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ScanImage: Flexible software for operating laser scanning microscopes

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Abstract

Background: Laser scanning microscopy is a powerful tool for analyzing the structure and function of biological specimens. Although numerous commercial laser scanning microscopes exist, some of the more interesting and challenging applications demand custom design. A major impediment to custom design is the difficulty of building custom data acquisition hardware and writing the complex software required to run the laser scanning microscope.

Results: We describe a simple, software-based approach to operating a laser scanning microscope without the need for custom data acquisition hardware. Data acquisition and control of laser scanning are achieved through standard data acquisition boards. The entire burden of signal integration and image processing is placed on the CPU of the computer. We quantitate the effectiveness of our data acquisition and signal conditioning algorithm under a variety of conditions. We implement our approach in an open source software package (Scanlmage) and describe its functionality.

Conclusions: We present Scanlmage, software to run a flexible laser scanning microscope that allows easy custom design.

Background

Laser scanning microscopies (LSM) include some of the most important imaging modalities in biology. For example, confocal laser scanning microscopy (CLSM) is the tool of choice for high-resolution fluorescence microscopy in cultured and fixed tissue preparations [1-3]. Twophoton excitation laser scanning microscopy (2PLSM) is ideal for fluorescence microscopy in scattering media, such as living skin and brain tissue [4,5].

Historically, new developments and applications of laser scanning microscopy have been limited primarily by the availability of new hardware. The development of suitable laser light sources and powerful data acquisition systems running on desktop computers brought CLSM to fruition [3]. In the case of 2PLSM, the development of modelocked pulsed light sources operating in the red and near IR spectral range [6] made it practical [5].

Several lines of commercial CLSMs and 2PLSMs are available. A manufacturer typically will offer one principal model and allow the customer to choose between different versions and options. Fundamentally, in terms of optics and software, a single general purpose design is offered. However, exciting applications demand specialized design. Often these applications include some of the most promising experimental developments. Currently, most hardware components of CLSMs and 2PLSMs (lasers, optics, scanning mirrors, detectors, and computers) are mature and readily available. The development of cutting edge applications using custom design is often limited by the availability of suitable software to control laser scanning microscopes.

In our laboratory we have written flexible software to control LSMs (ScanImage). In a LSM, a signal (typically fluorescence) is detected as a focused laser beam is scanned across a sample. The signal emitted from within a number of tiny, contiguous regions (called pixels) [3,7] is collected over short time intervals (the pixel time, T_p). The integrated signal is converted to a digital pixel value and the collection of all the pixels from the scanned region defines the image. The location of the pixel in the image is determined by the location of the laser at the time of acquisition. Synchronization of the position of the laser beam and the signal collection is therefore essential for imaging.

In order to time scanning and acquisition precisely and to achieve high performance in terms of signal-to-noise ratio, on-line averaging, and real-time image refresh, many commercially available laser-scanning microscopes (e.g. Olympus Fluoview™, Olympus America Inc., Melville, NY; Bio-Rad Radiance 2100™, Bio-Rad Laboratories, Hercules, CA) use proprietary signal conditioning electronics and data acquisition boards. Commercial systems are suitable for many applications and have also been customized for specific experimental needs [4,8–10]. However, complete custom design is often more advantageous and cost effective [11–13]. Two major impediments to custom design are the specialized software and hardware required for laser scanning microscopy.

Here we present a software package called *ScanImage* for collection of laser-scanned images that functions at a high level without the need for elaborate custom hardware [14,15]. The key idea is to use fast data acquisition boards and CPU-based numeric computations to perform most of the tasks that are accomplished by DSP boards and analog integrators in typical commercial systems. Thus *ScanImage* simplifies the design and construction of custom microscopes. An additional advantage is that *ScanImage* is written in MATLAB (version 6.1 or later; MathWorks Inc., Natick, MA), and thus already fully integrated into a highlevel image analysis environment.

