent's welfare, and the lower the cost of mistakes, the more bad news will be repressed. The next result brings to light the key insight concerning the *social* determinants of wishful thinking.

Proposition 1. (MAD principle) (i) An agent's degree of realism λ^i decreases with that of others, λ^{-i} , (substitutability) if $\theta_L > 0$, and increases with it (complementarity) if $\theta_L < 0$. (ii) λ^i increases with the degree of spillovers $1 - \alpha$ if $\theta_L > 0$, and decreases if $\theta_L < 0$.

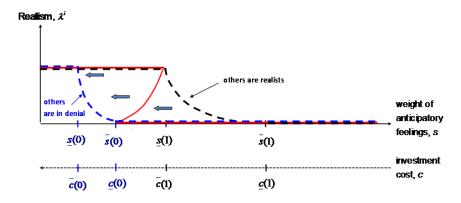


Figure 3: Groupthink ($\theta_L < 0$). The dashed lines give agent *i*'s optimal awareness λ^i when others are realists ($\lambda^j = 1$) or deniers ($\lambda^j = 0$); arrows indicate the shift between the two. The solid lines define the social equilibria.

The intuition for what I shall term the "Mutually Assured Delusion" (MAD) principle is simple. If others' blindness to bad news leads them to act in a way that is better for an agent than if they were well informed ($\theta_L > 0$), it makes those news not as bad, thus reducing his own incentive to engage in denial. But if their avoidance of reality makes things worse than if they reacted appropriately to the true state of affairs ($\theta_L < 0$), future prospects become even more ominous, increasing the incentive to look the other way and take refuge in wishful thinking. In the first case, individual's ways of thinking are strategic substitutes, in the latter they are strategic complements. It is worth emphasizing that this "psychological multiplier", less than 1 in the first case and greater in the second, arises even though agents' payoffs are separable and there is no scope for social learning.

Proposition 1 shows that the scope for contagion hinges on whether overoptimism has positive or negative spillovers. Examples of both types of interaction are provided below, using financial institutions as the main illustration.

• Limited-stakes projects, public goods: $\theta_L > 0$. The first scenario characterizes activities with limited downside risk, in the sense that pursuing them remains socially desirable for the organization even in the low state where the private return falls short of the cost. This corresponds for instance to a bank's employees issuing "plain vanilla" mortgages or lending to safe, brick-and mortar companies –activities that remain generally profitable even in a mild recession, though less so than in a boom. Other areas in which an individual's motivation and "can-do" optimism is always valuable to others include team sports, political mobilization and other forms of good citizenship.

• High-stakes projects: $\theta_L < 0$. The second scenario corresponds to ventures in which the downside is severe enough that persisting has negative social value for the organization. The archetype is a firm like Enron, Lehman Brothers, Citigroup or AIG, whose high-risk strategy could be either extremely profitable (state H) or dangerously misguided (state L), in which case most stakeholders are likely to bear heavy losses: layoffs, firm bankruptcy, evaporated stock values, pensions and reputations, costly lawsuits or even criminal prosecution.

In such contexts, the greater is other players' tendency to ignore danger signals about "tail risk" and forge ahead with the strategy –accumulating yet more subprime loans and CDO's on the balance sheet, increasing leverage, setting up new off-the-books partnerships—the deeper and more widespread the losses will be if the scheme was flawed, the assets "toxic", or the accounting fraudulent. Therefore, when red flags start mounting, the greater is the temptation for everyone whose future is tied to the firm's fate to also look the other way, engage in rationalization, and "not think about it".²¹

The proposition's second result shows how cognitive interdependencies (of both types) are amplified, the more closely tied an individual's welfare is to the actions of others.²² Groupthink is thus most important for closed, cohesive groups whose members perceive that they largely share a common fate and have few exit options. This is in line with Janis' (1972) findings, but with a more operational notion of "cohesiveness", $1 - \alpha$. Such vesting can be exogenous or arise from a prior choice to join the group, in which case wishful beliefs about its future prospects also correspond to ex-post rationalizations of a sunk decision.²³

2.3. Social cognition

I now solve for a full social equilibrium in cognitive strategies, looking for fixed points of the mapping $\lambda^{-i} \to \lambda^i$. The main intuition stems from Proposition 1 and is illustrated by the solid lines in Figures 2 and 3. From (10)-(11), $\lambda = 1$ is an equilibrium (realism is the best response to realism) for $s \leq \underline{s}(1)$, and similarly $\lambda = 0$ is an equilibrium (denial is the best

²¹Enron's employees, whose pension portfolios had on average 58% in company stock, could have moved out at nearly any point, but most never did (Samuelson (2001)). At Bears Stearns, 30% of the stock was held until the last day by employees –with presumably good access to diversification and hedging instruments– who thus lost their capital together with their job. The pattern was similar at many other financial institutions.

²²This intuition is reflected in (9), through the term $(1 - \alpha) \lambda^{-i} \theta_L$. A lower α also increases the cost of suboptimal effort when $\theta_L > 0$ and raises it when $\theta_L < 0$, reinforcing this effect (term $c - \alpha (\delta + s) \alpha \theta_L$).

²³Such a prior investment stage is modeled in Section 4, in the context of asset markets.

response to denial) for $s \geq \bar{s}(0)$, where

(12)
$$\underline{s}(1) = \frac{m/\delta + c - \delta\alpha\theta_L}{\theta_H},$$

(13)
$$\bar{s}(0) = \frac{m/\delta + c - \delta\alpha\theta_L}{\alpha\theta_L + q\Delta\theta}.$$

When $\theta_L > 0$ (cognitive substitutes), $\underline{s}(\lambda^{-i})$ and $\overline{s}(\lambda^{-i})$ are both decreasing in λ^{-i} , so $\underline{s}(1) < \overline{s}(0)$ and the two pure equilibria correspond to distinct ranges. When $\theta_L < 0$ (cognitive complements), on the other hand, both thresholds are increasing in λ^{-i} , and if that effect is strong enough one can have $\overline{s}(0) < \underline{s}(1)$, creating a range of overlap.

Proposition 2. (Groupthink) (i) If the following condition holds,

$$(14) \qquad (1-q)\left(\theta_H - \theta_L\right) < (1-\alpha)\left(-\theta_L\right),\,$$

then $\bar{s}(0) < \underline{s}(1)$ and for any s in this range, both realism $(\lambda = 1)$ and collective denial $(\lambda = 0)$ are equilibria, with an unstable mixed-strategy equilibrium in between. Under denial agents always choose $e^j = 1$, even when it is counterproductive.

- (ii) If (14) is reversed, $\underline{s}(1) < \overline{s}(0)$. The unique equilibrium is $\lambda = 1$ to the left of $(\overline{s}(1), \underline{s}(0))$, a declining function $\lambda(s)$ inside the range, and $\lambda = 0$ to the right of it.
- (iii) The same results characterize the equilibrium set as a function of c, with a nonempty range of multiplicity $[\bar{c}(1), \underline{c}(0)]$ if and only if (14) holds.

Equation (14) reflects the MAD principle at work. The left-hand side is the basic incentive to think that actions are highly productive (θ_H rather than θ_L) when there are no spillovers ($\alpha = 1$) or, equivalently, fixing everyone else's behavior at e = 1 in both states. The right-hand side corresponds to the expected losses –relative to what the correct course of action would yield– inflicted on an agent by others' delusions, and which he can (temporarily) avoid recognizing by denying the occurrence of the bad state altogether. These endogenous losses, which transform reality from second best to third best, must be of sufficient importance relative to the first, unconditional, motive for denial.

• Comparative statics. The proposition also yields several testable predictions. First, there is the stark reversal in how agents respond to others' beliefs (or actions) depending

on the sign of θ_L . Second, complete comparative statics on the equilibrium set are obtained. Focusing on the more interesting case where (14) holds:

- (a) The more vested in the group outcome are its members, the more likely is collective denial—a form of escalating commitment: as $1-\alpha$ increases, both $\bar{s}(0)$ and $\underline{s}(1)$ decrease (since $\theta_L < 0$) and therefore so do the highest and lowest equilibrium values of λ . In particular, it is easy to find (Corollary 1 in online Appendix C) a range of parameters for which an isolated agent never self-deceives, but when interacting with others, all of them always do so.
- (b) A more desirable high state θ_H has the same effects. A more likely one (higher q) also lowers the equilibrium threshold for $\lambda = 0$, but leaves that for $\lambda = 1$ unchanged; consequently, it expands the range where multiplicity occurs.
- (c) A worse low state θ_L has two effects. First, the private cost of a wrong decision rises, making a realistic equilibrium easier to sustain as there is no harmful delusion of others to "escape from": $\underline{s}(1)$ increases. When others are in denial, however, a lower θ_L also worsens the damage they do.²⁴ If $1/\alpha 1/q$ is small this effect is dominated by the previous one, so s(0) increases: sufficiently bad news will force people to "snap out" of collective delusion. With closely tied fates or high priors $(1/\alpha 1/q)$ large enough), on the other hand, the "scaring" effect dominates. Thus $\bar{s}(0)$ decreases, the range of multiplicity widens, and a worsening of bad news can now cause a previously realistic group to take refuge in groupthink.
 - *Implications*. The types of enterprises most prone to collective delusions are thus:
- (a) Those involving new and complex technologies or products that combine a generally profitable upside with a lower-probability but potentially disastrous downside –a "black swan" event. High-powered incentives, such as performance bonuses affected by common market uncertainty, have similar effects, as do highly leveraged investments that put the firm at risk of bankruptcy.
- (b) Those in which participants have only *limited exit options* and, consequently, a lot riding on the soundness or folly of other's judgements. Such dependence typically arises from irreversible or illiquid *sunk investments*: specific human capital, company pension plan, professional reputation, etc. Alternatively, it could reflect the large-scale public good nature of the problem: state of the economy, quality of the government or other society-wide

 $^{^{24}}$ From (13), $sgn\{\partial \bar{s}(0)/\partial \theta_L\} = sgn\{1/\alpha - 1/q - \delta \theta_H/(m/\delta + c)\}$, with $1/\alpha - 1/q > 0$ by (14).

institutions which a single individual has little power to affect, global warming, etc. ²⁵

Finally, the model shows how a propensity to "can-do" optimism (high s) can be very beneficial at the entrepreneurial stage –starting a business, mobilizing energies around a new project ($\theta_L > 0$)– but turn into a source of danger once the organization has grown and is involved in more high-stakes ventures (e.g., a mean-preserving spread in θ , with $\theta_L < 0$).²⁶

2.4. Asymmetric roles: hierarchies and corporate culture

I now relax all symmetry assumptions, as well as the state-invariance of payoffs to "inaction" (e = 0). I then use this more general framework to show how, in hierarchical organizations, cognitive attitudes will "trickle down" and subordinates follow their leaders into realism or denial. Let the payoff structure (1) be extended to

(15)
$$U_2^i \equiv \sum_{j=1}^n \left(a_{\sigma}^{ji} e^j + b_{\sigma}^{ji} (1 - e^j) \right), \text{ for all } i = 1, \dots n \text{ and } \sigma \in \{H, L\}.$$

Each agent j's choice of $e^j = 1$ thus creates a state-dependent value a^{ji}_{σ} for agent i, while $e^j = 0$ generates value b^{ji}_{σ} ; for i = j, these correspond to agent i's private returns to action and inaction. All payoffs remain linearly separable for the same expositional reason as before, but complementarities or substitutabilities are easily incorporated (see Section 7). Agents may also differ in their preference and cognitive parameters c^i, m^i, δ^i , their proclivity to anticipatory feelings s^i or even their priors q^i . The generalization of (3) is then

(16)
$$a_L^{ii} - b_L^{ii} < \frac{c^i}{s^i + \delta^i} < q^i \left(a_H^{ii} - b_H^{ii} \right) + (1 - q^i) \left(a_L^{ii} - b_L^{ii} \right),$$

while that of $\theta_H > \theta_L$ (H is the better state under full information), is

(17)
$$\sum_{i=1}^{n} a_H^{ji} > \sum_{i=1}^{n} b_L^{ji}.$$

²⁵This point is pursued in Bénabou (2008), where I study the dynamics of national ideologies about the relative efficacy of markets and governments in delivering education, health insurance, pensions, etc.

²⁶Similarly, through most of human history collective activities (hunting, foraging, fighting, cultivation) were typically characterized by $\theta_L > 0$, making group morale valuable and susceptibility to optimism (a high s or low m) an evolutionary advantageous trait. (For a related account, see von Hippel and Trivers (2011)). Modern technology and finance now involve many high-stakes activities ($\theta_L << 0 << \theta_H$), for which those same traits can be a source of trouble. With leverage, for instance, payoffs become $\theta'_H \equiv \theta_H + B(\theta_H - R)$ and $\theta'_L \equiv \theta_L + B(\theta_L - R)$, where B is borrowing and $R \in (\theta_L, \theta_H)$ the gross interest rate.

Following the same steps as in the symmetric case and denoting Λ^{-i} the vector of other agents' strategies, it is easily seen that agent *i*'s best response λ^{i} is similar to that in Lemma 1, but with the cutoffs for realism and denial now given by

(18)
$$\underline{s}^{i}(\Lambda^{-i}) \equiv \frac{m^{i}/\delta^{i} + c^{i} - \delta^{i} \left(a_{L}^{ii} - b_{L}^{ii}\right)}{\sum_{j=1}^{n} \left(a_{H}^{ji} - a_{L}^{ji}\right) + \sum_{j \neq i} \lambda^{j} \left(a_{L}^{ji} - b_{L}^{ji}\right) + a_{L}^{ii} - b_{L}^{ii}},$$

(19)
$$\bar{s}^{i}(\Lambda^{-i}) \equiv \frac{m^{i}/\delta^{i} + c^{i} - \delta^{i} (a_{L}^{ii} - b_{L}^{ii})}{q \left[\sum_{j=1}^{n} \left(a_{H}^{ji} - a_{L}^{ji} \right) + \sum_{j \neq i} \lambda^{j} \left(a_{L}^{ji} - b_{L}^{ji} \right) \right] + a_{L}^{ii} - b_{L}^{ii}}.$$

Thus λ^i is (weakly) increasing in λ^j , representing cognitive complementarity, whenever $a_L^{ji} - b_L^{ji} < 0$, meaning that j's delusions (leading to $e^j = 1$ when $\sigma = L$) are harmful to i; conversely, $a_L^{ji} - b_L^{ji} > 0$ leads to substitutability. This is a bilateral version of the MAD principle. Similarly, agent i is more likely to engage in denial when surrounded by deniers $(\lambda^j \equiv 0)$ than by realists $(\lambda^j \equiv 1)$ if and only if $\sum_{j=1}^n (a_L^{ji} - b_L^{ji}) < 0$, meaning that others' mistakes are harmful on average, and generalizing $\theta_L < 0$. Multiple equilibria occur when this (expected) loss is sufficiently large relative to the "unconditional" incentive to deny:

(20)
$$(1-q)\sum_{i=1}^{n} \left(a_{H}^{ji} - a_{L}^{ji}\right) < \sum_{i \neq i} \left(b_{L}^{ji} - a_{L}^{ji}\right),$$

which clearly generalizes (14).

Proposition 3. (Organizational cultures) Let (16)-(20) hold for all i = 1, ... n. There exists a non-empty range $[\bar{s}^i(0), \underline{s}^i(1)]$ (respectively, $[\bar{c}^i(1), \underline{c}^i(0)]$) for each i, such that if $(s^1, ... s^n) \in \Pi_{i=1}^n [\bar{s}^i(0), \underline{s}^i(1)]$ (respectively, if $(c^1, ... c^n) \in \Pi_{i=1}^n [\bar{c}^i(1), \underline{c}^i(0)]$) both collective realism $(\lambda^i \equiv 1)$ and collective denial $(\lambda^i \equiv 0)$ are equilibria.²⁷

• Directions of cognitive influence. Going beyond multiplicity, interesting results emerge for organizations in which members play asymmetric roles. Thus, (18)-(19) embody the intuition that an agent's way of thinking is most sensitive to how the people whose decisions have the greatest impact on his welfare (in state L) deal with unwelcome news:²⁸

²⁸This condition is ensured in particular when $|a_L^{ij} - b_L^{ij}| \ll |a_L^{ii} - b_L^{ii}|$ and $b_L^{ji} - a_H^{ji} > \gg \max\{\sum_{k \neq i,j} |a_L^{ki} - b_L^{ki}|, |a_L^{ii} - b_L^{ii}|, \sum_{j=1}^n |a_H^{ji} - a_L^{ji}|\}$.

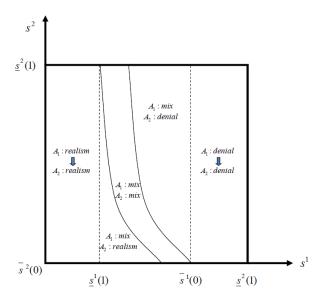


Figure 4: "Trickle down" of realism and denial in a hierarchy. The equilibrium strategies of manager (A_1) and worker(s) (A_2) are indicated in each region, with the arrows illustrating complete top-down determination.

$$(21) \quad \frac{\partial \underline{s}^{i}}{\partial \lambda^{j}} >> \left| \frac{\partial \underline{s}^{j}}{\partial \lambda^{i}} \right| \text{ and } \frac{\partial \overline{s}^{i}}{\partial \lambda^{j}} >> \left| \frac{\partial \overline{s}^{j}}{\partial \lambda^{i}} \right| \quad \text{iff} \quad \frac{b_{L}^{ji} - a_{L}^{ji}}{\left| b_{L}^{ij} - a_{L}^{ij} \right|} >> \max \left\{ \left(\frac{\underline{s}^{j}}{\underline{s}^{i}} \right)^{2}, \left(\frac{\overline{s}^{j}}{\overline{s}^{i}} \right)^{2} \right\}.$$

Consider, for instance, the simplest form of hierarchy: two agents, 1 and 2, such as a manager and worker. If $a_L^{12} - b_L^{12}$ is sufficiently negative while $|a_L^{21} - b_L^{21}|$ is relatively small, agent 2 suffers a lot when agent 1 loses touch with reality, while the converse is not true. Workers thus risk losing their job if management makes overoptimistic investment decisions, whereas the latter has little to lose if workers put in more effort than realistically warranted. When the asymmetry is sufficiently pronounced it leads to a testable pattern of predominantly top-down cognitive influences, illustrated in Figure 4.

Proposition 4. (Cognitive trickle-down) There exists a nonempty range of parameters such that $[\underline{s}^1(1), \overline{s}^1(0)] \subset [\overline{s}^2(0), \underline{s}^2(1)] \equiv S$ and, for all $(s^1, s^2) \in S \times S$, the equilibrium is unique and such that:

- (i) The qualitative nature of the manager's cognitive strategy –complete realism, complete denial, or mixing– depends only on her own s^1 , not on the worker's s^2 .
- (ii) If the manager behaves as a systematic denier (respectively, realist), so does the worker: where $\lambda^1 = 1$ it must be that $\lambda^2 = 1$, and similarly $\lambda^1 = 0$ implies $\lambda^2 = 0$.
- (iii) Only when both agents are in partial denial (between the two curves in Figure 4) does

the worker's degree of realism also influence that of the manager.

