

2.59 For Code-Time-Division Multiple Access, the received signal is given by:

$$y(t) = \sum_{k=1}^K \sum_{i=-M}^M A_k b_k[i] s(t - iT - \tau_k) + \sigma n(t). \text{ Since each user offset is controlled so that}$$

$$\tau_k - \tau_{k-1} = T/K, \quad y(t) = \sum_{j=-KM}^{KM+K-1} A_{\lfloor \frac{j}{K} \rfloor + 1} b[j] s(t - jT/K) + \sigma n(t)$$

Since the waveform $s(t)$ has a duration T , every bit overlaps with $2(K-1)$ bits where each pair of bits has a different amplitude. The cross-correlations between every 2 pair of signature waveforms is given by:

$$\rho_{kl} = \int_0^T s(t) s(t - (l-k)T/K) dt, \quad l > k$$

$$\rho_{kl} = \int_0^T s(t) s(t - T + (l-k)T/K) dt, \quad l < k$$

Therefore calling $R(\tau) = \int s(t) s(t - \tau) dt$ we have

$$\rho_{kl} = \begin{cases} R\left(\frac{l-k}{K}T\right), & l > k \\ R\left(T - \frac{l-k}{K}T\right), & l < k \end{cases}$$

$$\text{We conclude that } \mathbf{R}[0] = \begin{bmatrix} 1 & R(T/K) & R(2T/K) & \dots & R\left(\frac{K-1}{K}T\right) \\ R(T/K) & 1 & \dots & \dots & R\left(\frac{K-2}{K}T\right) \\ R(2T/K) & \vdots & \ddots & \dots & \vdots \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ R\left(\frac{K-1}{K}T\right) & R\left(\frac{K-2}{K}T\right) & \dots & \dots & 1 \end{bmatrix}$$

$$\mathbf{R}[1] = \begin{bmatrix} 0 & R\left(\frac{K-1}{K}T\right) & R\left(\frac{K-2}{K}T\right) & \dots & R(T/K) \\ 0 & 0 & \dots & \dots & R\left(\frac{2}{K}T\right) \\ 0 & \vdots & \ddots & \dots & \vdots \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & \dots & 0 \end{bmatrix}$$