Results and Discussion Description of Scanlmage

ScanImage controls a laser-scanning microscope (Figure 1A). It is written entirely in MATLAB and makes use of

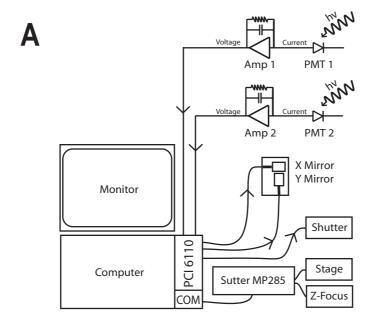
standard multifunction boards (e.g. National Instruments, Austin, TX) for data acquisition and control of scanning. The software generates the analog voltage waveforms to drive the scan mirrors, acquires the raw data from the photomultiplier tubes (PMTs), and processes these signals to produce images. ScanImage controls three input channels (12-bits each) simultaneously, and the software is written to be easily expandable to the maximum number of channels the data acquisition (DAQ) board supports and that the CPU can process efficiently. The computer bus speed dictates the number of samples that can be acquired before an overflow of the input buffer occurs, while the CPU speed and bus speed combine to determine the rate of data processing and ultimately the refresh rate of images on the screen. Virtually no customized data acquisition hardware is required for either scan mirror motion or data acquisition.

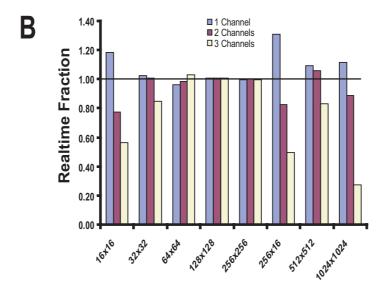
Typical pixel times in biological laser scanning microscopy are > 2 μ s (the pixel time depends on the pixels per line and the time per line; see Figure 2 for more information on the image construction algorithm). We have benchmarked *ScanImage* while acquiring three channels simultaneously with ~3 μ s pixel times (Figure 1B). Under these demanding conditions, *ScanImage* updates and saves the images with minimal delay from the time they are actually obtained (Figure 1B). The actual size of the image (in microns) depends on the microscope optics and the angles navigated by the scan mirrors.

We have chosen MATLAB as our development environment for its powerful numerical manipulation abilities and data acquisition (DAQ) engine. The DAQ engine directly communicates with the acquisition board and presents a flexible, object-oriented environment in which to construct DAQ software. In many scientific and engineering communities, MATLAB has become the dominant language for desktop numerical computing [16]. Integration of custom written analysis functions and incorporation of additional software is much more tractable for novice programmers in MATLAB, simplifying much of the experimental design process.

Data Acquisition in Scanlmage

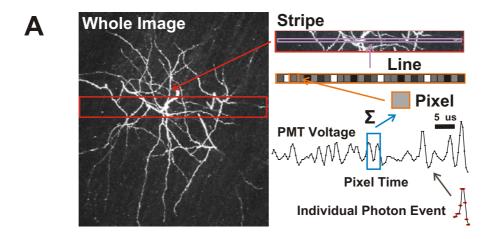
The signal from the detector (typically a PMT) is a current that needs to be converted to a voltage before acquisition. This conversion can be done with a standard amplifier [17] (see Stanford Research Systems, Sunnyvale, CA for examples) equipped with a low pass filter. The roll-off frequency of the filter has to be $<0.5\,f_s$, where f_s is the rate at which the detector signal is sampled. In *ScanImage* we compromise between the degradation in the signal-tonoise ratio due to limited sampling of the signal and the increasing computational load placed on the CPU with higher sample rates.





Pixels Per Line x Lines Per Frame

Figure IWiring Diagram and Performance Benchmarking for Scanlmage A) Typical wiring diagram for a microscope running Scanlmage. Scanning, data acquisition, and laser shuttering are accomplished by a single data acquisition board (PCI 6110, National Instruments). Stage and Z-focus motors are controlled through a Sutter 3-axis motor controller (Sutter MP285) that is programmed through a serial communications (COM) port. **B)** Performance of Scanlmage. We computed the realtime fraction as the average time it took Scanlmage to process and display the acquired data (i.e. a stripe; see Figure 2) normalized to the acquisition time for that portion of data. Values were averaged over 20 frames acquired at each configuration. The realtime fraction was computed using an 800 MHz Pentium III computer with 512 MB of RAM. A realtime fraction above one indicates the software was able to run in realtime (i.e. Scanlmage had completed processing and displaying all of the previously collected data before the next portion of data was fully acquired). For realtime fractions less than one, the display lags the acquisition but no data is lost. The low realtime fraction when acquiring 16 lines per frame on multiple channels indicates that we are approaching the fundamental speed limit for graphics updates.