Let agent 2 now be replicated into n-1 identical workers, each with influence $[a_{\sigma}^{j1}e^{j}+b_{\sigma}^{j1}(1-e^{j})]/(n-1)$ over the manager, but subject to the same influence from him as before, $a_{\sigma}^{1j}e^{1}+b_{\sigma}^{1j}(1-e^{1})$. Figure 4 then remains operative, showing how the leader's attitude toward reality tends to spread to all his subordinates, while being influenced by theirs only in a limited way, and over a limited range.

This result has clear applications to corporate and bureaucratic culture, explaining how people will contagiously invest excessive faith in a leader's "vision".²⁹ Likewise in the political sphere, a dictator need not exert constant censorship or constraint to implement his policies, as crazy as they may be: he can rely on people's mutually reinforcing tendencies to rationalize as "not so bad" the regime they (endogenously) have to live with.

The above is of course an oversimplified representation of an organization; yet the same principles will carry over to more complex hierarchies with multiple tiers (by "chaining" condition (21) across levels i, j, k, etc.), strategic interactions, control rights, transfer payments, etc. Such extensions lie outside the scope of this paper and are left to future work.

3. Welfare, Cassandra's curse and free speech protections

Are members of a group in collective denial worse or better off than if they faced the truth –as an alternative equilibrium or by means of some collective commitment mechanism? I adopt here the ex-ante, behind-the-veil perspective of organizational designers who could choose the structure of payoffs (activities, incentives, employees' types) and information (hard or soft signals, treatment of dissenters) to maximize total surplus. Computing welfare as of t=0 is also consistent with a revealed-preferences approach: from agents' willingness-to-pay to ensure collective realism or denial, inferences can be made about their deep preferences

²⁹In Rotemberg and Saloner (1993), a manager's "vision" (prior beliefs or preferences favoring some activities over others) serves as a commitment device to reduce workers' concerns about ex-post expropriation of their innovations. In Prendergast (1993), a manager's use of subjective performance evaluations to assess subordinates' effort at seeking information leads them to distort their reports in the direction of his (expected) signal. In neither model do workers actually espouse the manager's beliefs, nor would he ever want them to report anything but the truth. In Hermalin (1998), a team leader with private information about the return to effort works extra-hard to motivate his coworkers; the resulting separating equilibrium raises all effort levels, but involves no mistaken belief. In Van den Steen (2005), agents with diverse priors do not learn but instead sort themselves through the labor market. Managers with a strong "vision" thus tend to attract employees with similar priors, as this helps alleviate incentive and coordination problems within the firm.

parameters, such as $s.^{30}$

Focusing for simplicity on the symmetric specification of Section 2.1, consider first state $\sigma = L$. When agents are realists (setting $\lambda^j = 1$ in (7)), equilibrium welfare is $U_{L,R}^* = 0$. When they are deniers (setting $\lambda^j = 0$ in (8)), it is given by:

$$(22) U_{L,D}^*/\delta = -m - c + \delta\theta_L + sq\theta_H + s(1-q)\theta_L.$$

As illustrated in Figure 5, whether collective denial of bad news is harmful or beneficial thus depends on whether s lies below or above the threshold

(23)
$$s^* \equiv \frac{m/\delta + c - \delta\theta_L}{q\theta_H + (1 - q)\theta_L}.^{31}$$

Proposition 5. Welfare following bad news (state L):

(1) If $\theta_L < 0$, then $s^* > \max\{\bar{s}(0), \underline{s}(1)\}$. Whenever realism $(\lambda = 1)$ is an equilibrium, it is superior to denial $(\lambda = 0)$. Moreover, there exists a range in which realism is not an equilibrium but, if it can be achieved through collective commitment, yields higher welfare.

(2) If $\theta_L > 0$, then $s^* < \bar{s}(0)$. The equilibrium involves excessive realism for $s \in (s^*, \bar{s}(0))$ and excessive denial for $s \in (\underline{s}(1), s^*)$, when this interval is nonempty.

Given how damaging collective delusion is in state L with $\theta_L < 0$, it makes sense that when realism can also be sustained as an equilibrium it dominates, and that when it cannot the group may try to commit to it. Conversely, with $\theta_L > 0$, boosting morale in state L ameliorates the free-rider problem, so the group would want to commit to ignoring adverse signals when $s \geq s^*$ but the only equilibrium involves realism.³²

Consider now welfare in state H. Given (3), everyone chooses $e^i = 1$ in both equilibria. Under denial, however, agents can never be sure of whether the state is truly H, or it was really L and they censored the bad news. As a result of this "spoiling" effect, welfare is only

(24)
$$U_{H,D}^*/\delta = -c + \delta\theta_H + s \left[q\theta_H + (1-q)\theta_L \right] < -c + (\delta + s)\theta_H = U_{H,R}^*/\delta.$$

 $^{^{30}}$ One may nonetheless ask what would change if welfare was evaluated based on U_1^i rather than U_0^i (though it would then not be measurable through organizational-design decisions). This turns out to make no difference, apart from a trivial parameter renormalization: see footnote 33.

 $^{^{32}}$ If θ_L is high enough that $\delta\theta_L > c + m/\delta$, then $s^* < 0$: overoptimism in state L is socially beneficial even absent anticipatory emotions (s = 0). A good example is team morale in sports.

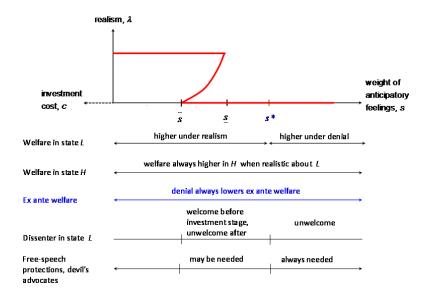


Figure 5: Welfare and dissenting speech (groupthink case)

Averaging over the two states, finally, the mean belief about θ remains fixed (by Bayes' rule), so the net welfare impact of denial, $\Delta W_0 \equiv q \left(U_{H,D}^* - U_{H,R}^* \right) + (1-q) \left(U_{L,D}^* - U_{L,R}^* \right)$, is just

(25)
$$\Delta W_0 \equiv (1 - q)\delta \left[(\delta + s) \theta_L - c - m/\delta \right],$$

realized in state L. In assessing the overall value of social beliefs one can thus focus on material outcomes and ignore anticipatory feelings, which are much more difficult to measure but wash out across states of nature.³³

Proposition 6. (1) Welfare following good news (state H) is always higher, the more realistic agents are when faced with bad news (the higher is λ).

(2) If $\theta_L \leq 0$, denial always lowers ex-ante welfare. If $\theta_L > 0$, it improves it if and only if $(\delta + s) \theta_L > c + m/\delta$.

These results, also illustrated in Figure 5, lead to a clear distinction between two types of collective beliefs and the settings that give rise to them.³⁴

³³This is also true when evaluating (unconditional) utilities from the point of view of date 1. The welfare differential across denial and realistic group outcomes is then $\Delta W_1 = (1-q) \left[(\delta+s)\theta_L - c \right]$, which just amounts to renormalizing c to $c+m/\delta$ in $\Delta W_0/\delta$. Furthermore, m can be taken (if desired) as arbitrarily small or even zero; see footnote 15.

 $^{^{34}}$ They are also testable, since ΔW_0 measures agents' willingness to pay (positive or negative) for organizational designs or commitment devices that ensure collective realism.

- Valuable group morale. When $\theta_L > 0$, e = 1 is socially optimal even in state L, but since $\alpha(s+\delta)\theta_L < c$ it is not privately optimal. If agents can all manage to ignore bad news at relatively low cost, either as an equilibrium or through commitment, they will be better off not only ex-post but also ex-ante: $\Delta W_0 > 0$. This is in line with other results on the value of overoptimism in settings where agents with correct beliefs would underprovide effort.
- Harmful groupthink. The novel case is the one in which contagious delusions can arise, $\theta_L < 0$, and it also leads to a more striking conclusion: not only can such reality avoidance greatly damage welfare in state L, but even when it improves it those gains are always dominated by the losses induced in state $H: \Delta W_0 < 0.35$ This normative result also has positive implications for how organizations and polities deal with dissenters, revealing an important form of time inconsistency between ex ante and ex post attitudes.
- The curse of Cassandra. Let $\theta_L < 0$ and consider a denial equilibrium, as in Figure 5. Suppose now that, in state L, an individual or subgroup with a lower s or different payoffs attempts to bring the bad news back to everyone's attention. If this occurs after agents have sunk in their investments it simply amounts to deflating expectations in (2), so they will refuse to listen, or may even try to "kill the messenger" (pay a new cost to forget). Anticipating that others will behave in this way, in turn, allows everyone to more confidently invest in denial at t = 0. To avoid this deleterious outcome, organizations and societies will find it desirable to set up ex-ante guarantees such as whistle-blower protections, devil's advocates, constitutional rights to free speech, independence of the press, etc. These will ensure that bad news will most likely "resurface" ex-post in a way that is hard to ignore, thus lowering the ex-ante return of investing in denial.

Similar results apply if the dissenter comes at an interim stage, after people have censored but before investments are made. For $s < s^*$ they should welcome the opportunity to correct course, but in practice this can be hard to achieve, requiring full coordination. With payoff heterogeneity, dissenters' motives may also be suspect. Things are even starker for $s > s^*$, meaning that people strongly value hope and dislike anxiety. Facing the truth

³⁵The "shadow of doubt" cast over the good state by the censoring of the bad state could also distort some decisions in state H, given more than two action choices. If, on the other hand, agents are less than fully aware of their own tendency to self deception, the losses in state H are attenuated and ex-ante gains become possible. Thus, with $\chi < 1$ in (6), q is simply replaced by $q/[q + \chi(1-q)]$ in (22) and (24), and ΔW_0 consequently augmented by $s\delta(1-\chi)q(1-q)/[q+\chi(1-q)]$.

(state L) now lowers everyone's utility, generating a universal unwillingness to listen —the curse of Cassandra. Free-speech guarantees, anonymity and similar protections nonetheless remain desirable ex-ante, as they avoid welfare losses in state H and, on average, save the organization or society from wasting resources on denial and repression.

4. Market exuberance

4.1. The dynamics of manias and crashes

I now consider delusions in asset markets. To take recent examples, state H may correspond to a "new economy" in which high-tech startups will flourish and their prospects are best assessed using "new metrics"; to a long-term rise in housing values; or to any other positive and lasting shift in fundamentals. Conversely, state L would reflect an inevitable return to "old" economy valuations, the unsustainability of many adjustable-rate mortgages, no-docs loans and other subprime debt, or the presence of extensive fraud. Investors finding reasons to believe in H even as evidence of L accumulates corresponds to what Shiller (2005) terms "new-era thinking", and of which he relates many examples. This section will provide the first analytical model of this phenomenon.³⁶

To this end, I extend the basic framework in two ways, adding an ex-ante investment stage and deriving final payoffs from market prices: see Figure 6.³⁷ A continuum of firms or investors i can each produce $k^i \leq K$ units of a good or asset (housing, office space, mortgage-backed security, internet startup) in period 0 and an additional $e^i \leq E$ units in period 1, where K and E reflect capacity constraints or "time to build" technological limits. The cost of production in period 0 is set to 0 for simplicity, while in period 1 it is equal to c. All units are sold at t = 2, at which time the expected market price $P_{\sigma}(Q)$ will reflect total supply $Q \equiv \bar{k} + \bar{e} \in [0, K + E]$ and stochastic market conditions θ_{σ} , with $\sigma = H, L$ and $P'_{\sigma}(Q) < 0$. Between the two investment phases agents all observe the signal σ , then decide how to process it, with the same information structure and preferences as before.

The absence of an interim or futures market before date 2 is a version (chosen for simplicity) of the kind of "limits to arbitrage" commonly found in the finance literature. Specifically,

³⁶As discussed in Section 6, neither rational bubbles nor informational cascades involve any element of wishful thinking, motivated rationalization or information avoidance.

³⁷The initial investment stage is an example of endogenizing the degree (previously, $1 - \alpha$) of agents' interdependence or "vesting" in the collective outcome.

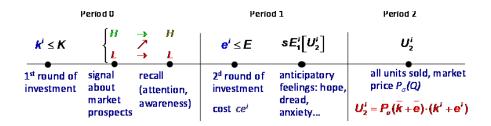


Figure 6: The market game

I assume that: (i) goods produced in period 0 cannot be sold before period 2, for instance because they are still work-in-progress whose quality or market potential is not verifiable: startup company, unfinished residential development or office complex, new type of financial instrument, etc.; (ii) short sales are not feasible.

Limited liquidity and arbitrage are empirically descriptive of the types of markets which the model aims to analyze.³⁸ In the recent financial crisis, a dominant fraction of the assets held by major U.S. investment banks did not have an active trading market and objective price, but were instead valued according to the bank's own models and projections, or even according to management's "best estimates".³⁹ Similarly, the notional value of outstanding Collateralized Debt Obligation (CDO) tranches stood in 2008 at about \$2 trillion worldwide, and that of Credit Default Swaps (CDS) at around \$50 trillion; and yet for most of them there was and still is no established, centralized marketplace where they could easily be traded. These are instead very illiquid ("buy and hold") and hard-to-price assets: originating in private deals, highly differentiated and exchanged only over-the-counter.⁴⁰

Suppose that, ex-ante, the market is sufficiently profitable that everyone invests up to capacity at the start of period $0: k^j = \bar{k} = K$.⁴¹ Moreover, following (3), let

$$P_L(K) < \frac{c}{s+\delta} < \frac{c}{\delta} < qP_H(K+E) + (1-q)P_L(K+E).$$

³⁸Shiller (2003) cites several studies documenting the fact that short sales have never amounted to more than 2% of stocks, whether in number of shares or value. Gabaix et al. (2007) provide specific evidence of limits to arbitrage in the market for mortgage-backed securities.

³⁹Reilly (2007) reports that only 36% of Lehman Brothers' 2007-QII balance sheet and 18% of Bear Stearns' were Level 1 assets in the FASB nomenclature, namely those which "trade in active markets with readily available prices". Level 2 assets ("mark to model") accounted for 56% and 74% respectively, and Level 3 ("reflect management's best estimates of what market participants would use in pricing the assets") for 8% in both cases. For Level 2, moreover, the major trading houses commonly used computer programs designed for "plain vanilla" loans to value novel and highly complex securities (Hansell, (2008)).

⁴⁰In housing, the market for regional-index futures (Case-Shiller) is also still small and fairly illiquid.

⁴¹The optimality of this first-stage strategy (given expected equilibrium profits in both states) is formally proved in online Appendix C.

It is thus a dominant strategy for an agent at t = 1 to invest the maximum $e^i = E$ if his posterior is no worse than the prior q, and to abstain if he is sure that the state is L.

Consider now what unfolds when agents observe the signal L at the end of period 0.

• Realism. If market participants acknowledge and properly respond to bad news ($\lambda^{j} \equiv 1$) they will not invest further at t = 1, so the price at t = 2 will be $P_{L}(K)$. For an individual investor i with stock k^{i} , the net effect of ignoring the signal is then

(26)
$$U_{0,D}^{i} - U_{0,R}^{i} = -m + \delta \left[(\delta + s) P_{L}(K) - c \right] E + \delta sr(\lambda^{i}) \left[P_{H}(K + E) - P_{L}(K) \right] (k^{i} + E).$$

The second term reflects the expected losses from investing at t=1, while the last one represents the value of maintaining hope that the market is strong or will eventually recover, in which case total output will be K+E and the price $P_H(K+E)$. Realism is an equilibrium if $U_{0,D}^i \leq U_{0,R}^i$ for $\lambda^i = 1$ and $k^i = K$, or

(27)
$$s \leq \frac{m/\delta + [c - \delta P_L(K)] E}{[P_H(K+E) - P_L(K)] (K+E) + P_L(K)E} \equiv \underline{s}(1).$$

• Denial. If the other participants remain bullish in spite of adverse signals, they will keep investing at t = 1, causing the already weak market to crash: at t = 2, the price will fall to $P_L(K + E) < P_L(K)$. The net value of denial for investor i is now

(28)
$$U_{0,D}^{i} - U_{0,R}^{i} = -m + \delta \left[(\delta + s) P_{L}(K + E) - c \right] E + \delta s r(\lambda^{i}) \left[P_{H}(K + E) - P_{L}(K + E) \right] (k^{i} + E).$$

In the second term, the expected losses from overinvestment are higher than when other participants are realists. Through this channel, which reflects the usual *substitutability* of investments in a market interaction, each individual's cost of delusion increases with others' exuberance. The third term makes clear, however, that the psychological value of denial is also greater, since acknowledging the bad state now requires *recognizing an even greater capital loss* on preexisting holdings. This is again the MAD principle at work.

Denial is an equilibrium if $U_{0,D}^i \geq U_{0,R}^i$ for $\lambda^i = 0$ and $k^i = K$, or

(29)
$$s \ge \frac{m/\delta + [c - \delta P_L(K+E)] E}{q [P_H(K+E) - P_L(K+E)] (K+E) + P_L(K+E)E} \equiv \bar{s}(0).$$

In such an equilibrium, each investor keeps optimistically accumulating assets that have in fact become "toxic", both to his *own* balance sheet and to the *market* at large.

When does other participants' exuberance make each individual more likely to also be exuberant? Intuitively, contagion occurs when the substitutability effect, which bears on the marginal units E produced in period 1, is dominated by the capital-loss effect on the outstanding position K inherited from period 0. Formally, $\bar{s}(0) < \underline{s}(1)$ requires that K be large enough relative to E, though not so large as to preclude (27).

Proposition 7. (Market manias and crashes) If

(30)
$$P_H(K+E)(1+E/K) < c/\delta < P_H(K+E),$$

there exists $q^* < 1$ such that, for all $q \in [q^*, 1]$, there is a non-empty interval for s (or c) in which both realism and evidence-blind "exuberance" are equilibria, provided m is not too large. Contagious exuberance leads to overinvestment, followed by a deep crash.

The model provides a microfounded and psychologically-based account of market group-think, investment frenzies and ensuing crashes.⁴² It also identifies key features of the markets prone to such cycles, distinguishing it from traditional models of bubbles or herding.

First, there must be a "story" about shifts in fundamentals that is minimally plausible a priori (q must not be too low): technology, demographics, globalization, etc. The key result is that investors's beliefs in the story can then quickly become resistant to any contrary evidence.⁴³ Second, when the new opportunity first appears (q rising above the threshold), there is an initial phase of investment buildup and rising price expectations.⁴⁴ Finally, the assets in question must involve both significant uncertainty and limited liquidity. These conditions are typical of assets tied to new technologies or financial instruments, whose potential will take a long time to be fully revealed.

⁴²As explained in Section always, equilibrium multiplicity represents more broadly the potential to greatly amplify small shocks, translating here into a "fragility" of the market to recurrent manias.