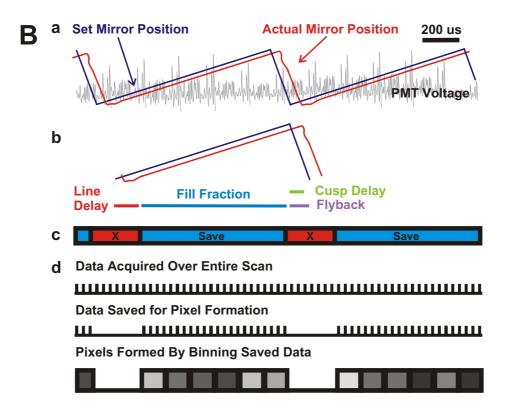


Figure 2
Image Construction and Signal Processing in ScanImage A) Schematic depicting the algorithm of image creation in ScanImage. Pixels are constructed by summing the PMT voltage over the pixel time T_p. To achieve fast (i.e. realtime) refresh rates we break the acquisition of an image down into a set of stripes acquired and displayed in succession. The stripes are concatenated to form the entire image. B) Further details of image construction in ScanImage. a) Mirror position signal delivered by ScanImage (blue trace) and the actual mirror position (red trace) for two lines of acquisition (PMT voltage shown in gray). b) Definitions of acquisition parameters. The flyback (purple) and line delay (red) regions of the acquired PMT signal are discarded from final image data, which keeps only the fill fraction (blue) of the PMT voltage for image construction. Because the scan mirrors have inertia, their actual position lags the set position by ~7% of the scan period, which is corrected by the cusp delay (green). c) ScanImage retains the data acquired during the linear portions of the scan (blue) and discards the intervening data (red). d) Samples are summed to form the pixels in the final image.

With current computer hardware we operate *ScanImage* with $f_{\rm S}$ = 1.25 MHz. This sampling frequency allows nearly ideal imaging (in terms of apparent quantum efficiency and bleedthrough between pixels, discussed below) for pixel times as short as 3 μ s. An appropriate roll-off frequency would be ~300–500 kHz. In the future, faster computer architectures will allow more rapid sampling and number crunching and hence shorter pixel times. The sampled data is streamed to memory. An overview of the image construction algorithm used in *ScanImage* is shown in Figure 2A.

Sampled data are summed in real-time over the pixel times. Once the data is collected, it is compared with the output signals to the scan mirrors. The position of the scan mirrors dictates where the pixels lie in the final image. The mirror driver electronics (see Cambridge Technology, Cambridge, MA for examples) and the command voltage output to the drivers from the DAQ board determine the mirror position. During a cycle of the mirror motion useful data are collected only when the mirrors are moving at constant velocity (i.e. linear voltage versus time regime; see Figure 2B). Data acquired when the mirrors are turning around or flying back to their starting positions (flyback) are removed (Figure 2B; figure caption for details).

The timing for image formation requires synchronization of the mirror scan forms and the data acquisition engine. This is achieved by triggering data acquisition and data output using a TTL trigger generated by the DAQ board (i.e. under the control of a software panel). This mechanism for triggering also allows *ScanImage* to be externally triggered by a TTL from another application or hardware device. Appropriate sampling rates and output rates are hard-coded in *ScanImage*, while many other acquisition parameters can be chosen based on the demands of particular applications.

Quality of the Images Collected by ScanImage

We evaluated the performance of our signal conditioning method (Figures 2 &3). We compared the variability of the integral of a simulated PMT signal to the variability of the signal sum computed at a fixed sample rate as is done in *ScanImage* (see Figure 2B for details). In simulations the PMT voltage was modeled as a Poisson process with mean photon rate of 0.5 photons per μ s. Each single-photon pulse was Gaussian with unit amplitude and 2.35 μ s full-width-at-half-maximum (FWHM) [18]. Each simulated pulse was constructed at 500 MHz. A 20 ms waveform was created by summing Poisson-distributed pulses and dividing them into 2000 pixel intervals (duration 10 μ s). Each of these intervals constituted a trial in the analysis of variability described below. Trials were sampled at 200 kHz

to 5 MHz in 100 kHz steps. A typical trial sampled at different rates is shown in the inset of Figure 3A.

How does the signal to noise ratio vary with sampling frequency? A useful measure of the quality of the signal is the coefficient of variance (CV_y). CV_y is the ratio of the standard deviation (σ_y) to the mean ($\bar{\gamma}$) of the signal summed over a pixel interval (γ). CV_y is related to the apparent quantum efficiency ($\hat{\eta}$) of the acquisition system and the mean number of pulses per pixel interval (\bar{N}) by Equation 1:

$$\hat{\eta} = \frac{\left(\overline{\gamma}\right)^2}{\sigma_y^2 \overline{N}} = \frac{1}{\overline{N}} \frac{1}{CV_y^2} \tag{1}$$

 $\hat{\eta}$ is inversely related to the noise introduced by the signal conditioning in addition to the inherent shot noise of the light source and multiplicative noise due to the variable pulse-amplitude distribution [19]. For optimal sampling with uniform pulse amplitudes, $\hat{\eta}$ will be 1 since $\sigma_{\gamma}^2 = \overline{\gamma} = \overline{N}$ (see **Equation 1**); this can be accomplished by direct integration of the signal (Figure 3A, red line). Thus we can interpret any reduction in $\hat{\eta}$ from 1 as a decrease of the signal-to-noise ratio (SNR) of the system.

We verified our simulation by fitting the histogram of the number of events (N) to a Poisson model (Figure 3B). This analysis yielded a mean value for $\bar{N}=4.96\pm.09$ (p < .05) photons per pixel interval (10 μ s duration) as expected. We then analyzed the trials sampled at different frequencies to determine the effects of finite sample frequency on $\hat{\eta}$. Variation of the pulse amplitudes can be modeled directly by convolving the pulse amplitude distribution with our model, but does not alter the optimal signaling criteria; it merely reduces the maximum value of $\hat{\eta}$ to a value lower than 1 [18].

 η was computed at each sample rate from the simulated pulses (Figure 3A). Note that the digital integrator shows nearly ideal behavior ($\hat{\eta}\approx 1$). As expected, for low sampling frequencies $\hat{\eta}$ is small, reflecting the fact that data (single photon events) are missed by the sampling scheme. $\hat{\eta}$ increases with sample rate until it approaches 1 around the Nyquist limit of 1 MHz (i.e. since we simulated the PMT voltage with 2.35 μs pulses). We repeated this analysis with data coming from an actual PMT filtered at ~330 KHz (blue points in Figure 3A). The lower filtering frequency broadens the pulses (3–4 μs FWHM) and hence

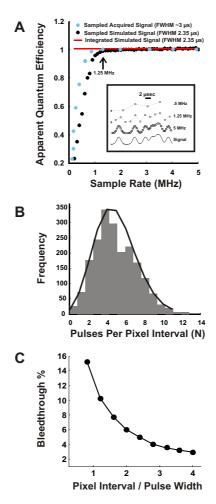


Figure 3 Image Quality in ScanImage A) Apparent quantum efficiency as a function of sampling rate in ScanImage for a single-photon-pulse with a 2.35 μ s FWHM and unit amplitude. The red trace shows the apparent quantum efficiency ($\hat{\eta}$) of the signal

(see inset) determined by digital integration. The black trace shows $\,\hat{\eta}\,$ sampled at 200 kHz to 5 MHz. $\,\hat{\eta}\,$ approaches I as the sample rate approaches I MHz. The blue points are the normalized apparent quantum efficiencies from an actual PMT illuminated by a constant light source (data pre-filtered at 330 kHz). Scanlmage uses a sample rate of 1.25 MHz (arrow), which yields nearly ideal signal-to-noise $\,\hat{\eta}\,\approx I$. This analysis is only valid for pulses that are all least 2.35 $\,\mu$ s in duration. Inset: 20- $\,\mu$ s pulse interval comprised of 2.35- $\,\mu$ s events sampled at different rates. B) Histogram of the events in the pixel interval (bars) and Poisson fit (line). C) Model of bleedthrough of photons from adjacent pixels. A single-photon-pulse with a 2.5 $\,\mu$ s FWHM was placed randomly in pixel intervals of widths 2 to 10 $\,\mu$ s. The number of trials at each pixel interval was 10,000. The percent bleedthrough equaled 100*(1 - IPP/IEP) where IEP is the integral of the entire pulse and IPP is the integral of the region of the pulse that fell in the pixel interval. Shown is the mean value of the percent bleedthrough for each pixel time normalized with respect to the pulse width (Pixel Interval/Pulse Width). The error bars (SEM) were smaller than the marker points and were omitted.

increases the performance of our algorithm at lower sample rates. At 1.25 MHz, the image has an essentially ideal $\hat{\eta}$.