⁴³By contrast, in standard models of stochastic bubbles everyone realizes they are trading a "hot potato" whose value does not reflect any fundamentals, must eventually collapse and can do so at any instant. Limited liquidity also plays no role there, nor does it in models of herding.

⁴⁴In the interim period there is no objective market price, but all participants' "mark to model" or "best estimates" values remain at $qP_H(K+E)+(1-q)P_L(K+E)$, which reflects only the increased prior q instead of falling to the very low $P_L(K+E)$ actually warranted by the red flags which they are ignoring ($\sigma = L$). Note also that the most economically important aspect of market manias is not price volatility or mispricing per se but the resulting misallocation of resources, which is what the present analysis focuses on.

The model's comparative statics also shed light on other puzzles. From (26)-(29), we have:

- (a) Escalating commitment at the individual level: the more an agent has invested to date, the more likely he is to continue in spite of bad news, thus displaying a form of the sunk cost fallacy: by (28), $\partial (U_{0,D}^i U_{0,R}^i)/\partial k^i > 0$. Moreover, while k^i represents here an outstanding inventory or financial position, any other illiquid asset with market-dependent value, such as sector-specific human capital in banking or finance, has the same effect.⁴⁵
- (b) Market momentum: the larger the market buildup $(k^{-i} = K)$, the more likely is each agent to continue investing in spite of bad news, if demand is (sufficiently) less price sensitive in the low state than in the high one. Indeed, the incentive to discount bad news rises with prospective capital losses, which in a denial equilibrium are proportional to $P_H(K + E) P_L(K + E)$ and therefore increasing in K when $\partial^2 P/\partial Q\partial\theta > 0$. This occurs for instance with linear demand $Q(P,\theta) = \theta (a bP)$, or when demand is concave and good fundamentals correspond to a scarcity of a close substitute: $P_{\sigma}(Q) = \mathcal{P}(Q + Z(\theta_{\sigma}))$, with $Z', \mathcal{P}', \mathcal{P}'' < 0.46$

This simple asset-market model could be extended in several ways. First, in a dynamic context, outstanding stocks will result stochastically from the combination of previous investment decisions and demand realizations. Second, one could relax the strong form of limits to arbitrage imposed by the assumption that trades occur only at t=2. Forward or short trades could instead involve transactions costs or an adverse price impact due to limited market liquidity.⁴⁷ Finally, instead of ignoring red flags, the contagion analysis could be recast (as in Section 5) in terms of market participants' unwillingness to seriously examine the true nature –investment-grade, or highly "toxic" – of the assets being accumulated.

4.2. Regulators, politicians and economists

Another set of actors with "value at risk" in an exuberant market are politicians and regulators, whose reputation and career will suffer if the disaster scenario (state L, worsened

⁴⁵An initial stake raises the propensity to wishful exuberance, but is not a precondition. Equation (26) or (28) can be positive (for $\lambda^i = 0$) even with $k^i = 0$, given a sufficient sensitivity to anticipatory feelings, s^i .

⁴⁶By (28), $\partial(U_{0,D}^i - U_{0,R}^i)/\partial K|_{e^j = E} > 0$ at $r(\lambda^i) = q$, so that agent i's best response is $\lambda^i = 0$ (and $e^i = E$), if and only if $[P'_H(K+E) - P'_L(K+E)]/[-P'_L(K+E)] > [(\delta+s)/sq][E/(k^i+E)]$. This inequality holds if $\partial^2 P/\partial Q \partial \theta$ is large enough and k^i/E (equal to K/E in equilibrium) high enough that the right-hand side is less than 1. With linear demand, it becomes $(\theta_H - \theta_L)/\theta_H > [(\delta+s)/sq][E/(k^i+E)]$.

⁴⁷Trying to sell (or sell short) in period 1 could also be self-defeating, as it would reveal again to the market that the state is L, generating an immediate price collapse. For a model of how market thinness generates endogenous limits to arbitrage and delays in trade, see Rostek and Weretka (2008).

by market participants' overinvestment) occurs. This should normally make them try to dampen the market's enthusiasm, but if the buildup has proceeded far enough (high K) that large, economy-wide losses are unavoidable in the bad state, they will also become "believers" in a rosy future or smooth landing. Consequently, they will fail to take measures that could have limited (tough not avoided) the damage, thus further enabling the investment frenzy and subsequent crash.⁴⁸ Some academics and policy advisers may also have *intellectual capital* vested in the virtues of unfettered markets: a severe crisis proving such faith to be excessive would damage its value and the general credibility of laissez-faire arguments.

5. Contagious ignorance: the role of risk

In this section I derive versions of the MAD principle and groupthink results that are based on intertemporal risk attitudes rather than anticipatory utility, and where willful blindness takes the form of ex-ante information avoidance (not wanting to know) rather than ex-post belief distortion (reality denial). There are three reasons for doing so. First, as seen earlier, both types of behaviors are observed in experiments and real-world situations. Second, the role of risk in cognitive distortions is of intrinsic interest, and this section can also be read as a stand-alone contribution to the literature on attitudes toward information. Finally, this will make clear that the paper's results are not tied to any particular assumption about the individual motive for non-standard updating, nor the form that the latter takes.⁴⁹ They concern instead the social transmission of beliefs, which a simple and general insight relates to the structure of interactions among agents. In the present case, it implies that willful ignorance will be contagious (complementarity) when its collateral effect is to magnify the risks borne by others, and self-dampening (substitutability) when it attenuates those risks.

• Technology. I use here the general interaction structure of Section 2.4, which will bring to light most clearly the roles played by different types of risks.⁵⁰ For simplicity, all

⁴⁸On serial blindness to red flags and deliberate information-avoidance by FED chairman Greenspan and other top financial regulators, see Goodman (2008), SEC (2008, 2009) and online Appendix D. Ball (2012). points to a likely role of groupthink at the FED in altering chairman Bernanke's views on monetary policy.

⁴⁹The MAD mechanism is robust along many other dimensions, such as nonseparable payoffs, alternative informational structures and limited sophistication (adaptive learning); see online Appendix B.

 $^{^{50}}$ In the restricted symmetric model of Section 2.1, by contrast, parameters such as θ_L or α affect both the variance and mean of payoffs. Thus, while results qualitatively similar to those of Proposition 9 can be obtained, they are not easily interpretable and the conditions required are much more constraining.

payoffs are now received in the last period (t = 2), with⁵¹

(31)
$$a_H^{ii} - b_H^{ii} > 0 > a_L^{ii} - b_L^{ii} \equiv -f_L^i$$

(32)
$$qa_H^{ii} + (1-q)a_L^{ii} > qb_H^{ii} + (1-q)b_L^{ii},$$

(33)
$$d_L^i \equiv \sum_{i \neq i} \left(b_L^{ji} - a_L^{ji} \right) \geqslant 0,$$

(34)
$$A_H^i \equiv \sum_{i=1}^n a_H^{ji} \gtrless \sum_{i=1}^n b_L^{ji} \equiv B_L^i.$$

The first equation specifies that the privately optimal action for agent i is $e^i = 1$ in state H and $e^i = 0$ in state L. The second one implies that when uninformed, a risk-neutral agent will choose $e^i = 1$; if the state turns out to be L, he then incurs a loss of $f_L^i > 0$ (f stands for "fault"). The third equation defines the total impact on agent i that results when everyone else chooses $e^{j} = 1$ in state L, which they will do if uninformed. The most natural case is that where $d_L^i \geq 0$ (so d stands for collateral "damage"), but I also allow $d_L^i < 0$. The last equation compares which of state H or L is better for agent i when everyone is informed; the most plausible case is $A_H^i > B_L^i$, but this is not required for any of the results.

• Preferences. I simply replace the combination of anticipatory preferences and malleable memory used so far with Kreps-Porteus (1978) preferences. Thus, at date 1 agents evaluate final lotteries according to an expected utility function $U_1 = E_1[u(x)]$, and at date 0 they evaluate lotteries over date-1 utilities U_1 according to an expected utility function $E_0[v(U_1)]$. Expectations are now standard rational forecasts (there is no forgetting) and agents' only informational choice is whether or not to learn the signal $\sigma = H, L$ at t = 0. Both options are taken to be costless, but it would be trivial to allow for positive costs of becoming informed or remaining uninformed. For comparability with the previous results I take agents to be risk-neutral at date 1, $u(x) \equiv x$. The function v(x), on the other hand, is strictly concave, generating a ceteris paribus preference for the late resolution of uncertainty. To avoid corner solutions I take v(x) to be defined over all of \mathbb{R} , and for some results will also require (without much loss of generality) that that there exist $\gamma > 1$ and $\gamma' > 1$ such that 52

$$\lim_{x\to +\infty} [v(x)/x^{1/\gamma}] \quad and \quad \lim_{x\to -\infty} [-v(x)/\left(-x\right)^{\gamma'}] \quad are \ well-defined \ and \ positive.$$

Thus a costs incurred in period 1 are thus "folded into" the final payoffs, with appropriate discounting: thus a_H^{ii} corresponds here to $a_H^{ii} - c^i/\delta^i$ in Section 2.4.

The final payoffs, with appropriate discounting: thus a_H^{ii} corresponds here to $a_H^{ii} - c^i/\delta^i$ in Section 2.4.

The final payoffs, with appropriate discounting: a_H^{ii} for a_H^{ii} fo

At t = 0, when deciding whether or not to learn the state of the world, agents face a tradeoff between their preference for late resolution and the decision value of information. The novel feature of the problem considered here is that each one's prospects also depend on how *others* act, and therefore on who else chooses to be informed or remain ignorant.

• The MAD principle for risks. Consider an agent i and let $d \in \mathbb{R}$ parametrize the losses he will incur due to the mistakes of those who choose $e^j = 1$ in state L. Thus $d = \sum_{j \in J} (b_L^{ji} - a_L^{ji}) \geq 0$, where J denotes the uninformed subset. Agent i' final payoffs are given by the lottery $\mathcal{I}(d)$ if he finds out the state at t = 0 and by $\mathcal{N}(d)$ if he does not, where:⁵³

(36)
$$\mathcal{I}(d) \equiv \begin{cases} q: & A_H^i \\ 1 - q: & B_L^i - d \end{cases}, \quad \mathcal{N}(d) \equiv \begin{cases} q: & A_H^i \\ 1 - q: & B_L^i - f_L^i - d \end{cases}.$$

He therefore prefers to remain ignorant if

(37)
$$\varphi^{i}(d) \equiv v \left(q A_{H}^{i} + (1-q) \left(B_{L}^{i} - f_{L}^{i} - d \right) \right) - q v(A_{H}^{i}) - (1-q) v(B_{L}^{i} - d) > 0.$$

Consider first the case in which everyone else is informed or, equivalently, agent i is insulated from their mistakes. Thus d = 0, and he prefers to know the state if

(38)
$$\varphi^{i}(0) = v\left(qA_{H}^{i} + (1-q)\left(B_{L}^{i} - f_{L}^{i}\right)\right) - qv(A_{H}^{i}) - (1-q)v(B_{L}^{i}) < 0.$$

Since v is strictly increasing, this holds when faulty decisions are costly enough,

$$(39) f_L^i > \underline{f}^i,$$

where $f^i > 0$ is defined by equality in (38).

Consider now the role of d: as it rises, (36) makes clear how others' ignorance renders agent i's future more risky, increasing the variance in *both* feasible prospects $\mathcal{I}(d)$ and $\mathcal{N}(d)$. This extra risk, which he cannot avoid, makes finding out whether the state is H or L more scary, and thus reduces his willingness to know. The following results, illustrated in Figure 7, characterize more generally each agent's attitude towards information.

Lemma 2. The function $\varphi^{i}(d)$ is strictly quasiconvex, reaching a negative minimum at

(40)
$$d_*^i \equiv -\left(A_H^i - B_L^i\right) + \left(\frac{1-q}{q}\right) f_L^i,$$

 $[\]overline{}^{53}$ Agents here have a common prior, $q^i = q$, but this can easily be relaxed, as in Proposition 3.

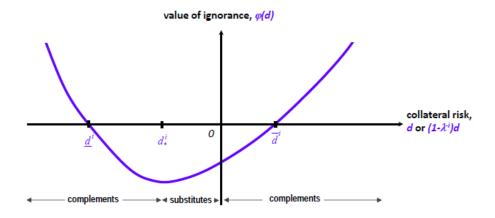


Figure 7: collateral risk and informational decisions

independent of $v(\cdot)$. Furthermore, if $v(\cdot)$ satisfies (35) then $\varphi^i(d) \to +\infty$ as $|d| \to +\infty$, so there exists finite thresholds $\underline{d}^i < d_*^i < \overline{d}^i$ such that $\varphi^i(d) > 0$ if and only if $d \notin [\underline{d}^i, \overline{d}^i]$.

The intuition is clearest when d is positive and relatively large, meaning that others' mistakes impose nontrivial collateral damages in state L; this is also the most empirically relevant case. What matters is payoff risk, however, so information aversion also occurs when others' ignorance has a sufficiently positive payoff—that is, when d is negative enough.⁵⁴ The size of the collateral stakes |d|, or more precisely its contribution to $|d - d_*^i|$, plays here the same role for agents who dislike variance in their date-1 utility U_1^i as d itself (or $-(1-\alpha)\theta_L$ in the symmetric case) played earlier for agents disliking a low level of U_1^i . The term d_*^i corrects in particular for the fact that it is not just the sum of risks that matters, but also their correlation: remaining uninformed leads to a costly mistake (f_L^i) when L occurs, which is also when the agent incurs d from others' ignorance.⁵⁵

These results lead a to full characterization of agents' cognitive best responses.

Proposition 8 (MAD principle for risks). (i) Given any two subsets of agents J and J' not containing i, denote $d = \sum_{j \in J} (b_L^{ji} - a_L^{ji})$ and $d' = \sum_{j \in J'} (b_L^{ji} - a_L^{ji})$. Agent i's incentive

⁵⁴Note also that $\left(\varphi^i\right)'(d) > 0$ on \mathbb{R}_+ as long as $d_*^i < 0$, or equivalently $qA_H^i + (1-q)\left(B_L^i - f_L^i\right) > B_L^i$. This condition is most plausible, as it means that a single risk-neutral agent at date 1 prefers the lottery $\mathcal{N}(0)$ to the degenerate one in which the state is L with probability 1. In the benchmark model of Section 2.1, for instance, $A_H^i = \theta_H - c^i/\delta^i$, $B_L^i = 0$ and $f_L^i = c^i/\delta^i - \alpha\theta_L$, so $d_*^i < 0$ is always implied by (32).

⁵⁵This increases the value of information for d > 0 and lowers it for d < 0, thus raising the threshold d_*^i beyond which higher d's makes the agent less willing to become informed $(\varphi' > 0)$. For $f_L^i = 0$, $|d - d_*^i| = |A_H^i - (B_L^i - d)|$ is just the spread in payoffs common to $\mathcal{I}(d)$ and $\mathcal{N}(d)$. Note also how the opposite roles of avoidable and unavoidable risks are reflected in φ^i , which is concave in f_L^i and quasiconvex in d.

to avoid information is higher when the set of uninformed agents is J' rather than J if and only if $(d'-d)(d-d_*^i) > 0$.

(ii) Let each agent be equally affected by the mistakes of all others: $b_L^{ji} - a_L^{ji} = d$ for all i, j with $j \neq i$. The informational choices of all agents are strategic complements if d lies outside the interval $[\min\{d_*^i, 0\}, \max\{d_*^i, 0\}]$, and strategic substitutes if it lies within.

The first part of the proposition demonstrates the role of collateral risk most generally. First, if $J \subset J'$, more agents remaining ignorant make i more averse to information when they add to the total risk he bears, in the sense of moving d further away from d_*^i . Second, taking J and J' disjoint (for example, i's hierarchical superiors and subordinates, respectively) shows that an agent's wanting or not wanting to know is most sensitive to how the people whose ignorance imposes the greatest risk on him deal with uncertainty. This naturally leads, as in Section 2.4, to a trickle-down of attitudes towards information —from management to workers, political leader to followers, etc.

The second part of the proposition is illustrated in Figure 7 by a simple rescaling of d. In this "horizontal" case the value of ignorance is $\varphi^i((1-\lambda^{-i})d)$, where $1-\lambda^{-i}$ is the fraction of others who choose to remain uninformed and d is now the "normalized" damage.

• Groupthink as contagious ignorance. When the total uncertainty he faces due to the ignorance of others $(d = d_L^i)$ defined in (33) is large enough, an agent who would otherwise have positive demand for information $(f_L^i) = \underline{f}^i$ will prefer to also avoid learning the state of the world. Thus $\varphi^i(0) < 0 < \varphi^i(d_L^i)$, meaning that knowledge is a best reply to knowledge and ignorance a best reply to ignorance, in a manner that echoes Propositions 2 and 3. As a consequence, risk also spreads and becomes systemic throughout the organization.

Proposition 9 (endogenous systemic risk). Let (31), (32) and (39) hold for all i, and $v(\cdot)$ satisfy (35). There exists a non-empty set $D^i \equiv (-\infty, \underline{d}^i) \bigcup (\overline{d}^i, +\infty)$ for each i, with $\underline{d}^i < 0 < \overline{d}^i$, such that if $(d_L^1, \ldots d_L^n) \in \prod_{i=1}^n D^i$, for all i, both collective realism (every agent becoming informed at date 0) and collective willful ignorance (every agent choosing to remain uniformed) are equilibria. In the latter, each agent i's willingness to pay to avoid information is positive and increasing in $|d_L^i|$ on each side of D^i .

• The role of risk preferences. Given a structure of interactions, intuition suggests that for multiple regimes to arise, agents' preference for late resolution should be neither too large nor too small. Indeed, if (37) (respectively, (38)) holds for some function v, it also holds for any w that is increasing and more (respectively, less) concave.⁵⁶

Proposition 10. Let $\{v_{\gamma}(x), \gamma \geq 1\}$ be a family of concave functions on \mathbb{R} such that $v_{\gamma'}$ is strictly more concave than v_{γ} whenever $\gamma' > \gamma$. Given a payoff structure $(a^{ij}_{\sigma}, b^{ij}_{\sigma})^{i,j=1,\dots n}_{\sigma=H,L}$ satisfying (31)-(34), there exists a range $[\underline{\gamma}, \bar{\gamma}]$ such that the informed and uniformed organizational equilibria coexist if and only if $\gamma \in [\underline{\gamma}, \bar{\gamma}]$.

The bounds $\underline{\gamma}$ and $\bar{\gamma}$ can be derived explicitly in the case of quadratic utility: $v(x) = x - \gamma x^2/2$ for $x \in (-\infty, 1/\gamma)$. Conditions (37) and (38) then become

(41)
$$\frac{2f_L^i}{\gamma} < q \left(A_H^i - B_L^i + d_L^i + f_L^i \right)^2 - f_L^i \left(f_L^i - 2B_L^i + 2d_L^i \right),$$

(42)
$$\frac{2f_L^i}{\gamma} > q \left(A_H^i - B_L^i + f_L^i \right)^2 - f_L^i \left(f_L^i - 2B_L^i \right),$$

which respectively define $\underline{\gamma}$ and $\bar{\gamma}$. Proposition 12, given in the Appendix, shows that $\underline{\gamma} < \bar{\gamma}$ and a range of equilibrium multiplicity exists, provided $|d_L^i|$ is large enough.