We also modeled the expected bleedthrough of photons from adjacent pixels (Figure 3C). A simulated test pulse with a FWHM of 2.5 μ s was placed randomly in pixel intervals of widths 2 to 10 μ s. The percent bleedthrough was calculated as the percentage of the area of the pulse that

fell outside of the pixel interval in which it was placed. We see that the bleedthrough for the shortest pixel times recommended (\sim 3.0 μ s) is \sim 10%. Longer pixel times under normal imaging conditions (Pixel Interval/Pulse Width \sim 2) yield a bleedthrough of only \sim 6%.

Currently *ScanImage* performs well with a 1.25 MHz acquisition rate and a 330 kHz filter frequency (blue points and arrow in Figure 3A) depending on the application. Using sampling rates above 1.25 MHz (together with higher filter frequencies) is currently an issue of bus and CPU speed as mentioned. The sample rate can be adjusted manually in the software to a multiple of 1.25 MHz (e.g. 2.5 MHz) without any corruption of image quality. This yields an effective range of pixel times of 2–3-µs. Pixel times as low as 2 µs are feasible with a 500 kHz filter acquiring at 1 ms per line.

Conclusions

We have shown that our algorithm creates digital images with near-ideal noise properties and realtime refresh rates.

Scanlmage Features

We now briefly describe the software that we have created to turn the data acquisition algorithm into a full image acquisition program. The features presented here can be easily extended through the MATLAB interface. The wiring diagram for a LSM using *ScanImage* is given in Figure 1A.

Multi-Channel Acquisition

Many applications, including quantitative calcium imaging, can involve the use of two dyes with different spectral properties (e.g. green calcium sensitive, Fluo-4, and red calcium insensitive, Alexa Fluor-594) [15]. Optics can be easily designed to separate and simultaneously collect both of the emitted wavelengths in separate channels. We have integrated support for processing 3 separate fluorescence channels independently in *ScanImage*. The data are collected, processed, and displayed simultaneously in real time (Figure 1B).

3-Dimensional Image Acquisition

The microscope focus is under the control of *ScanImage* allowing automated collection of stacks of images from different focal planes. These stacks can be set and collected easily in *ScanImage* using any configuration. Kalman filtering can be implemented per focal plane for noise reduction.

Structure of Acquired Data

ScanImage stores data in TIF files for easy portability and compatibility. TIF files can include multiple frames for storage of three-dimensional, multi-channel, and time series data in the same file. The pixel intensities are saved as 16-bit unsigned integers, exploiting the full dynamic

range of the detector and DAQ boards. Different acquisition channels are interleaved. The experimental details are written into a header string that is placed into the *Image-Description* field of the generic TIF header, and can be accessed via the standard header reading modules included in all image-processing programs, including MATLAB.

Automation of Stage Controls

LSM often involves finding the region (or regions) of interest (ROIs) in a complex and large specimen. The ability to select and save ROIs can help in the design of complex imaging experiments. *ScanImage* allows the user to define an arbitrary number of ROIs for imaging. *ScanImage* uses its control of the stage and focus to automate collection of focal stacks of data as well as for saving and retrieving ROIs. Through a system of experimental cycles it is possible to select multiple ROIs and image them in succession at a selected repetition rate any number of times.

Focus Interface

Before data acquisition the structure to be imaged needs to be located. For this purpose a rapid acquisition mode is necessary where the user can observe the image in real-time as the specimen and focal positions move. *ScanImage* includes a focus mode to accomplish this. The image seen in focus mode is identical to the one that will be acquired. Multiple channels can be focused simultaneously in real-time. Image zooming and rotation are accomplished in the focus mode by changing the signal output to the mirrors.

Modular Design of Scanlmage: User Functions

One of the key advantages of *ScanImage* is the user-friendly development environment, MATLAB. Users can easily develop and test data analysis functions off-line and incorporate them into the software without fear of interfering with the data acquisition. A flowchart of *ScanImage* from a programming perspective is given in Figure 4A and a screenshot of the software is shown in Figure 4B.

Any MATLAB function can be automatically executed after an image is acquired to aid in analysis of the experiment while it is being conducted (see *ScanImage* manual for details). In addition to MATLAB functions, programmers can compile C and Fortran code and run it with MATLAB calls in the same user function.

Modular Design of Scanlmage: Controlling Additional Devices

From a programming perspective, the code allows the generation of custom graphical interfaces that can be incorporated easily into *ScanImage* (see Figure 4A). As an example, additional serial ports may need to be integrated to run other optical equipment. A GUI can be constructed with its own initialization file and run in parallel to *Scan-*

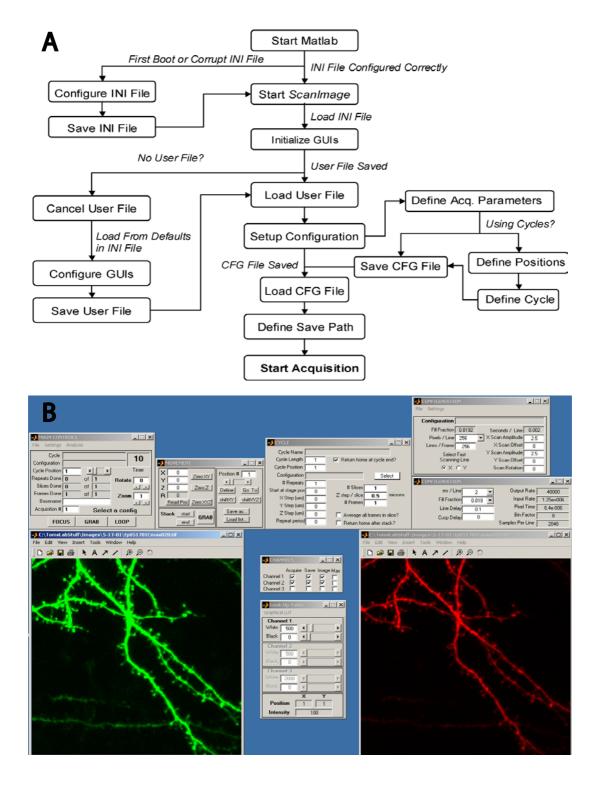


Figure 4
Flowchart and Screenshot of Scanlmage A) Scanlmage uses a series of text files to remember configurations for different microscopes, users, and experimental configurations. Each aspect of the software and the associated files is detailed in the Scanlmage manual. B) A screenshot of Scanlmage acquiring data from 2 channels simultaneously.

Image (see the *ScanImage* manual for details). This GUI can use the same convenient tools for handling GUIs that *ScanImage* uses while offering the programmer flexibility in both design and development.

Availability and Distribution

ScanImage is freely available as OSI Certified open source software. The license can be found in the *ScanImage* folder in the *ScanImage* License.txt file. All terms of the license, including details on referencing *ScanImage* in published reports, must be followed when using *ScanImage*.

The software and documentation on installation are available from: http://svobodalab.cshl.edu/software main.html.

Please email any questions or suggestions about the software to scanimage@cshl.edu

Methods

Programming

All programming and benchmarking was done in MAT-LAB 6.1 running on a Windows 2000 Professional PC with an 800 MHz Pentium III processor and 512 MB of RAM.

List of Abbreviations

2PLSM two-photon excitation laser scanning microscopy

CLSM confocal laser scanning microscopy

DAQ data acquisition

CPU central processing unit

TTL transistor-transistor logic

PMT photo-multiplier tube

GUI graphical user interface

SNR signal-to-noise-ratio

LUT look-up table

DSP digital signal processing

COM communications port

FWHM full-width-at-half-maximum

SEM standard error of the mean

RAM random access memory

Author's Contributions

BLS and KS conceived and planned this project. TAP and BLS wrote the majority of the code, with contributions from KS. Simulations and experiments were performed by TAP with KS. TAP and KS drafted the manuscript.

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