• Modeling choices. Compared to anticipatory utility and imperfect recall, Kreps-Porteus preferences have the advantage of well-established axiomatic foundations. On the other hand, the results they lead to are much less tractable analytically. The thresholds determining equilibrium do not generally admit closed-form solutions, whereas in Propositions 1-3 they were obtained explicitly, with readily interpretable comparative statics. For financial markets, similarly, one could derive results based on risk attitudes that parallel those of Section 4, but they would be less transparent and perhaps somewhat less intuitive. Indeed it may be difficult for agents embedded in a social or market context to avoid informative signals, so the relevant question is more often how to deal with the information one does have.

6. Relations and contrasts to other theories

The paper has connections to several literatures. The first one is that on cognitive dissonance and other forms of self-deception, the second one that on anticipatory feelings and attitudes

⁵⁶By definition, w is more concave than v if $w = \omega \circ v$, for some increasing and concave function ω .

toward information.⁵⁷ Most papers so far have focused on individual rather than social beliefs, and none has asked what makes wishful thinking infectious or self-limiting. The analysis of group morale and groupthink in organizations relates the paper to a third line of work, which deals with heterogeneous beliefs and overoptimism in firms.⁵⁸ Beliefs there are most often exogenous (reflecting different priors), whereas here they endogenously spread, horizontally or vertically, through all or part of the organization. Beyond economics, the paper relates to the work in management on corporate culture and to that in psychology on "social cognition".

In models of social conformity and in models of herding, collective errors arise from divergences between individuals' private signals and their publicly observable statements or actions. Departing from these standard channels, the paper identifies a novel mechanism generating interdependent beliefs and behaviors, which: (i) requires neither private information nor lack of anonymity; (ii) accounts for both conformism and contrarianism, with clear predictions as to when each should be observed; (iii) is in line with the micro-experimental and case-study evidence of biased updating and information avoidance; (iv) generates many distinctive and potentially testable comparative-statics results.

A first alternative source of group error is social pressure to conform.⁵⁹ For instance, if agents are heard or seen by both a powerful principal (boss, group leader, government) and third parties whom he wants to influence, they may just toe the line for fear of retaliation. Their true beliefs should still show up ex-post in any unmonitored actions they were able to take, yet in many cases of organizational or market failure no such discrepancy is observed.⁶⁰ Self-censorship should also not occur when agents can communicate separately with the

⁵⁷On cognitive dissonance, see Akerlof and Dickens (1982), Schelling (1986), Kuran (1993), Rabin (1994), Bénabou and Tirole (2002, 2004, 2006b), Compte and Postlewaite (2004) and Di Tella et al. (2007). On anticipation, see Loewenstein (1987), Caplin and Leahy (2001), Landier (2000), Caplin and Eliaz (2005), Brunnermeier and Parker (2005), Bernheim and Thomadsen (2005), Köszegi (2006, 2010), Eliaz and Spiegler (2006), Brunnermeier et al. (2007) and Bénabou and Tirole (2011). For an evolutionary account of self-deception see, e.g., von Hippel and Trivers (2011), who argue that it initially evolved to facilitate the deception of others, but once developed also affected different aspects of behavior.

⁵⁸On the theoretical side, see, e.g. Rotemberg and Saloner (1993), Bénabou and Tirole (2003), Fang and Moscarini (2005), Van den Steen (2005), Gervais and Goldstein (2007) and Landier et al. (2009). On the empirical side, see, e.g., Malmendier and Tate (2005, 2008) or Camerer and Malmendier (2007).

⁵⁹One could also invoke an exogenous (Asch-like (1956)) preference for agreeing with the majority, but this has no real predictive content, e.g., for which settings are more conducive to the phenomenon (congruent vs. dissimilar objectives), or whether conformist preferences apply to genuine beliefs or only stated opinions.

⁶⁰See, e.g., footnote 21 on the cases of Enron, Lehman Brothers, and mortgage-securitization managers.

boss, who should then want to hear both good and bad news. There are nonetheless many instances where deliberately confidential and highly credible warnings were flatly ignored, with disastrous consequences for the decision-maker.⁶¹

A second important source of conformity is signaling or career concerns. Thus, when the quality of their information is unknown, agents whose opinion is at odds with most already expressed may keep it to themselves, for fear of appearing incompetent or lazy (Ottaviani and Sørensen (2001), Prat (2005)). Significant mistakes in group decisions can result in contexts where differential information is important, if anonymous communication or voting is not feasible.⁶² The mechanism explored here, by contrast, is portable between environments with and without anonymity, including financial markets and the electoral arena, where investors and voters make decisions privately.

The model's application to market manias and crashes links the paper to the literatures on bubbles and herding, but the mechanism is very different from those of existing models. First, in a standard cascade, each investor acts exactly as a cool-headed and benevolent statistician would advise him to. He thus goes against his own signal only in instances where the herd is truly more likely to have it right, and more generally displays the usual desire for accurate knowledge. This seems a far cry from the wishful assumptions and rationalizations ("new economy", this "time is different", "they are not making any more land", etc.) repeatedly described by observers and historians. Second, in herding models the problem is a failure to aggregate private signals, which becomes less relevant when more of this data becomes common knowledge, for example through statistical sources or the media. In market groupthink, by contrast, investors have access to very similar information, but their processing of it is distorted by a contagious form of motivated thinking.

⁶¹For instance, Enron V.P. Sharon Watkins' memo to CEO Ken Lay, and FED governor Edward Gramlich's warnings to Chairman Greenspan (see online Appendix D).

⁶²Private information is also not a key issue in many collective errors. Thus, in the two space shuttle disasters, NASA mission managers and engineers were all looking at the same data; see online Appendix D.

⁶³See, e.g., Banerjee (1992), Bikhchandani, Hirshleifer and Welch (1992), Caplin and Leahy (1994), Chamley and Gale (1994). In versions of herding models with naive agents (e.g., Eyster and Rabin (2009)), agents put excessive weight on the actions of others, but still without any kind of wishful thinking or motivated reasoning –they just lack statistical or strategic sophistication. Experimental tests show that people in fact overweigh their *own* information (a form of overconfidence) relative to that embodied in other players' moves, making cascades relatively rare and short-lived (e.g., Goeree et al. (2007), Weiszacker (2010)).

⁶⁴In the financial crisis of 2008, most key data on household debt, no-doc loans, mounting default rates, historical boom and bust cycles in real estate, etc., was easily accessible to the major players, including regulators (see, e.g., Foote et al. (2012)), and even loudly advertised by a few but prominent Cassandras.

7. Conclusion

This paper developed a model of how wishful thinking and reality denial spread through organizations and markets. In settings where others' ignorance of bad news imposes negative externalities (lower expected payoffs, increased risk), it makes such news even worse and thus harder to accept, resulting in a contagion of willful blindness. Conversely, where overoptimism has beneficial spillovers (thus dampening the impact of adverse signals), exante avoidance and ex-post distortion of information tend to be self-limiting. This mechanism of social cognition does not rely on complementarities in technology or preferences, agents herding on a subset of private signals, or exogenous biases in inference; it is also quite robust. The "Mutually Assured Delusion" (MAD) principle is thus broadly applicable, helping to explain corporate cultures characterized by dysfunctional groupthink or valuable group morale, why willful ignorance and delusions flow down hierarchies, and the emergence of market manias sustained by "new-era" thinking, followed by deep crashes.

In each of these applications, the institutional and market environment was kept simple, so as to make clear the workings of the underlying mechanism. Enriching these context-specific features should be quite fruitful. For hierarchical organizations, richer payoff and information structures could be incorporated, along with greater heterogeneity of interests among agents. Potential applications include the spread of organizational corruption (e.g., Anand et al. (2005)), corporate politics (e.g. Zald and Berger (1998)) and organizational-design questions such as the optimal mix of agents, network structure and communication mechanisms (e.g. Calvó-Armengol et al. (2011), Van den Steen (2010)). In the financial sphere, one could study how different market and regulatory structures can create complementarities in risk management through banks' willingness to find out, or avoid finding out, the true quality of the assets on their balance sheets. Exploring the sources, propagation and consequences of collective belief distortions remains a rich and promising research agenda.

Appendix A: Main Proofs

In the proofs given here, I maintain the text's focus on cognitive decisions in state L, fixing everyone's recall strategy in state H to $\lambda_H = 1$. In online Appendix C (Lemmas 5 and 6), I show that this is not a binding restriction: with the payoffs (1) there is no equilibrium with $\lambda_H < 1$ and no profitable individual deviation to $\lambda_H^i < 1$ from an equilibrium with $\lambda_H = 1$.⁶⁵ These results, as well as Proposition 11, are proved using the more general specification

(A.1)
$$U_2^i \equiv \theta \left[\alpha e^i + (1 - \alpha)e^{-i} \right] + \gamma,$$

where γ , like θ , is now also state-dependent and $\Delta \gamma \equiv \gamma_H - \gamma_L$ can be of either sign.

Proof of Proposition 1. Parts (ii) and (iii) follow from the monotonicity of Ψ in θ_L and α . Note that no assumption of symmetry in strategies was imposed (λ^{-i} could, a priori, be the mean of heterogenous recall rates). Therefore, the only equilibria are the symmetric ones described in the proposition.

Proof of Proposition 2. By Lemma 1, $\lambda = 1$ is an equilibrium when $s \leq \underline{s}(1)$, or $\Psi(1, s|1) \leq 0$ and $\lambda = 0$ is an equilibrium when $s \geq \overline{s}(0)$, or $\Psi(0, s|0) \geq 0$. Finally, $\lambda \in (0, 1)$ is an equilibrium if and only if $\Psi(\lambda, s|\lambda) = 0$. Now, from (9) and (6),

(A.2)
$$\Psi(\lambda, s|\lambda) = -m/\delta - c + (\delta + s) \alpha \theta_L + sq \left(\frac{\Delta \theta + (1 - \alpha) \lambda \theta_L}{q + (1 - q)(1 - \lambda)} \right).$$

This function is either increasing or decreasing in λ , depending on the sign of $(1 - \alpha)\theta_L + (1 - q)\Delta\theta$. One can also check, using (10)-(11), that the same expression governs the sign of $\underline{s}(1) - \bar{s}(0)$. The equilibrium set is therefore determined as follows:

- (a) If (14) does not hold, $\Psi(\lambda, s|\lambda)$ is increasing, so $\Psi(0, s|0) < \Psi(1, s|1)$, or equivalently $\underline{s}(1) < \overline{s}(0)$ by (10)-(11). There is then a unique equilibrium, equal to $\lambda = 1$ if $\Psi(1, s|1) \leq 0$, interior if $\Psi(0, s|0) < 0 < \Psi(1, s|1)$, and equal to $\lambda = 0$ if $0 < \Psi(0, s|0)$.
- (b) If (14) does hold, $\Psi(\lambda, s|\lambda)$ is decreasing, so $\Psi(1, s|1) < \Psi(0, s|0)$, or equivalently $\bar{s}(0) < \underline{s}(1)$ by (10)-(11). Then: (i) $\lambda = 1$ is the unique equilibrium for $\Psi(0, s|0) \leq 0$, meaning that $s \leq \bar{s}(0)$, while $\lambda = 0$ is the unique equilibrium for $\Psi(1, s|1) \geq 0$, meaning

⁶⁵Under the very weak condition that each agent encodes his own information (for future recall) in a cost-effective manner, which Lemma 5 shows can always be ensured. This is seen most clearly for $\lambda_H^i = \lambda_L^i = 0$, which is informationally equivalent to $\lambda_H^i = \lambda_L^i = 1$ but wastes m in each state.

that $s \geq \underline{s}(1)$; for $\Psi(1, s|1) < 0 < \Psi(0, s|0)$, or $\overline{s}(0) < s < \underline{s}(1)$, both $\lambda = 1$ and $\lambda = 0$ are equilibria, together with the unique solution to $\Psi(\lambda, s|\lambda) = 0$, which is interior.

Proof of Lemma 2 and Propositions 8-9. From (37), we have

(A.3)
$$\varphi'(d) \equiv -(1-q) \left[v' \left(q A_H^i + (1-q) \left(B_L^i - f_L^i - d \right) \right) - v' (B_L^i - d) \right],$$

so $\varphi'(d) > 0$ if and only if $B_L^i - d < qA_H^i + (1-q)(B_L^i - f_L^i - d)$, or $d > d_*^i$ defined in (40). Therefore, $\varphi(d)$ is strictly quasiconvex, with a minimum at d_*^i . Moreover, $qA_H^i + (1-q)(B_L^i - f_L^i - d_*^i) = B_L^i - d_*^i$, implying $\varphi(d_*^i) = v(B_L^i - d_*^i) - qv(A_H^i) - (1-q)v(B_L^i - d_*^i)$, or

(2) As d tends to $+\infty$, $\varphi^i(d) \approx v(-d(1-q))) - (1-q)v(-d)$, which behaves as $[(1-q) - (1-q)^{\gamma}] \times (-d)^{\gamma}$ and thus tends to $+\infty$, since $\gamma' > 1$. Similarly, as d tends to $-\infty$, $\varphi^i(d) \approx v(-d(1-q))) - (1-q)v(-d)$, which behaves as $[(1-q) - (1-q)]^{1/\gamma} \times (d)^{1/\gamma}$ and thus tends to $+\infty$, since $1/\gamma < 1$. The rest of Lemma 2 and Proposition 8 follow immediately, as does Proposition 9 since (39) implies $\varphi^i(0) < 0$, hence $\underline{d}^i < 0 < \overline{d}^i$.

Proof of Proposition 5. Part (1) follows directly from (23) and (12)-(13). In Part (2), it is easily seen that $s^* < \bar{s}(0)$, but $s^* < \underline{s}(1)$ requires $(1-q) \Delta \theta [m/\delta + c - \delta \alpha \theta_L] < \delta (1-\alpha) \theta_L \theta_H$, which can go either way.

Proof of Proposition 7. Assume for now that at t = 0, everyone else invests $k^{-i} = K$. Since investing (respectively, abstaining) at t = 1 is a dominant strategy given posterior $\mu^j = r(\lambda^j) \ge q$ (respectively, $\mu^j = 0$), the price in state L will be $P_L(K + (1 - \lambda^{-i})E)$ and the date-0 expected utilities of realism and denial equal to

$$(A.5) U_{L,R}(\lambda^i, \lambda^{-i}; k^i)/\delta = (\delta + s)P_L(K + (1 - \lambda^{-i})E)k^i,$$

(A.6)
$$U_{L,D}(\lambda^{i}, \lambda^{-i}; k_{,}^{i})/\delta = -m/\delta + (\delta + s)P_{L}(K + (1 - \lambda^{-i})E)(k^{i} + E) - cE + sr(\lambda^{i}) \left[P_{H}(K + E) - P_{L}(K + (1 - \lambda^{-i})E)\right](k^{i} + E).$$

The net incentive for denial, $\Delta U_L \equiv U_{L,D} - U_{L,R}$, is thus given by

(A.7)
$$[\Delta U_L(\lambda^i, \lambda^{-i}; \bar{k};) + m]/\delta = [(\delta + s)P_L(K + (1 - \lambda^{-i})E) - c]E,$$
$$+ sr(\lambda^i) [P_H(K + E) - P_L(K + (1 - \lambda^{-i})E)] (k^i + E).$$

Setting $r(\lambda^i) = 1$, realism is a (personal-equilbrium) best response to λ^{-i} for an agent entering period 1 with stock k^i if

(A.8)
$$m/\delta \ge \left[(\delta + s) P_L(K + (1 - \lambda^{-i})E) - c \right] E + s \left[P_H(K + E) - P_L(K + (1 - \lambda^{-i})E) \right] (k^i + E).$$

Conversely, denial $(r(\lambda^i) = q)$ is a (personal-equilibrium) best response for i if

(A.9)
$$m/\delta \leq \left[(\delta + s) P_L(K + (1 - \lambda^{-i})E) - c \right] E$$
$$+ sq \left[P_H(K + E) - P_L(K + (1 - \lambda^{-i})E) \right] (k^i + E).$$

For given k^i and λ^{-i} , these two conditions are mutually exclusive. When neither holds, there is a unique $\lambda^i \in (0,1)$ that equates ΔU_L to zero, defining a mixed-strategy (personal equilibrium) best-response. The next step is to solve for (symmetric) social equilibria.

1. Realism. From (A.8), $\lambda^i = \lambda^{-i} = 1$ is an equilibrium in cognitive strategies if

(A.10)
$$[(\delta + s)P_L(K) - c]E + s[P_H(K + E) - P_L(K)](k^i + E) \le m/\delta.$$

This condition holds for all $k^i \leq K$ if and only if

(A.11)
$$s \le \frac{m/\delta + [c - \delta P_L(K)] E}{[P_H(K + E) - P_L(K)] (K + E) + P_L(K)E} \equiv \underline{s}(1; K).$$

Moving back to the start of period 0, one now verifies that it is indeed an equilibrium for everyone to invest $k^i = K$. Since agents will respond to market signals $\sigma = H, L$, the expected price is $qP_H(K+E) + (1-q)P_L(K) > 0$, whereas the cost of period-0 production is 0 (more generally, sufficiently small). Thus, it is optimal to produce to capacity.

2. Denial From (A.9), $\lambda^i = \lambda^{-i} = 0$ is a cognitive equilibrium if

(A.12)
$$[(\delta + s)P_L(K + E) - c]E + sq[P_H(K + E) - P_L(K + E)](k^i + E) \ge m/\delta.$$

This condition holds for $k^i = K$ if

(A.13)
$$s > \frac{m/\delta + [c - \delta P_L(K+E)] E}{q [P_H(K+E) - P_L(K+E)] (K+E) + P_L(K+E) E} \equiv \bar{s}(0; q, K).$$

An agent with low k^i , however, has less incentive to engage in denial. In particular, for $s < \underline{s}(1;K)$, (A.10) for $k^i = 0$ precludes (A.12) from holding at $k^i = 0$. Let $\bar{k}(s,q)$ therefore

denote the unique solution in k^i to the linear equation

(A.14)
$$[(\delta + s)P_L(K + E) - c]E + sq[P_H(K + E) - P_L(K + E)](k^i + E) = m/\delta.$$

Subtracting the equality obtained by evaluating (A.12) at $s = \bar{s}(0; q, K)$ yields

$$sq [P_H(K+E) - P_L(K+E)] (K - \bar{k})$$
= $(s - \bar{s})P_L(K+E)E + (s - \bar{s})q [P_H(K+E) - P_L(K+E)] (K+E)$,

where the arguments are dropped from \bar{k} and \bar{s} when no confusion results. Thus,

(A.15)
$$K - \bar{k} = \frac{s - \bar{s}}{s} \times \left(\frac{q P_H(K + E) + (1 - q) P_L(K + E)}{q [P_H(K + E) - P_L(K + E)]} E + K \right) > \frac{s - \bar{s}}{s} \times (K + E).$$

Note that $\bar{k} \leq K$ (and is thus feasible) if and only if $s \geq \bar{s}$. One can now examine the optimal choice of k^i at t = 0, which will be either $k^i = K$ or some $k^i \leq \bar{k}$.

(a) For $k^i > \bar{k}(s,q)$, (A.14) implies that denial is the unique best response to $\lambda^{-i} = 0$, leading agent i to produce $e^i = E$ in both states at t = 1. These units and the initial k^i will be sold at the expected price $\bar{P}_q(K+E) \equiv qP_H(K+E) + (1-q)P_L(K+E) > 0$. Therefore, producing K in period 0 is optimal among all levels $k^i > \bar{k}(s,q)$, and yields ex-ante utility

(A.16)
$$U_D(0, K, K)/\delta = (\delta + s)\bar{P}_q(K + E)(K + E) - cE - (1 - q)m/\delta.$$

(b) For $k^i \leq \bar{k}(q;s)$, on the other hand, agent *i*'s continuation (personal-equilibrium) strategy is some $\lambda^i = \lambda(k^i) \geq 0$: in state L he weakly prefers to be a realist, achieving

(A.17)
$$U(\lambda^{i}, 0, k^{i}_{,}K)/\delta = (\delta + s)\bar{P}_{q}(K + E)(k^{i} + E) - cE$$

 $-(1 - q)\{(1 - \lambda^{i}) m/\delta - \lambda^{i} [c - (\delta + s)P_{L}(K + E)]E\}.$

The agent prefers $k^i = K$ to any $k^i \leq \bar{k}(q;s)$ if $U_D(0,K,K) > U(\lambda^i,0,k^i_jK)$, or

(A.18)
$$(\delta + s)\bar{P}_{q}(K+E)(K-k^{i}) > (1-q)\lambda^{i} \{m/\delta + [c - (\delta + s)P_{L}(K+E)]E\}.$$

Using (A.15) and $\lambda^i \leq 1$, it suffices that

(A.19)
$$\left(\frac{s - \bar{s}(0; q, K)}{s}\right) \left(\frac{\bar{P}_q(K + E)(K + E)}{1 - q}\right) \ge \frac{m}{\delta(\delta + s)} + \left(\frac{c}{\delta + s} - P_L(K + E)\right) E.$$

Since $\bar{P}_q(K+E)$ tends to $P_H(K+E)$ as q tends to 1, (A.19) will hold for q close enough to 1, provided $s-\bar{s}(0;q,K)$ remains bounded away from 0. Lemmas 3 and 4 (in online Appendix C) formalize this idea, showing that there exist a threshold $q^*(K) < 1$ and a nonempty interval $S^*(K)$ such that, for all $q > q^*(K) : S^*(K) \subset (\bar{s}(0;q,K),\underline{s}(1;K))$ and (A.19) holds for all $s \in S^*(K)$. Consequently, when $q > q^*(K)$ both $(k^i = K, \lambda^i = 1)$ and $(k^i = K, \lambda^i = 0)$ are equilibria of the two-stage market game, for any $s \in S^*(K)$. Indeed, we showed that: (i) for $s < \underline{s}(1;K)$, when others play $(k^{-i} = K, \lambda^{-i} = 1)$ agent i finds it optimal to also invest $k^i = K$ and then be a realist; (ii) for $s > \bar{s}(0;q,K)$, when others play $(k^{-i} = K, \lambda^{-i} = 0)$ he finds it optimal to invest K in period 0 even though he knows that this will cause him to engage in denial if state L occurs. \blacksquare

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Online Appendix B: Robustness and Extensions

B.1. Collective Apathy and Fatalism

The form of denial considered in the benchmark model of Section 2 is a collective "illusion of control" or overconfidence, leading to persistence in a costly course of action in spite of widely available evidence that it is doomed. The opposite case is collective apathy: rather than acknowledging a crisis that could be partly remedied through timely action, everyone pretends that things "could be worse" and that "nothing can be done" to improve them anyway. One can think of an ethnic group subject to discrimination or threat by another one, but whose members pessimistically deem it useless to fight back (Cialdini (1984), Hochschild (1996)). Another example is global-warning denial. A third one, examined below, is "tuning out" the distress of others. To capture these ideas, I simply extend (1) to

(B.1)
$$U_2^i = \theta \left[\alpha e^i + (1 - \alpha)e^{-i} - \kappa \right], \text{ where } \kappa \geq 0.$$

- When $\kappa < \min\{1, \theta_H/\Delta\theta\}$, state H remains (conditional on $e^j \equiv 1$) a more favorable state than L, and one can show that for κ below a certain threshold all the results of the case $\kappa = 0$ carry over with little change. In particular, if $-\kappa > 0$ it plays a role very similar to an individual's outstanding market position k^i in the Section 4.
- When $\kappa > \max\{1, \theta_H/\Delta\theta\}$, state H corresponds to a *crisis state*: action is called for, but even when carried out effectively $(e^j \equiv 1)$ it will not suffice to offset the shock, leaving agents worse off than in state L. Intuition now suggests that an equilibrium in which agents respond appropriately to crises can coexist with one in which they systematically censor such signals, remaining passive and fatalistic even though they actually have individual agency. ⁶⁶

Indeed, this problem is closely related to the original one, once recast in terms of the relative effectiveness of *inaction*. Formally, let $\tilde{\theta}$ take values $\tilde{\theta}_{\tilde{H}} \equiv -\theta_L$ in state $\tilde{H} \equiv L$ and $\tilde{\theta}_{\tilde{L}} \equiv -\theta_H < 0$ in state $\tilde{L} \equiv H$, with respective probabilities $\tilde{q} \equiv 1 - q$ and $1 - \tilde{q}$; similarly, let $\tilde{c} \equiv -c$. Using these transformed variables, it is then easy to obtain "parallels" to Propositions 2 to 6. In particular, condition (3) is replaced by

⁶⁶Furthermore, there is no equilibrium in which agents censor the signal $\sigma = L$ –just like when $\kappa = 0$ (or κ sufficiently below min $\{1, \theta_H/\Delta\theta\}$ more generally) there is no equilibrium in which they censor $\sigma = H$. See Lemma 6 and the proof of Proposition 11 in online Appendix C, with $\Delta \gamma \equiv -\kappa \Delta \theta$.

(B.2)
$$q\theta_H + (1 - q)\theta_L < \frac{c}{\alpha(s + \delta)} < \frac{c}{\alpha\delta} < \theta_H,$$

and the equilibrium strategies and thresholds are obtained by replacing $\Delta\theta$ with $-\kappa\Delta\theta$ and θ_H , θ_L , q, and c with their "tilde" analogues. In online Appendix C, I thus prove:

Proposition 11. Assume (B.2) and $\kappa > \max\{1, \theta_H/\Delta\theta\}$. All the results in Proposition 2 remain, but with denial ($\lambda < 1$) now occurring in state H only and leading to inaction. Facing up to crises and fatalistic inertia are both social equilibria if and only if $q(\kappa\Delta\theta) < (1-\alpha)\theta_H$.

The left-hand side of this modified MAD condition reflects the action-independent gain from being in the no-crisis state, while the right-hand side measures the endogenous losses inflicted by all those who, denying that a crisis has occurred, *fail to act*.

• Helping others or tuning out. Studies of how people respond to the distress of others –victims of accidents, wars, natural disasters, famine, genocide, etc. – display two important puzzles. First, they show a greater willingness to help when the number of those perceived to be in need is small than when it is large. Slovic (2007) discusses many experiments documenting such "psychic numbing" (lowered affective reactions and donations) in response to even small absolute increases in the size of the at-risk group. A second regularity, common to most public-goods situations, is that people give and help more when they know or expect that others are doing so.⁶⁷

The above results can help understand both phenomena. Let K be the number of people in need, or emphasized as being in need, and let θ be the severity of their situation. At cost c, each individual i = 1, ... n can help $(e^i = 1)$ up to a victims, and he experiences an empathic disutility equal to the total amount of suffering,

(B.3)
$$U_2^i = -\theta \left[K - a \sum_{j=1}^n e^j \right].$$

Note that this does not assume that people intrinsically undervalue "statistical lives" or actions that represent only "a drop in the ocean". Instead, this will be a result. Indeed, (B.3)

⁶⁷The first phenomenon is distinct from (but combines with) the "identifiable victim effect". Small et al. (2007) thus found that donations to a specifically identified Malawian child facing the risk of starvation decreased by more than a half when information about the child was complemented with background statistics documenting the scale of food shortages in Africa. An alternative explanation for the second set of findings is social norms; see, e.g., Bénabou and Tirole (2006a).

corresponds to (B.1) with $\alpha = 1/n$, $\kappa = K/na$ and θ simply replaced by θna . Therefore, as K increases beyond a critical threshold:

- (a) The loss in utility from acknowledging $\theta = \theta_H$ overtakes an individual's ability to remedy it, causing him to switch from helping to "tuning out" the problem by censoring from awareness and recall all painful evidence of the crisis: turning the page of the newspaper, switching the channel, rationalizing the situation as not so bad, etc.
- (b) The level at which an individual switches from response to non-response depends on how many others he believes are helping or tuning out: what matters to i is $K a\sum_{j\neq i}^n e^j$. Hence, within some range of K, both collective generosity and collective apathy –what Slovic terms the "collapse of compassion" are social equilibria, even though charitable giving involves no increasing returns.
- (c) Vivid, memorable images of the *intensity* of individual suffering θ (but not the number, K, which has the opposite effect) make the crisis more difficult to put "out of mind" and thus reduce the scope of apathy. In the multiplicity range, one small such example, widely publicized, can trigger a large equilibrium shift.

A somewhat different class of collective delusions are mass panics and hysterias. While the model does generate episodes of excessive doubt and overcautiousness, ⁶⁸ or even fatalistic apathy (as just seen), these seem too mild to capture what goes on in a full-fledged panic. Understanding the sources and transmission mechanisms that underlie delusional group pessimism, rather than optimism, is an interesting question for further research.

B.2. Robustness

While the benchmark model of Section 2 involves a number of specific assumptions, the insights it delivers are very general. Section 5 already demonstrated this claim with respect to the specification of individual agents' preferences and cognition, by replacing both anticipatory utility and malleable memory (or attention, awareness) with Kreps-Porteus (1978) preferences for late resolution of uncertainty. I show here how the paper's framework and main results also extend to a variety of other settings.

⁶⁸Recall first that when agents censor bad news, they never fully believe in the good state $(\sigma = H)$, even when it actually occurs $(r(\lambda^i) < 1)$ for any $\chi > 0$. Second, investors who fear (perhaps from having been burned once) falling prey to the next wave of collective overoptimism may shy away from even positive expected-value investments (this occurs when condition (A.18) in the appendix is reversed).

• Strategic interactions. The focus has so far been on environments in which an agent's welfare depends on others' actions, but his return to acting does not. Quite intuitively, strategic complementarities in payoffs will reinforce the tendency for contagion, whereas substitutabilities will work against it.⁶⁹ To see this, let agent i' expected payoff in state $\sigma = H, L$ now be $\Pi^i_{\sigma}(e^i, \mathbf{e}^{-i})$, where \mathbf{e}^{-i} denotes the vector of others' actions; his incentive to act is then

(B.4)
$$\pi_{\sigma}^{i}(\mathbf{e}^{-i}) \equiv \Pi_{\sigma}^{i}(1, \mathbf{e}^{-i}) - \Pi_{\sigma}^{i}(0, \mathbf{e}^{-i}).$$

In state L, the differential in i's anticipatory value of denial that results from others' "blind" persistence, previously given by $-s(1-\alpha)\theta_L$, is now $-s[\Pi_L^i(1,\mathbf{0})-\Pi_L^i(1,\mathbf{1})]$, which embodies the same MAD intuition. The new ingredient is that others' persistence now also changes the return to investing in state L (previously a fixed $\alpha\theta_L$), by $\pi_L^i(\mathbf{1})-\pi_L^i(\mathbf{0})$, with sign governed by $\Sigma_{j\neq i}$ $\partial^2\Pi_L^i/\partial e^i\partial e^j$. When actions are complements, delusion is thus less costly if others are also in denial, whereas with substitutes (as in the asset market of Section 4) it is more costly.

- Signal structure. Instead of "tuning out" bad news, selective awareness can take the form of spending resources to retain good ones—through rehearsal, preserving evidence, etc. This case, in which attention or recall is naturally imperfect but can be raised at some cost, is equivalent to setting m < 0, with all key results unchanged. The use of binary signals and actions is also inessential: with a richer state space, self-deception takes the form of a partitional coarsening of signals, as is standard in models of communication.
- Sophistication and common knowledge. While the model is an equilibrium one, strategic sophistication and common knowledge of rationality are inessential to the main results. For denial to be contagious, for instance, an agent does not need to know why others around him are escalating a risky corporate strategy, or accumulating dubious assets (Section 4) in spite of mounting red flags. It suffices that he see that they do $(e^j = 1 \text{ when } \sigma = L)$

⁶⁹Sources of complementarity may include technological gains from coordination or a desire for social conformity –whether intrinsic or resulting from sanctions imposed on norm violators. At the same time, without anticipatory feelings, preferences for late resolution of uncertainty or some other non-standard role of beliefs, no amount of complementarity can generate results similar to the model's: agents with standard preferences, including "social" ones, always have (weakly) positive demand for knowledge and thus never engage in reality denial or information avoidance.

and simply understand that this worsens his prospects: greater leverage implies a higher probability of firm bankruptcy if profits fall short, greater market buildup a deeper crash if fundamentals are weak, etc. Formally, the key property is that the slope of an agent's cognitive best-response (λ^i) to others' material actions (e^{-j}) in state L hinges on whether he is made or worse off by their mistakes (e.g., the sign of θ_L).

To demonstrate this claim, I present here a *bounded-rationality* version of the model in which agents simply best-respond to past aggregate investment, and show that it leads to results very similar to those of the fully rational case.⁷⁰

Let the game summarized by Figure 1 be repeated many times, and index those where state L occurs by $\tau \in \mathbb{N}$. At any stage t=1, agent i's optimal decision depends only on his own belief about θ . At stage t=0, by (1)-(2) the only aspect of other agents' play affecting his future payoffs is the aggregate action e_{τ}^{-i} they will choose at t=1, impacting him by $(1-\alpha)\theta e_{\tau}^{-i}$. Instead of forecasting e_{τ}^{-i} by using as before the equilibrium cognitive response λ_{τ}^{-i} to $\sigma=L$, let each agent now simply best-respond to the aggregate investment level $e_{\tau-1}^{-i}$ observed in the previous (similar) round.⁷¹ For simplicity, and without loss of generality, assume also that:

- (i) Consistently with the idea of bounded rationality, agents are unsophisticated about their own cognitive processes, as they are with respect to those of others: $\chi = 0$ in (6);
- (ii) Agents form a continuum, with parameter s distributed according to F(s) on $[s_{\min}, s_{\max}]$; heterogeneity could also be with respect to c or θ_H , or idiosyncratic signals about these variables. The continuum assumption will "smooth out" best responses and also equate e_{τ}^{-i} with the aggregate response (including i's), denoted e_{τ} .

With agents thus best responding to past play, the optimal choice between $\hat{\sigma}_{\tau}^{i} = L$ and $\hat{\sigma}_{\tau}^{i} = H$ is still governed by comparing (7) and (8), but with $(1 - \lambda^{-i})\theta_{L}$ replaced by $e_{\tau-1}\theta_{L}$; in addition, $r(\lambda^{i})$ simply becomes 1, since $\chi = 0$. The set of realists at any stage $\tau \geq 1$ of this adaptive process therefore consists of the agents with $s^{i} \leq \underline{s}(1 - e_{\tau-1})$, where the function $\underline{s}(\cdot)$ is still given by (10); their proportion is thus $\lambda_{\tau} = F\left[\underline{s}(1 - e_{\tau-1})\right]$. Since realists choose

⁷⁰The same would be true with other standard specifications of adaptive learning, such as fictitious play or replicator dynamics.

⁷¹The state σ drawn in any repetition of the stage game is also assumed to be observable ex-post (at stage t=2, when material payoffs are realized), even by those who temporarily forgot it. Such ex-post observability is in any case irrelevant for full groupthink ($\lambda^j \equiv 0$), where everyone invests in both states.

 $e_{\tau}^{i}=0$ and deniers $e_{\tau}^{i}=1$, moreover, we have $e_{\tau}=1-\lambda_{\tau}$. Hence the law of motion

(B.5)
$$\lambda_{\tau} = F\left(\frac{m/\delta + c - \delta\alpha\theta_{L}}{\alpha\theta_{L} + \Delta\theta + (1 - \alpha)\lambda_{\tau - 1}\theta_{L}}\right), \quad \forall \tau > 1.$$

For $\theta_L > 0$, λ_{τ} is decreasing in λ_{-1} , generating stable cobweb dynamics converging to a unique equilibrium (steady-state), and a multiplier less than 1 for responses to any local change in parameters. By contrast, when $\theta_L < 0$ the transition function is increasing, generating monotone dynamics, a scope for multiple equilibria (reached from different initial conditions e_0) and a multiplier locally greater than 1 (and increasing in $-\theta_L$).⁷²

⁷²Thus, $\lambda = 1$ and $\lambda = 0$ are both equilibria when $[s_{\min}, s_{\max}] \subset [\underline{s}(0), \underline{s}(1)]$, which can be ensured only when $\theta_L < 0$. There is even a continuum of equilibria for $[s_{\min}, s_{\max}] \equiv [\underline{s}(0), \underline{s}(1)]$ and $F(s) \equiv (\underline{s})^{-1}(s)$. Even with a unique equilibrium (or selecting the one reached from $e_0 = 1$), the multiplier can be made arbitrarily large by appropriate choice of θ_L . Finally, in the limit where F degenerates to a mass-point (homogenous agents), the fixed points of (B.5) coincide exactly with the equilibrium set of Proposition 2 (for $\chi = 0$).

Online Appendix C: Additional Proofs

Corollary 1 (to Proposition 2). Denote by $\underline{s}(\lambda^{-i}, \alpha)$ and $\overline{s}(\lambda^{-i}, \alpha)$ the thresholds respectively given by (10) and (11), and by $\tilde{s} \equiv \underline{s}(\lambda^{-i}, 1)$, which is independent of λ^i . Let $\alpha' < 1$ be such that $\delta[\alpha'\theta_L + \theta_H] > c$ and (14) holds. Then, for all m small enough, $\overline{s}(0, \alpha') < \underline{s}(1, \alpha') < \tilde{s}$ and:

- (i) For $\underline{s}(1, \alpha') < s < \tilde{s}$, $\lambda = 1$ is the unique equilibrium when $\alpha = 1$, and $\lambda = 0$ the unique equilibrium when when $\alpha = \alpha'$;
- (ii) For $\bar{s}(0, \alpha') < s < \underline{s}(1, \alpha)$, $\lambda = 1$ is the unique equilibrium when $\alpha = 1$, and $\{0, 1\}$ is the stable equilibrium set when $\alpha = \alpha'$.

Proof. The fact that $\bar{s}(0, \alpha') < \underline{s}(1, \alpha')$ is simply equation (14), while $\underline{s}(1, \alpha') < \tilde{s}$ if

(C.1)
$$[m/\delta + c - \delta\alpha'\theta_L] [\alpha'\theta_L + \Delta\theta] < [m/\delta + c - \delta\theta_L] [\alpha'\theta_L + \Delta\theta + (1 - \alpha')\theta_L]$$

For m = 0, this becomes:

$$(c - \delta \alpha' \theta_L) (\alpha' \theta_L + \Delta \theta) < (\alpha' \theta_L + \Delta \theta + (1 - \alpha') \theta_L) (c - \delta \theta_L) \iff$$

$$(C.2) (1 - \alpha') \delta \theta_L [\alpha' \theta_L + \Delta \theta] < (1 - \alpha') \theta_L (c - \delta \theta_L) \iff \delta [\alpha' \theta_L + \Delta \theta] > c - \delta \theta,$$

since $\theta_L < 0$, by (14). Therefore, since $\delta \left[\alpha' \theta_L + \theta_H \right] > c$, (C.1) holds for m small enough. With $\alpha = 1$, the uniqueness of equilibrium follows from $s < \tilde{s} = \underline{s}(1,1)$ and Proposition 2.2. With $\alpha = \alpha'$, results (i) and (ii) respectively follow from parts 2 and 1 of Proposition 2.

Proof of Proposition 3. Setting $\lambda^j \equiv 1$ in (18) and $\lambda^j \equiv 0$ in (19) yields the result.

Proof of Proposition 4. To make things simple, let $m^1=m^2$, $c^1=c^2$, $\delta^1=\delta^2$, $a_H^{11}=a_H^{22}$, $a_L^{11}=a_L^{22}$ and $a_H^{11}-a_L^{11}=a_H^{22}-a_L^{22}\equiv a>0$; finally, set $b^{ij}=0$ for all i,j. The asymmetry in roles is then captured by $X\equiv \left(a_H^{12}-a_L^{12}\right)/a>\left(a_H^{21}-a_L^{21}\right)/a\equiv x$ and, especially, $Y\equiv -\left(a_L^{12}-b_L^{12}\right)/a>-\left(a_L^{21}-b_L^{21}\right)/a\equiv y$. I shall first provide conditions ensuring

(C.3)
$$\bar{s}^2(0) < \underline{s}^1(0) < \underline{s}^1(1) < \bar{s}^1(0) < \bar{s}^1(1) < \underline{s}^2(1),$$

which implies $[\underline{s}^1(1), \bar{s}^1(0)] \subset [\bar{s}^2(0), \underline{s}^2(1)] \equiv S$, as illustrated in Figure 4. From (18)-(19), the middle inequality is equivalent to y < (1-q)(1+x), which can always be ensured given q < 1. The inequalities $\underline{s}^1(0) < \underline{s}^1(1)$ and $\bar{s}^1(0) < \bar{s}^1(1)$ hold for all y > 0 (complementarity).

Turning finally to the two outer conditions, we have $\bar{s}^2(0) < \underline{s}^1(0)$ if

$$q\left(a_H^{12} - a_L^{12} + a_H^{22} - a_L^{22}\right) > a_H^{21} - a_L^{21} + a_H^{11} - a_L^{11},$$

or qX > x + 1 - q, while $\bar{s}^{1}(1) < \underline{s}^{2}(1)$ if

$$q\left[a_{H}^{21}-a_{L}^{21}+a_{H}^{11}-a_{L}^{11}+a_{L}^{21}-b_{L}^{21}\right]>a_{H}^{12}-a_{L}^{12}+a_{H}^{22}-a_{L}^{22}+a_{L}^{12}-b_{L}^{12},$$

or Y > qy + X - qx + 1 - q; both are clearly satisfied for X sufficiently larger than x and Y sufficiently larger than X. I can now prove the claims (a)-(c) made in the text.

- (i) The result follows from the fact that $\bar{s}^2(0) \leq s \leq \underline{s}^2(1)$ and the definitions of these two thresholds in Proposition 1.
- (ii) The same definitions imply that an equilibrium with $(\lambda^1, \lambda^2) = (1, 1)$ (respectively, $(\lambda^1, \lambda^2) = (0, 0)$) exists if and only if $s^2 \leq \underline{s^2}(1)$ and $s^1 \leq \underline{s^1}(1)$ (respectively, $s^2 \geq \overline{s^2}(0)$ and $s^1 \geq \overline{s^1}(0)$), which corresponds to the left (respectively, right) region in Figure 4. In the middle region one must therefore have $\lambda^1 = \lambda_1^*(s^1; \lambda^2) \in (0, 1)$, where λ_1^* is the mixed-strategy best-response characterized in Proposition 1. It is decreasing in s^1 and increasing (respectively increasing) in λ^2 since for $a_L^{21} b_L^{21} = -ya < 0$.
- (iii) Consider now the boundary loci within the middle region. An equilibrium with $(\lambda^1, \lambda^2) = (\lambda_1^*(s^1; 1), 1)$ exists if and only if $s^1 \in [\underline{s}^1(1), \overline{s}^1(1)]$ and $s^2 \leq \underline{s}^2(\lambda_1^*(s^1; 1))$. This is a decreasing function of s^1 , which declines from $\underline{s}^2(\lambda_1^*(\underline{s}^1(1); 1)) = \underline{s}^2(1)$ at $s^1 = \underline{s}^1(1)$ to $\underline{s}^2(\lambda_1^*(\overline{s}^1(0); 1))$ at $s^1 = \overline{s}^1(0)$. For $|a_L^{21} b_L^{21}|/a = y$ small enough, $\lambda_1^*(\overline{s}^1(0); \lambda_2)$ is very insensitive to the value of λ_2 , so $\lambda_1^*(\overline{s}^1(0); 1) \approx \lambda_1^*(\overline{s}^1(0); 0) = 0$ and hence $\underline{s}^2(\lambda_1^*(\overline{s}^1(0); 1)) \approx \underline{s}^2(0) < \overline{s}^2(0)$. Therefore the curve $\underline{s}^2(\lambda_1^*(s^1; 1))$ cuts the lower boundary of S_2 at a point $s_1 < \overline{s}^1(0)$, as on Figure 4.

Similarly, with $(\lambda^1, \lambda^2) = (\lambda_1^*(s^1; 0), 0)$ exists if and only if $s^1 \in [\underline{s}^1(0), \overline{s}^1(0)]$ and $s^2 \geq \overline{s}^2(\lambda_1^*(s^1; 0))$. This is a decreasing function of s^1 , which declines to $\overline{s}^2(\lambda_1^*(\overline{s}^1(0); 0)) = \overline{s}^2(0)$ at $s^1 = \overline{s}^1(0)$, from $\overline{s}^2(\lambda_1^*(\underline{s}^1(1); 0))$ at $s^1 = \underline{s}^1(1)$. For y small enough, $\lambda_1^*(\underline{s}^1(1); \lambda_2)$ is very insensitive to the value of λ_2 , so $\lambda_1^*(\underline{s}^1(1); 0) \approx \lambda_1^*(\underline{s}^1(1); 1) = 1$ and hence $\overline{s}^2(\lambda_1^*(\underline{s}^1(1); 1)) \approx \overline{s}^2(1) > \underline{s}^2(0)$. Therefore, the curve $\overline{s}^2(\lambda_1^*(s^1; 0))$ cuts the upper boundary of S_2 at a point $s_1 > \underline{s}^1(1)$, as in Figure 4. Finally, for $a_L^{21} - b_L^{21} = 0$,

(C.4)
$$\underline{s}^{2}(\lambda_{1}^{*}(s^{1};1)) = \underline{s}^{2}(\lambda_{1}^{*}(s^{1};0)) < \overline{s}^{2}(\lambda_{1}^{*}(s^{1};0)) = \overline{s}^{2}(\lambda_{1}^{*}(s^{1};1)),$$

since agent 1's behavior is independent of that of agent 2. For y small enough, it remains the case that $\underline{s}^2(\lambda_1^*(s^1;1)) < \overline{s}^2(\lambda_1^*(s^1;1))$, by continuity. These properties of the two curves imply that equilibria of the form $(\lambda^1, \lambda^2) = (\lambda_1^*(s^1;1), 1)$, $(\lambda^1, \lambda^2) = (\lambda_1^*(s^1;0), 0)$ and $(\lambda^1, \lambda^2) = (\lambda_1^*(s^1;\lambda_2), \lambda_2^*(s^2;\lambda_1))$ exist only in the three respective regions indicated in Figure 4. The equilibrium is therefore unique, except possibly in the middle region where both agents mix. But since it is unique for x = y = 0, by continuity it remains so for x and y small enough.

Lemmas for the proof of Proposition 7. I prove here the claims made following equation (A.19) in the paper's main appendix.

Lemma 3. Under (30), there exists $\tilde{q}(K) < 1$ such that, for all $q \in [\tilde{q}(K), 1]$, $\bar{s}(0; q, K) < \underline{s}(1; K)$.

Proof. By (A.11)-(A.13), $\bar{s}(0; q, K) < \underline{s}(1; K)$ means that

(C.5)
$$\frac{m/\delta + [c - \delta P_L(K+E)] E}{q [P_H(K+E) - P_L(K+E)] (K+E) + P_L(K+E)E} < \frac{m/\delta + [c - \delta P_L(K)] E}{[P_H(K+E) - P_L(K)] (K+E) + P_L(K)E}.$$

If (C.5) holds for m = 0, the first denominator must be greater than the second, as $P_L(K + E) < P_L(K)$. Therefore, (C.5) holds for all $m \ge 0$ if and only if it holds for m = 0, or

$$\frac{c - \delta P_L(K+E)}{c - \delta P_L(K)} < \frac{q \left[P_H(K+E) - P_L(K+E) \right] (K+E) + P_L(K+E) E}{P_H(K+E)(K+E) - P_L(K) K}
= \frac{P_H(K+E)(K+E) - P_L(K+E) K}{P_H(K+E)(K+E) - P_L(K) K} - (1-q) \frac{\left[P_H(K+E) - P_L(K+E) \right] (K+E)}{P_H(K+E)(K+E) - P_L(K) K},$$

that is,

$$(1-q)\frac{[P_H(K+E)-P_L(K+E)](K+E)}{P_H(K+E)(K+E)-P_L(K)K} < \frac{P_H(K+E)(K+E)-P_L(K+E)K}{P_H(K+E)(K+E)-P_L(K)K} - \frac{c-\delta P_L(K+E)}{c-\delta P_L(K)}.$$

Finally, the condition takes the form

(C.6)
$$1 - q < \left(\frac{cK/(K+E) - \delta P_H(K+E)}{c - \delta P_L(K)}\right) \left(\frac{P_L(K) - P_L(K+E)}{P_H(K+E) - P_L(K+E)}\right).$$

Condition (30) ensures that $cK/(K+E) > \delta P_H(K+E)$, hence the result.

Lemma 4. Assume (30). For any $\eta \in (0, 1/2)$ define $s_{\eta}(0; 1, K) \equiv (1 - \eta)\bar{s}(0; 1, K) + \eta \underline{s}(1; K)$. There exists $q_{\eta}^*(K) < 1$ such that, for all $q \in (q_{\eta}^*(K), 1]$ condition (A.19) holds for all s in the nonempty interval $S_{2\eta}(K) \equiv (s_{2\eta}(0; 1, K)), \underline{s}(1; K)$.

Proof. For q close to 1 $\bar{s}(0;q,K)$ is close to $\bar{s}(0;1,K)$, so there exists $\hat{q}_{\eta}(K) \in (\tilde{q}(K),1]$ such that, for all $q \in (\hat{q}_{\eta}(K),1]$:

(C.7)
$$\bar{s}(0;q,K) < (1-\eta)\bar{s}(0;1,K) + \eta \underline{s}(1;K) \equiv s_{\eta}(0;1,K) < \underline{s}(1;K)$$

This implies, for any $s \in S_{2\eta}(K)$:

$$1 - \frac{\bar{s}(0; q, K)}{s} > \frac{s_{2\eta}(0; 1, K) - s_{\eta}(0; 1, K)}{\underline{s}(1; K)} = \eta \left(\frac{\underline{s}(1; K) - \bar{s}(0; 1, K)}{\underline{s}(1; K)} \right) = \eta \left(1 - \frac{\bar{s}(0; 1, K)}{\underline{s}(1; K)} \right).$$

Therefore, condition (A.19) holds provided that

$$1 - q \le \eta \left(1 - \frac{\bar{s}(0; 1, K)}{\underline{s}(1; K)} \right) \left(\frac{\bar{P}_q(K + E) \left(K + E \right)}{m / \left[\delta \left(\delta + s \right) \right] + \left[c / \left(\delta + s \right) + \bar{s}(0; 1, K) - P_L(K + E) \right] E} \right),$$

which will be the case for all q in some nonempty subinterval $(q_{\eta}^*(K), 1]$ of $(\hat{q}_{\eta}(K), 1]$.

From Lemmas 3 and 4, the last step in the proof of Proposition 7 stated in the main Appendix follows: pick any $\eta \in (0, 1/2)$, e.g., $\eta > 0$ and very small, then define $S^*(K) \equiv S_{2\eta}(K)$ and $q^* = q^*_{\eta}(K)$.

Proofs for Proposition 11 and the restriction to $\lambda_H^i = 1$ in Proposition 1. A strategy profile for agent i at t = 0 (his "self 0") is a pair $\lambda^i = (\lambda_H^i, \lambda_L^i)$ of probabilities with which he truthfully encodes $\hat{\sigma}^i = \sigma$ in each state $\sigma^i = H, L$. A strategy profile for the same agent at t = 1 (his "self 1") is a pair $\xi^i = (\xi_H^i, \xi_L^i)$ of probabilities with which he chooses $e^i = 1$ in each recall state $\hat{\sigma}^i = H, L$. An intrapersonal equilibrium consists of a quadruplet $(\lambda_H^i, \lambda_L^i; \xi_H^i, \xi_L^i)$ and posterior beliefs (r_H^i, r_L^i) in each recall state that together constitute a Perfect Bayesian Equilibrium for agent i (keeping fixed the strategies of all $j \neq i$):

(i) The posterior beliefs (or "reliability") of each recall state are given by Bayes' rule:

(C.8)
$$r_H^i \equiv \Pr\left[\sigma^i = H \mid \hat{\sigma}^i = H\right] = \frac{q\lambda_H^i}{q\lambda_H^i + (1 - q)(1 - \lambda_L^i)},$$

(C.9)
$$r_L^i \equiv \Pr\left[\sigma^i = L \mid \hat{\sigma}^i = L\right] = \frac{(1-q)\lambda_L^i}{(1-q)\lambda_L^i + q(1-\lambda_H^i)}.$$

- (ii) Date-1 actions are optimal: $\xi_{\sigma}^{i} = 1$ if $\alpha E[\theta \mid \hat{\sigma}_{i}] > c$ and $\xi_{\sigma}^{i} = 0$ if $\alpha E[\theta \mid \hat{\sigma}_{i}] < 0$.
- (iii) At t = 0, the agent in each state $\sigma = H, L$ optimally chooses (or randomizes between) which $\hat{\sigma} = H, L$ to encode, taking (i) and (ii) as given.

Lemma 5. Let m > 0 and fix any strategies $(\lambda_H^{-i}, \lambda_L^{-i})$ (whether equilibrium or not) of players $j \neq i$. If $(\lambda_H^i, \lambda_L^i)$ is an intrapersonal equilibrium for i such that $\max\{\lambda_H^i, \lambda_L^i\} < 1$, then (1,1) is also an equilibrium and it makes him strictly better off in both states.

Proof. I shall omit time-0 subscripts for simplicity. For any $(\sigma, \hat{\sigma}) \in \{L, H\}^2$, let $V_{\sigma\hat{\sigma}}^i$ denote the date-0 expected value of U_1^i that agent i could achieve in state σ by encoding it as $\hat{\sigma}$, if his behavior at date 1 was guided by "naive" posteriors, i.e. $\xi^i = 1$ when $\hat{\sigma} = H$ and $\xi^i = 0$ when $\hat{\sigma} = L$. The $V_{\sigma\hat{\sigma}}^i$'s do not depend on any actual or conjectured mixing probabilities used by the agent at t = 0. Next, define $U_{\sigma\hat{\sigma}}^i$ from the same encoding choices as $V_{\sigma\hat{\sigma}}^i$, but anticipating that beliefs at t = 1 will be derived from $(\lambda_H^i, \lambda_L^i)$ using (C.8)-(C.9). Finally, let U_{σ}^i be the date-0 expected utility achieved in state σ by following the mixing strategy $(\lambda_H^i, \lambda_L^i)$. Thus, for all $\sigma, \hat{\sigma}$ and $\tilde{\sigma} \neq \sigma$,

$$(C.10) U_{\sigma\hat{\sigma}}^{i} \equiv r_{\hat{\sigma}}^{i} V_{\sigma\hat{\sigma}}^{i} + (1 - r_{\hat{\sigma}}^{i}) V_{\sigma\tilde{\sigma}}^{i},$$

(C.11)
$$U_{\sigma}^{i} = \lambda_{\sigma\sigma}^{i} U_{\sigma\sigma}^{i} + (1 - \lambda_{\sigma\sigma}^{i}) \left(U_{\sigma\tilde{\sigma}}^{i} - m \right).$$

For any alternative candidate strategy $(\lambda_H^{\prime i}, \lambda_L^{\prime i})$ I use the same notations but with "primes" on all the variables. I first show that

(C.12)
$$U_H^i = U_{HL}^i < U_{HH}^{'i} \iff (1 - r_H^{'i} - r_L^i) (V_{HH}^i - V_{HL}^i) < m,$$

(C.13)
$$U_L^i = U_{LH}^i < U_{LL}^{'i} \iff (1 - r_L^{'i} - r_H^i) (V_{LL}^i - V_{LH}^i) < m.$$

In each case the equality comes from the fact that $\lambda_{\sigma}^{i} < 1$, so that denial is an optimal strategy in state σ , and the equivalence between inequalities then follows from (C.10) applied to both $(\lambda_{H}^{i}, \lambda_{L}^{i})$ and $(\lambda_{H}^{i}, \lambda_{L}^{i})$. Next, note that for $(\lambda_{H}^{i}, \lambda_{L}^{i})$ to be a personal equilibrium the

inequalities in (C.12)-(C.13) must be reversed when $(\lambda_H^i, \lambda_L^i) = (\lambda_H^i, \lambda_L^i)$, meaning that

(C.14)
$$(1 - r_H^i - r_L^i) \min \{V_{HH}^i - V_{HL}^i, V_{LL}^i - V_{LH}^i\} \ge m.$$

Suppose first that $r_L^i + r_H^i \leq 1$, implying $V_{HH}^i - V_{HL}^i > 0$ and $V_{LL}^i - V_{LH}^i > 0$. Consider then $(\lambda_H^{ii}, \lambda_L^{'i}) \equiv (1, 1)$, which by (C.8)-(C.9) leads to $(r_H^{ii}, r_L^{'i}) = (1, 1)$. Equations (C.12)-(C.13) are clearly satisfied, and the same is true if r_H^i and r_L^i are both replaced by 1. Therefore, systematic truthfulness leads to higher expected utility in each state than the original $(\lambda_H^i, \lambda_L^i)$ and it is also an equilibrium.

Suppose next that $r_L^i + r_H^i > 1$. From (C.8)-(C.9), we have

(C.15)
$$r_L^i + r_H^i > 1 \Leftrightarrow \lambda_H^i + \lambda_L^i > 1.$$

Since $\max\{\lambda_H^i, \lambda_L^i\} < 1$, this implies $(\lambda_H^i, \lambda_L^i) \in (0, 1)^2$: the agent mixes in both states, so $V_{HH}^i - V_{HL}^i = V_{LL}^i - V_{LH}^i = m/(1 - r_H^i - r_L^i) < 0$. However, by definition of the $V_{\sigma\hat{\sigma}}^i$'s,

$$(C.16) \qquad \left(V_{HH}^{i} - V_{HL}^{i}\right)/\delta = (s+\delta)\left(\alpha\theta_{H} - c\right) + s\left(W_{H}^{i} - W_{L}^{i}\right),$$

(C.17)
$$\left(V_{LL}^i - V_{LH}^i \right) / \delta = \alpha (s\theta_H + \delta\theta_L) - c + s \left(W_H^i - W_L^i \right),$$

where $W_{\sigma}^{i} \equiv (1 - \alpha)\xi_{\sigma}^{-i}\theta_{\sigma} + \gamma_{\sigma}$ is the true final payoff that agent i will receive in state σ from the (aggregate) effort decisions ξ_{σ}^{-i} of the other players, and exogenously (last term). The two expressions differ by $\alpha\delta\left(\Delta\theta\right) > 0$, so $(\lambda_{H}^{i}, \lambda_{L}^{i})$ cannot be an equilibrium.

Intuitively, any strategy with distortion or memory censoring in both states represents an inefficient way of encoding information, wasting m > 0 with positive probability. It does not corresponds to a best response to others' behavior since the agent can, on his own, improve upon it (under the very weak assumption that he can coordinate his "self 0" and "self 1" on a Pareto-superior intrapersonal equilibrium, which always exists). I therefore restrict attention, throughout the paper, to efficient encoding strategies, meaning that $\lambda_H^i = 1$ or $\lambda_L^i = 1$ for every i. This also implies, by (C.8)-(C.9),

(C.18)
$$r_H^i \ge q \ge 1 - r_L^i \text{ and } \xi_H^i = 1 \ge \xi_L^i.$$

Finally, as explained in footnote 19, I generally restrict attention to symmetric equilibria (except in Section 2.4, or when there is a large number $(n \to +\infty)$ of identical agents, as in Section 4). These two conditions will be implicit in the use of the word "equilibrium".

Lemma 6. (1) For $\Delta \gamma \geq -(1-\alpha) \min\{\theta_H, \Delta \theta\}$ there can be no equilibrium with $\lambda_H = 0$, and no profitable individual deviation to $\lambda_H^i < 1$ from any equilibrium in which $\lambda_H = 1$. (2) For $\Delta \gamma > -\min\{(1-\alpha)\theta_H, (1-\alpha)\Delta\theta, \kappa^*(s)\Delta\theta\}\}$, where $\kappa^*(s) > 0$ is given by (C.23) below, there can be no equilibrium with $\lambda_H < 1$. Thus, the results of Propositions 2-6 remain unchanged, up to the substitution of $\Delta \gamma + \Delta \theta$ for $\Delta \theta$ everywhere.

Proof. Following the same reasoning as in text (or directly from (C.10)-(C.11)) and omitting time subscripts to lighten the notation, the incentive to misinterpret or misremember H as L (gross of the cost m) is given by

(C.19)
$$(U_{HL}^{i,} - U_{HH}^{i,} + m) / \delta = s \left(1 - r_L^i - r_H^i \right) (\gamma_H - \gamma_L) + \left(\xi_H^i - \xi_L^i \right) [c - \delta \alpha \theta_H]$$

$$+ s \alpha \left\{ \left[\left(1 - r_L^i \right) \xi_L^i - r_H^i \xi_H^i \right] \theta_H - \left[\left(1 - r_H^i \right) \xi_H^i - r_L^i \xi_L^i \right] \theta_L \right\}$$

$$+ s \left(1 - \alpha \right) \left(1 - r_L^i - r_H^i \right) \left\{ \left[\lambda_H^{-i} \xi_H^{-i} + \left(1 - \lambda_H^{-i} \right) \xi_L^{-i} \right] \theta_H \right.$$

$$- \left[\lambda_L^{-i} \xi_L^{-i} + \left(1 - \lambda_L^{-i} \right) \xi_H^{-i} \right] \theta_L \right\}.$$

The incentive to miscode L as H is given by the same expression, with H and L switched:

$$(C.20) \quad \left(U_{LH}^{i,} - U_{LL}^{i,} + m\right) / \delta = s \left(1 - r_H^i - r_L^i\right) \left(\gamma_L - \gamma_H\right) + \left(\xi_L^i - \xi_H^i\right) \left[c - \delta \alpha \theta_L\right] \\ + s \alpha \left\{ \left[\left(1 - r_H^i\right) \xi_H^i - r_L^i \xi_L^i \right] \theta_L - \left[\left(1 - r_L^i\right) \xi_L^i - r_H^i \xi_H^i \right] \theta_H \right\} \\ + s \left(1 - \alpha\right) \left(1 - r_H^i - r_L^i\right) \left\{ \left[\lambda_L^{-i} \xi_L^{-i} + \left(1 - \lambda_L^{-i}\right) \xi_H^{-i} \right] \theta_L \\ - \left[\lambda_H^{-i} \xi_H^{-i} + \left(1 - \lambda_H^{-i}\right) \xi_L^{-i} \right] \theta_H \right\}.$$

From Lemma 5 and (C.18) we know that $\lambda_H^i = 1$ or $\lambda_L^i = 1$ and that in either case, $\xi_H^i = 1$, so in a symmetric equilibrium, $\xi_H^{-i} = \xi_H^i = 1$.

1. Equilibria with $\lambda_H = 1$. This implies $r_L^i = 1$, so $\xi_L^i = 0 = \xi_L^{-i}$ and (C.19) becomes

$$\begin{split} \left(U_{HL}^{i,} - U_{HH}^{i,} + m\right)/\delta &= -sr_H^i \left(\gamma_H - \gamma_L\right) + \left[c - \delta\alpha\theta_H\right] \\ &- s\alpha \left[r_H^i\theta_H + \left(1 - r_H^i\right)\theta_L\right] - sr_H^i \left(1 - \alpha\right) \left[\theta_H - \left(1 - \lambda_L^{-i}\right)\theta_L\right] \\ &= -\left[\left(\delta + s\right)\alpha \left(r_H^i\theta_H + \left(1 - r_H^i\right)\theta_L\right) - c\right] - sr_H^i \Delta\gamma \\ &- \Delta\theta \left[\delta\alpha \left(1 - r_H^i\right) + sr_H^i \left(1 - \alpha\right)\right] - sr_H^i \left(1 - \alpha\right)\lambda_L^{-i}\theta_L. \end{split}$$

The first term is negative since $r_H^i \geq q$, so it suffices that

$$(C.21) sr_H^i \Delta \gamma \ge -\Delta \theta [\delta \alpha (1 - r_H^i) + sr_H^i (1 - \alpha)] - sr_H^i (1 - \alpha) \lambda_L^{-i} \theta_L.$$

This inequality is linear in r_H^i and holds for $r_H^i = 0$. For $r_H^i = 1$, it takes the form $\Delta \gamma \ge -(1 - \alpha) \left[\Delta \theta + \lambda_L^{-i} \theta_L \right]$, which holds whatever the sign of θ_L when $\Delta \gamma \ge -(1 - \alpha) \min \left\{ \Delta \theta, \theta_H \right\}$. Thus, an individual deviation to miscoding H as L is never profitable. As to miscoding L as H, (C.20) becomes

$$\begin{split} \left(U_{LH}^{i,} - U_{LL}^{i,} + m\right) / \delta &= -\left[c - \delta\alpha\theta_L\right] + s\alpha\left[\left(1 - r_H^i\right)\theta_L + r_H^i\theta_H\right] \\ &+ s\left(1 - \alpha\right)r_H^i\left[\theta_H - \left(1 - \lambda_L^{-i}\right)\theta_L\right] + sr_H^i\left(\gamma_H - \gamma_L\right) \\ &= -\left[c - \left(\delta + s\right)\alpha\theta_L\right] + sr_H^i\left[\Delta\theta + \Delta\gamma + \left(1 - \alpha\right)\lambda_L^{-i}\theta_L\right], \end{split}$$

which is identical to (9) except that $\Delta\theta$ is replaced by $\Delta\theta + \Delta\gamma$. Therefore, all the previous results and formulas shown for $\Delta\gamma = 0$ and imposing $\lambda_H^i \equiv 1$ remain the same, provided $\Delta\theta + \Delta\gamma > \text{replaces }\Delta\theta$ wherever it appears.

2. Ruling out equilibria with $\lambda_H < 1 = \lambda_L$. If $\lambda_H^i < 1$ then $\lambda_L^i = 1$ by Lemma 5, so $r_H^i = 1$ and hence $\xi_H^i = 1 = \xi_H^{-i}$. Therefore, (C.19) simplifies to:

$$(U_{HL}^{i,} - U_{HH}^{i,} + m) / \delta = -(1 - \xi_L^i) [(\delta + s) \alpha \theta_H - c] - sr_L^i \{ \Delta \theta [\alpha \xi_L^i + (1 - \alpha) \xi_L^{-i}] + \Delta \gamma + (1 - \alpha) \lambda_H^{-i} (1 - \xi_L^{-i}) \theta_H \}.$$

In (symmetric) equilibrium $\xi_L^i = \xi_L^i$ and $\lambda_H^i = \lambda_H^{-i}$, so this expression is strictly negative and no equilibrium with $\lambda_H^i < 1$ exists, when

(C.22)
$$\xi_L^i \Delta \theta + \left(1 - \xi_L^i\right) \lambda_H^i \left(1 - \alpha\right) \theta_H + \Delta \gamma \ge 0.$$

For $\Delta\theta + \Delta\gamma \geq 0$, we can rule out any equilibrium with $\xi_L^i = 1$, and in particular any equilibrium with $\lambda_H^i = 0$ (which implies $r_L^i = 1 - q$, so $\xi_L^i = 1$). As to an equilibrium with $\xi_L^i < 1$, given $\lambda_L^i = 1$ this requires that λ_H^i not be below the critical value that makes an agent indifferent to working or not, given $\hat{\sigma}^i = L : \theta_L + [1 - r_L(\lambda_H, 1)] \Delta\theta \leq c/\alpha (s + \delta)$, or

(C.23)
$$\lambda_H^i (1 - \alpha) \left(\frac{\theta_H}{\Delta \theta} \right) \ge (1 - \alpha) \left(\frac{\theta_H}{\Delta \theta} \right) \left[1 - \left(\frac{1 - q}{q} \right) \left(\frac{c/\alpha (s + \delta) - \theta_L}{\theta_H - c/\alpha (s + \delta)} \right) \right] \equiv \kappa^*(s).$$

Therefore, by (C.22), any equilibrium with $\xi_L^i < 1$ is ruled out for $\Delta \gamma \ge -\Delta \theta \min\{1, \kappa^*(s)\}$; hence the result. Note, moreover, that since $\kappa^*(s)$ is increasing, if the second inequality in (3) is strengthened to $q\theta_H + (1-q)\theta_L > c/\alpha\delta$, then $\kappa_H^*(0) > 0$ and such equilibria are ruled out for any s if $\Delta \theta \min\{1, \kappa^*(0)\} + \Delta \gamma > 0$.

Proof of Proposition 11. I again show the result for the more general specification (A.1), under which $\kappa \geq \max\{1, \theta_H/\Delta\theta\}$ is a special case of $\Delta\gamma \leq -\max\{\Delta\theta, \theta_H\}$. Note first that since $1 - r_L^i \leq q$, (B.2) implies that $\xi_L^i = 0$ and thus, in a equilibrium, $\xi_L^{-i} = \xi_L^i = 0$.

1. Ruling out equilibria with $\lambda_L^i < 1 = \lambda_H^i$. If $\lambda_L^i < 1$ then $\lambda_H^i = 1 = \lambda_H^{-i}$ in equilibrium by Lemma 5 and symmetry, so $r_L^i = 1$ and $\xi_L^i = 0 = \xi_L^{-i}$. Therefore, (C.20) simplifies to:

$$\begin{split} \left(U_{LH}^{i,} - U_{LL}^{i,} + m\right)/\delta &= sr_H^i \Delta \gamma - \xi_H^i \left[c - \delta \alpha \theta_L\right] + s\alpha \xi_H^i \left[\left(1 - r_H^i\right) \theta_L + r_H^i \theta_H\right] \\ &+ sr_H^i \left(1 - \alpha\right) \xi_H^{-i} \left[\lambda_H^{-i} \theta_H - \left(1 - \lambda_L^{-i}\right) \theta_L\right] \\ &= -\xi_H^i \left[c - (s + \delta) \alpha \theta_L\right] + sr_H^i \Delta \gamma + \xi_H^i \left[\Delta \theta + (1 - \alpha) \lambda_L^i \theta_L\right] \end{split}$$

Since $\Delta \gamma + \xi_H^i \left[\Delta \theta + (1 - \alpha) \lambda_L^{-i} \theta_L \right] \leq \Delta \gamma + \xi_H^i \left[\Delta \theta + \max \left\{ 0, \theta_L \right\} \right] < 0$, the previous expression is strictly negative, and no equilibrium with $\lambda_L^i < 1$ exists.

2. Equilibria with $\lambda_L = 1$. This implies $r_H^i = 1$, so $\xi_H^i = 1 = \xi_H^{-i}$ and (C.20) becomes

$$\begin{split} \left(U_{LH}^{i,} - U_{LL}^{i,} + m\right)/\delta &= -sr_L^i \left(\gamma_L - \gamma_H\right) - \left[c - \delta\alpha\theta_L\right] + s\alpha\theta_H + sr_L^i \left(1 - \alpha\right)\lambda_H^{-i}\theta_H \\ &= -\left[c - \left(\delta + s\right)\alpha(r_L^i\theta_L + \left(1 - r_L^i\right)\theta_H)\right] \\ &+ sr_L^i \Delta\gamma - \left(1 - r_L^i\right)\delta\alpha\Delta\theta + sr_L^i \left[\alpha\Delta\theta + \left(1 - \alpha\right)\lambda_H^{-i}\theta_H\right]. \end{split}$$

The first term is negative since $r_L^i \leq 1 - q$, so it suffices that

(C.24)
$$sr_L^i \Delta \gamma \le (1 - r_L^i) \delta \alpha \Delta \theta - sr_L^i \left[\alpha \Delta \theta + (1 - \alpha) \lambda_H^{-i} \theta_H \right].$$

This inequality is linear in r_L^i and holds for $r_L^i = 0$. For $r_L^i = 1$, it takes the form $\Delta \gamma \leq -\left[\alpha \Delta \theta + (1-\alpha) \, \lambda_H^{-i} \theta_H\right]$, which holds for all λ_H^i if $\Delta \gamma \leq -\left[\alpha \Delta \theta + (1-\alpha) \, \theta_H\right]$. This expression is greater than $-\max\{\Delta \theta, \theta_H\}$ whatever the sign of θ_L , hence the result ruling out any profitable individual deviation to $\lambda_L^i < 1$. As to (C.19), it becomes

$$(U_{HL}^{i,} - U_{HH}^{i,} + m) / \delta = -sr_L^i (\gamma_H - \gamma_L) + [c - \delta \alpha \theta_H] - s\alpha \theta_H - s(1 - \alpha) r_L^i \lambda_H^{-i} \theta_H$$
$$= -[(s + \delta)\alpha \theta_H - c] - sr_L^i [\Delta \gamma + (1 - \alpha) \lambda_H^{-i} \theta_H].$$

Since $-\Delta \gamma - \theta_H > 0$, $\lambda_H^i = 1$ is an equilibrium (implying $r_L^i = 1$) if and only if

(C.25)
$$s \leq \frac{m/\delta + \delta\alpha\theta_H - c}{-\Delta\gamma - \theta_H} \equiv \underline{s}(1).$$

Similarly, $\lambda_H^i=0$ is an equilibrium (implying $r_L^i=1-q$) if and only if

(C.26)
$$s \ge \frac{m/\delta + \delta\alpha\theta_H - c}{(1 - q)(-\Delta\gamma) - \alpha\theta_H} \equiv \bar{s}(0),$$

if $-\Delta \gamma > \alpha \theta_H / (1-q)$, otherwise, let $\bar{s}(0) \equiv +\infty$. Multiple equilibria occur for $\bar{s}(0) < \underline{s}(1)$, i.e. $q(-\Delta \gamma) < (1-\alpha)\theta_H$. The treatment of the mixed-strategy equilibrium is similar to that in Proposition 2.

Proposition 12. Let $v(x) \equiv x - \gamma x^2/2$, and let (31), (32) and (39) hold for all i. If $|d_L^i|$ is large enough, for all i, there is a non-empty range $[\underline{\gamma}, \overline{\gamma}]$ such the informed uniformed equilibria coexist if and only if $\gamma \in [\gamma, \overline{\gamma}]$.

Proof. Condition (37) takes the form

$$\begin{split} qA_{H}^{i} + \left(1 - q\right)\left(B_{L}^{i} - f_{L}^{i} - d_{L}^{i}\right) - \left(\gamma/2\right)\left[qA_{H}^{i} + \left(1 - q\right)\left(B_{L}^{i} - f_{L}^{i} - d_{L}^{i}\right)^{2}\right] > \\ qA_{H}^{i} + \left(1 - q\right)\left(B_{L}^{i} - d_{L}^{i}\right) - \left(\gamma/2\right)\left[q\left(A_{H}^{i}\right)^{2} + \left(1 - q\right)\left(B_{L}^{i} - d_{L}^{i}\right)^{2}\right] & \Longleftrightarrow \\ \left(1 - q\right)f_{L}^{i} + \left(\gamma/2\right)\left[qA_{H}^{i} + \left(1 - q\right)\left(B_{L}^{i} - f_{L}^{i} - d_{L}^{i}\right)\right]^{2} < \left(\gamma/2\right)\left[q\left(A_{H}^{i}\right)^{2} + \left(1 - q\right)\left(B_{L}^{i} - d_{L}^{i}\right)^{2}\right], \end{split}$$

which is equivalent to (41). Similarly, (38) is equivalent to (42). Together, they define a nonempty range for γ if and only if

$$q\left(A_{H}^{i}-B_{L}^{i}+f_{L}^{i}\right)^{2}-f_{L}^{i}\left(f_{L}^{i}-2B_{L}^{i}\right) < q\left(A_{H}^{i}-B_{L}^{i}+d_{L}^{i}+f_{L}^{i}\right)^{2}-f_{L}^{i}\left(f_{L}^{i}-2B_{L}^{i}+2d_{L}^{i}\right) \iff 2f_{L}^{i}d_{L}^{i} < q\left(\left(d_{L}^{i}\right)^{2}+2d_{L}^{i}\left(A_{H}^{i}-B_{L}^{i}+f_{L}^{i}\right)\right).$$

If $d_L^i > 0$, which is the main case of interest, this inequality becomes:

(C.27)
$$d_L^i > 2 \left[(1 - q) f_L^i / q - (A_H^i - B_L^i) \right] = 2d_*^i.$$

which holds for d large enough –e.g., for all d > 0 when $d_*^i < 0$. If $d_L^i < 0$, the condition is reversed, and thus holds for $-d_L^i$ large enough (in e.g., for all d < 0 when $d_*^i > 0$).

Recalling finally that the highest possible payoff, A_H^i , must lie in the interval $(-\infty, 1/\gamma)$ over which $v(x) = x - \gamma x^2/2$ is increasing, it must also be that $\bar{\gamma} A_H^i < 1$, or

$$2f_{L}^{i}A_{i}^{H} + f_{L}^{i}\left(f_{L}^{i} - 2B_{L}^{i} + 2d_{L}^{i}\right) < q\left(A_{H}^{i} - B_{L}^{i} + d_{L}^{i} + f_{L}^{i}\right)^{2} \iff$$

$$(C.28) \qquad 2q\left(A_{H}^{i} - B_{L}^{i} + d_{L}^{i}\right)^{2} > 2(1-q)f_{L}^{i}\left(A_{H}^{i} - B_{L}^{i} + d_{L}^{i}\right) + (1-q)\left(f_{L}^{i}\right)^{2}.$$

Define the polynomial $P(X) \equiv qX^2 - 2(1-q)f_L^iX - (1-q)(f_L^i)^2$. The discriminant is $\Delta' = (1-q)(f_L^i)^2$, therefore the required condition is

(C.29)
$$(q/f_L^i) (A_H^i - B_L^i + d_L^i) \notin ((1-q) - \sqrt{1-q}, (1-q) + \sqrt{1-q}),$$

which again holds if $|d_L^i|$ is sufficiently large.

Online Appendix D: Patterns of Denial

This appendix highlights certain patterns (in both words and deeds) that recur across most instances of organizational and market meltdown, from the Space Shuttle disasters to the recent financial crisis.⁷³

1. Preposterous probabilities. In his contribution to the Rogers Commission Report (1986) on the Challenger disaster, Nobel physicist Richard Feynman noted that:

"It appears that there are enormous differences of opinion as to the probability of a failure with loss of vehicle and of human life. The estimates range from roughly 1 in 100 to 1 in 100,000. The higher figures come from the working engineers, and the very low figures from management. What are the causes and consequences of this lack of agreement? Since 1 part in 100,000 would imply that one could put a Shuttle up each day for 300 years expecting to lose only one, we could properly ask 'What is the cause of management's fantastic faith in the machinery?' "

Feynman's simple reasoning makes clear that NASA management's risk estimates —one thousand times lower than those of their own engineers— made no statistical sense. The housing-related bubble and buildup to the current financial crisis abound in even more extreme statements of confidence —nothing short of probability one. In an August 2007 conference with analysts, Joseph Cassano, head of AIG. Financial Services, asserted

"It is hard for us, without being flippant, to even see a scenario within any kind of realm of reason that would see us losing one dollar in any of those transactions...".⁷⁴

As late as 2008, in a meeting with investors,

"Lehman's chief financial officer, Erin Callan,... exuded confidence... With firms like Citigroup and Merrill raising capital, an investor asked, why wasn't Lehman following suit? Glaring at her questioner, she said that Lehman didn't need more money at the time –after all, it had yet to post a loss during the credit crisis. The company had industry veterans in the executive suite who had perfected the science of risk management, she said. "This company's leadership has been here so long that they know the strengths and weaknesses... We know when we need to be worried, and when we don't." (Anderson and Duhig (2008))

⁷³In what follows, all the quotes concerning NASA come from The Rogers Commission Report (1986) and the Columbia Accident Investigation Board Final Report (2003).

⁷⁴Cited in Morgenson (2008). Not coincidentally, this is the London unit (which he founded) that sank the company after selling over \$500 billion in credit default swaps that could not be covered.

Are such statements by top executives only cynical attempts to deceive investors and analysts about the quality of their balance sheet? While there is surely an element of moral hazard, this explanation falls short on several counts. First, absurd claims of zero risk in highly turbulent times are simply not credible, and thus more likely to be read as negative signals about the executive's grasp of reality than reassurance about fundamentals. In fact, they typically do nothing to bolster a company's share price, credit rating or prevent a run (see Sorkin (2008) for many examples).

Second, knowingly deceiving investors often leads to criminal prosecution and prison, as well as ruinous civil lawsuits and loss of reputation. A key aspect of self-delusion in such cases involves the expectation of "getting away" with fraud and cover-up, rather than ultimately sharing the fate of predecessors at Drexel Burnham Lambert, Enron, Worldcom, and many others.⁷⁵ Even abstracting from legal liability, selective blindness and collective rationalizations about the unethical nature of an organization's practices are key elements in the process that leads otherwise respectable citizens to take part in those practices (e.g., Sims (1992), Cohan (2002), Tenbrunsel and Messick (2004), Anand et al. (2005), Schrand and Zechman (2008), Bazerman and Tenbrunsel (2011)).

Third, identical claims of zero risk are made in settings where no large financial gain is involved and the downside can be truly catastrophic –as with NASA mission managers and financial regulators. Asked in a 2007 Congressional testimony whether he was "at all concerned... that if one of these huge institutions fails, it will have a horrendous impact on the national and global economy", former FED Chairman Alan Greenspan replied:⁷⁶

"No, I'm not," "I believe that the general growth in large institutions have occurred in the context of an underlying structure of markets in which many of the larger risks are dramatically –I should say, fully–hedged." (Goodman (2008))

His absolute certainty then turned to "shocked disbelief" when the disaster scenario materialized a few months later.

⁷⁵In 2007 alone the FBI made over 400 arrests in subprime-related cases (including top fund managers at Lehman Brothers) and had ongoing criminal investigations into 26 major financial companies including Countrywide Financial, A.I.G., Lehman Brothers, Fannie Mae and Freddie Mac. These companies and their top executives (e.g., most of those cited in this appendix) are also being sued by several State attorney generals, in addition to countless shareholders groups, investors and borrowers.

⁷⁶For other instances of blindness to red flags and active information-avoidance by financial regulators, see SEC (2008, 2009).

2. New paradigms: this time is different, we are smarter and have better tools. Every case also displays the typical pattern of hubris, based on claims of superior talent or human capital. For AIG.'s Joseph Cassano, losses being simply unimaginable (as seen above),

"The question for us is, where in the capital markets can we gain the best opportunity, the best execution for the business acumen that sits in our shop?".

What Feynman termed "fantastic faith in the machinery" is also often vested in computer models and statistical data. Subprime lenders and the banks purchasing the derived CDO's could thus rely on the fact that

"We have a wealth of information we didn't have before," "We understand the data and can price that risk." (2005 interview of Joe Anderson, then a senior Countrywide executive, cited in BusinessWeek, "Not So Smart," August 2007)

This trove of information was then fed to sophisticated computer programs:

"'It's like having a secret sauce; everyone had their own best formulas," says Edward N. Jones, CEO of ARC Systems, which sold [underwriting and risk-pricing] technology to HSBC... and many of their rivals." (BusinessWeek (2007))

Closely related is the argument that previous rules of accounting, risk management or economics no longer apply, due to some radical shift in fundamentals. Thus,

"I don't think it's a bubble, David M. Rubenstein of Carlyle Group told the Financial Times in December 2006. I think really what's happening now is that people are beginning to use a different investment technique, and this investment technique, private equity, adds real value." (Business-Week, 2007)

Shiller (2005) documents how such "new era thinking", variously linked to railroads, electricity, internet, demography or deregulation, was involved in nearly all historical episodes of financial bubbles and manias. One can also see it at work in government:

"The [senior White House] aide said that guys like me were "in what we call the reality-based community," which he defined as people who "believe that solutions emerge from your judicious study of discernible reality." I nodded and murmured something about enlightenment principles and empiricism. He cut me off. "That's not the way the world really works anymore," he continued." We're an empire now, and when we act, we create our own reality. And while you're studying that

reality – judiciously, as you will – we'll act again, creating other new realities, which you can study too, and that's how things will sort out." (Suskind (2004))

3. Escalation, failure to diversify, divest or hedge. Wishful beliefs show up not only in words but also in deeds. Enron's CEO Ken Lay resisted selling his shares throughout the long downfall, pledging other assets to meet collateral requirements, even buying stock back later on and ending up ruined well before his legal troubles began (Eichenwald (2005), Pearlstein (2006)). The company's employees, whose pension portfolios had on average 58% in Enron stock, could have moved out at nearly any point, but most never did (Samuelson (2001)). At Bears Stearns, 30% of the stock was held until the last day by employees — with presumably good access to diversification and hedging instruments— who thus lost their capital together with their job. CEO James Cayne alone owned an unusually high 6% and went from billionaire to small millionaire in the process (spending most of the intervening months away playing golf and bridge). The pattern is similar at Lehman Brothers and other financial institutions.

Without looking to such extremes, Malmendier and Tate (2005, 2008) document many CEO's tendency to delay exercising their stock options and how this measure of overconfidence is a predictor of overinvestment. Studying individual investors, finally, Karlsson, et al. (2009) find that many more go online to check the value of their portfolios on days when the market is up than when it is down.

Some of the most interesting evidence comes from cases in which an official inquiry or trial was conducted following a public- or private-sector disaster. Extensive records of meeting notes, memos, emails and sworn depositions reveal how key participants behaved, in particular with respect to information.

4. Information avoidance, repainting red flags green and overriding alarms. The most literal case of willful blindness occurred after the Columbia mission sustained a large foam strike to its wing's thermal shield:

"At every juncture of [the mission], the Shuttle Program's structure and processes, and therefore the managers in charge, resisted new information. Early in the mission, it became clear that the Program was not going to authorize imaging of [damage to] the Orbiter because, in the Program's opinion, images were not needed. Overwhelming evidence indicates that Program leaders decided the foam strike was merely a maintenance problem long before any analysis had begun."

Similar "head-in the sand" behavior was extensively documented at the Securities and Exchange Commission, even before its decade-long ignorance of Bernard Madoff's giant Ponzi scheme was revealed. The Inspector General's Report (S.E.C. (2008)) thus states:

"The audit found that [the Division of] Trading and Markets became aware of numerous potential red flags prior to Bear Stearns' collapse, regarding its concentration of mortgage securities, high leverage, shortcomings of risk management in mortgage-backed securities and lack of compliance with the spirit of Basel II standards, but did not take actions to limit these risk factors."

Instead, as reported in Labaton (2008), "the commission assigned [only] seven people to examine [the major investment banks] —which last year controlled... combined assets of \$4 trillion. Since March 2007, the office has not had a director. And as of last month, the office had not completed a single inspection since it was reshuffled by Mr. Cox [the SEC chairman] more than a year and a half ago."

Similarly, at the FED...

"Edward M. Gramlich, a Federal Reserve governor... warned nearly seven years ago that a fast-growing new breed of lenders was luring many people into risky mortgages they could not afford. But when Mr. Gramlich privately urged Fed examiners to investigate mortgage lenders affiliated with national banks, he was rebuffed by Alan Greenspan... Mr. Greenspan and other Fed officials repeatedly dismissed warnings about a speculative bubble in housing prices... The Fed was hardly alone in not pressing to clean up the mortgage industry. When states like Georgia and North Carolina started to pass tougher laws against abusive lending practices, the Office of the Comptroller of the Currency successfully prohibited them from investigating local subsidiaries of nationally chartered banks." (Morgenson and Fabrikant (2007))

... and the Treasury:

"In 1997, the Commodity Futures Trading Commission,... led by a lawyer named Brooksley E. Born... was concerned that unfettered, opaque trading could "threaten our regulated markets or, indeed, our economy without any federal agency knowing about it," she said in Congressional testimony. She called for greater disclosure of trades and reserves to cushion against losses. Ms. Born's views incited fierce opposition from Mr. Greenspan and Robert E. Rubin, the Treasury secretary then. Treasury lawyers concluded that merely discussing new rules threatened the derivatives market... In the fall of 1998, the hedge fund Long Term Capital Management nearly collapsed, dragged

down by disastrous bets on, among other things, derivatives. Despite that event, Congress froze the Commission's regulatory authority for six months. The following year, Ms. Born departed. In November 1999, senior regulators—including Mr. Greenspan and Mr. Rubin—recommended that Congress permanently strip the C.F.T.C. of regulatory authority over derivatives." (Goodman (2008))

To avoid having to override alarms systems, it is sometimes simplest to turn them off from the start:

"The Commission was surprised to realize after many hours of testimony that NASA's safety staff was never mentioned... No one thought to invite a safety representative or a reliability and quality assurance engineer to the [prelaunch] January 27, 1986, teleconference between Marshall [Space Center] and Thiokol. Similarly, there was no representative of safety on the Mission Management Team that made key decisions during the countdown on January 28, 1986. The Commission is concerned about the symptoms that it sees."

Similarly, at Fannie Mae:

"Between 2005 and 2007, the company's acquisitions of mortgages with down payments of less than 10% almost tripled... For two years, Mr. Mudd operated without a permanent chief risk officer to guard against unhealthy hazards. When Enrico Dallavecchia was hired for that position in 2006, he told Mr. Mudd that the company should be charging more to handle risky loans. In the following months to come, Mr. Dallavecchia warned that some markets were becoming overheated and argued that a housing bubble had formed... But many of the warnings were rebuffed... Mr. Dallavecchia was among those whom Mr. Mudd forced out of the company during a reorganization in August." (Duhig (2008))

The cavalier misuse of computerized models and simulations beyond their intended purposes is also mirrored between the engineering and financial worlds. Thus,

"Even though [Columbia's] debris strike was 400 times larger than the objects [the computer program] Crater is designed to model, neither Johnson engineers nor Program managers appealed for assistance from the more experienced Huntington Beach engineers, who might have cautioned against using Crater so far outside its validated limits. Nor did safety personnel provide any additional oversight."

In the subprime-credit boom,

"Some trading desks [at major banks] took the most arcane security, made of slices of mortgages, and entered it into the computer as if it were a simple bond with a set interest rate and duration...

But once the mortgage market started to deteriorate, the computers were not able to identify all the parts of the portfolio that might be hurt." (Hansell, 2008)

5. Normalization of deviance, changing standards and rationales.

How do organizations react when what was not supposed to happen does, with increasing frequency and severity?

"This section [of the report] gives an insider perspective: how NASA defined risk and how those definitions changed over time for both foam debris hits and O-ring erosion. In both cases, engineers and managers conducting risk assessments continually "normalized" the technical deviations they found... Evidence that the design was not performing as expected was reinterpreted as acceptable and non-deviant, which diminished perceptions of risk throughout the agency... Engineers and managers incorporated worsening anomalies into the engineering experience base, which functioned as an elastic waistband, expanding to hold larger deviations from the original design. Anomalies that did not lead to catastrophic failure were treated as a source of valid engineering data that justified further flights... NASA documents show how official classifications of risk were downgraded over time."

The same pattern of normalizing close calls with disaster shows up as a precursor to corporate scandals and financial meltdowns. Several years before Ken Lay failed to heed V.P. Sherron Watkins' urgent plea that he and the CAO "sit down and take a good, hard, objective look at what is going to happen to Condor and Raptor [ventures] in 2002 and 2003", lest the company "implode in a wave of accounting scandals", he had refused to fire two high-revenue-generating oil traders after learning that they had stolen millions from the company and forged financial documents to hide it. A year later, those very same "rogue" traders used again falsified books to make huge unauthorized bets on oil prices, which went sour and exposed the company to several hundred millions dollars of potential losses (Eichenwald (2005)). In a near repeat scenario, in 2004 AIG Financial Services caused the parent company to be fined \$126 million for helping clients engage in tax and accounting fraud. Yet the same manager (J. Cassano) remained in charge and was even put on the newly formed committee in charge of quality and risk control—until his unit blew up the

company four years later.

6. Reversing the burden of proof. At the Beech-Nut Corporation in late 1970's, tests by the main food scientist suggested that the apple concentrate from a new (and cheaper) major supplier was probably adulterated. Top management responded by telling scientists that the company would not switch suppliers unless they could absolutely prove that it was. At the same time, they made it more difficult for them to conduct inspections.⁷⁷ Similarly, at NASA,

"When managers... denied the team's request for imagery, the Debris Assessment Team was put in the untenable position of having to prove that a safety-of-flight issue existed without the very images that would permit such a determination... Organizations that deal with high-risk operations must always have a healthy fear of failure – operations must be proved safe, rather than the other way around. NASA inverted this burden of proof..."

Similar reversals of evidentiary standards and shifting rationales were also documented in the decision process leading to the second Iraq war, particularly on the issue of weapons of mass destruction (Hersh (2004), Isikoff and Corn (2007)).

7. Malleable memories: forgetting the lessons of history. The commission investigating the Columbia accident was struck by how the same patterns had repeated themselves six years after Challenger:

"The Board found that dangerous aspects of NASA's 1986 culture, identified by the Rogers Commission, remained unchanged... Despite the constraints that the agency was under, prior to both accidents NASA appeared to be immersed in a culture of invincibility, in stark contradiction to post-accident reality. The Rogers Commission found a NASA blinded by its "Can-Do" attitude... which bolstered administrators' belief in an achievable launch rate, the belief that they had an operational system, and an unwillingness to listen to outside experts."

In the financial and regulatory worlds, the lessons of LTCM were also quickly forgotten, as were those of the internet bubble a few years later. Such failures of individual and collective memory are recurrent. They were even pointed out (and then forgotten...) by a key observer and participant:

⁷⁷The product was later shown to be 100% artificial. Beech-Nut was convicted and paid several million in fines and class-action settlements, while the CEO and the former Vice-President of manufacturing were sentenced to jail (Sims (1992)).

"An infectious greed seemed to grip much of our business community... The trouble, unfortunately, is that the shock of what has happened will keep malfeasance down for a while. But human nature being what it is –and memories fade– it will be back. And it is important that at that time appropriate legislation be in place to inhibit activities that we would perceive to be inappropriate." (Greenspan (2002)).

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