

Diffusion and scaling during early embryonic pattern formation

Thomas Gregor^{*†§¶}, William Bialek^{*†}, Rob R. de Ruyter van Steveninck^{||}, David W. Tank^{*†‡}, and Eric F. Wieschaus^{*§¶}

[§]Howard Hughes Medical Institute, ^{*}Lewis-Sigler Institute for Integrative Genomics, [†]Joseph Henry Laboratories of Physics, and [‡]Department of Molecular Biology, Princeton University, Princeton, NJ 08544; and ^{||}Department of Physics, Indiana University, Bloomington, IN 47405

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Development of spatial patterns in multicellular organisms depends on gradients in the concentration of signaling molecules that control gene expression. In the *Drosophila* embryo, Bicoid (Bcd) morphogen controls cell fate along 70% of the anteroposterior axis but is translated from mRNA localized at the anterior pole. Gradients of Bcd and other morphogens are thought to arise through diffusion, but this basic assumption has never been rigorously tested in living embryos. Furthermore, because diffusion sets a relationship between length and time scales, it is hard to see how patterns of gene expression established by diffusion would scale proportionately as egg size changes during evolution. Here, we show that the motion of inert molecules through the embryo is well described by the diffusion equation on the relevant length and time scales, and that effective diffusion constants are essentially the same in closely related dipteran species with embryos of very different size. Nonetheless, patterns of gene expression in these different species scale with egg length. We show that this scaling can be traced back to scaling of the Bcd gradient itself. Our results, together with constraints imposed by the time scales of development, suggest that the mechanism for scaling is a species-specific adaptation of the Bcd lifetime.

bicoid | morphogen | dipteran evolution

One of the classic challenges for models of embryonic development is the problem of scaling: Although organisms vary substantially in size, the variations in proportion are much less significant, and in cases where the fully developed organism has a segmented structure the number of segments often is invariant across a wide range of sizes. In well studied systems such as *Drosophila*, segmented structures have their origin in spatially periodic patterns of gene expression that are visible at early stages of embryonic development, and the emergence of these patterns has been described, at varying levels of detail, in terms of the diffusion and interaction of the relevant “morphogen” molecules (1–3). In nonbiological systems governed by similar equations, the spatial scale of patterns is set by local parameters analogous to the diffusion constants and reaction rates; hence, when we change the size of the system, the dimensions of the stripes remain fixed and the number of stripes changes (4). How then are we to understand the scaling of segment size and the conservation of their number in the biological case? Here, we use *Drosophila melanogaster* and a set of closely related dipteran species as model systems in which to address this problem.

Anteroposterior patterning in the *Drosophila* embryo is controlled by gradients in the concentration of maternal gene products that arise soon after fertilization. These protein molecules establish broad domains of gene expression that interact to establish final segmentation. One of the best studied maternal determinants in *Drosophila* is bicoid (*bcd*) (5). *Bcd* RNA is deposited during oogenesis at the anterior pole of the egg. After fertilization, the RNA is translated and a Bcd protein gradient is established along the anteroposterior axis of the egg. Subsequently, Bcd acts as a transcription factor, regulating genes such as *hunchback*, *krüppel*, and *even-skipped*

in a concentration-dependent manner (6), and these gene products feed into a regulatory circuit that generates striped patterns of expression of the gap and pair rule genes (cf. Fig. 2).

The Bcd gradient is established in a syncytium, where nuclei replicate without intervening cell division (7), and the size of the embryo stays constant, so that pattern formation is independent of growth. The absence of cell membranes would seem to provide an ideal environment for diffusion-based gradient formation. On the other hand, visual observation of the developing embryo reveals contractions of the egg cortex and large-scale cytoplasmic motions occurring with each mitotic cycle, raising questions about whether the relevant movement of any molecule can be described by simple diffusion.

Parallel to the question of whether diffusion is a good description of molecular motion in the embryo is the question of scaling. Certainly, related species of flies have similarly scaled proportions in their body plans, but relatively little is known about the underlying pattern of gene expression in the embryo. One can imagine, for example, scaling of body plan without scaling of the Bcd gradient itself, by changing the rules that the downstream genes use in responding to this gradient.

Here, we address both questions. To test the validity of the diffusion model, we use microinjections of inert, fluorescent molecules to probe and measure diffusive properties of embryonic cytoplasm of various dipteran species. To test for scaling, we use immunofluorescence stainings to compare Bcd gene expression profiles in those species. Our findings show that these different measurements, taken together, strongly constrain models for the formation and readout of the Bcd gradient.

Methods

Antibody Staining. Embryos were selected from early interphase of cell cycle 14, i.e., before significant membrane invagination, and the images were focused at mid-embryo to avoid geometric distortion. All species were stained with antibodies raised against *D. melanogaster* (8). For the *Lucilia sericata* and *D. melanogaster* embryos in Fig. 2*A*, we used rabbit anti-paired, guinea pig anti-runt, guinea pig anti-hunchback, and rat anti-giant. For the *D. melanogaster* and *Drosophila busckii* embryos in Fig. 2*B*, we used rat anti-hunchback and guinea pig anti-runt. Images were taken with a Zeiss LSM510 confocal microscope, with Zeiss $\times 10$ (N.A. 0.45) and $\times 20$ (N.A. 0.6) air objectives.

Diffusion Measurements. Dextran particles were purchased from Molecular Probes (10, 40, and 70 kDa) and Sigma-Aldrich (150 kDa). Corresponding hydrodynamic radii, r_s , were taken from ref. 9 and ref. 10, respectively. Calibrated volumes of ≈ 4 –5 pl

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[¶]To whom correspondence may be addressed. E-mail: gregor@princeton.edu or ewieschaus@princeton.edu.

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Table 1. Effective diffusion constants, D of dextran molecules of different sizes in *D. melanogaster*

Molecular mass, kDa	r_s , nm	N	D , $\mu\text{m}^2/\text{s}$
10	2.3	11	29.1 ± 4.2
40	4.5	20	17.6 ± 1.8
70	5.9	8	15.3 ± 1.4
150	9.0	5	12.9 ± 3.4

The sample size N refers to the number of diffusion experiments analyzed.

many spatially separated locations. If the underlying molecular motion is in fact diffusive, then these dynamics at each location will be fit by the solution of the diffusion equation, with only a single free parameter (the diffusion constant itself) that can be chosen to fit all of the data. Although the data were roughly consistent with analytic predictions for diffusion along one dimension, for quantitative analysis we used numerical calculations in realistic 3D geometries to more accurately model the expected concentration dynamics (see *Methods*). Fig. 1*B* indicates that concentration changes on the length and time scales relevant for development are well described by the diffusion equation and hence that the molecular motion can be approximated by random walks.

If random molecular movement is due to Brownian motion (passive diffusion), then it is governed by the Stokes–Einstein relationship: diffusion coefficients decrease inversely with increasing molecular radius. To test this relationship, we measured diffusion constants for dextran molecules of four different nominal molecular masses (Table 1). Fig. 1*C* shows a good fit of the Stokes–Einstein relation to our data with an effective cytoplasmic viscosity of 4.2 cP ($1 \text{ P} = 0.1 \text{ kg}\cdot\text{m}^{-1}\cdot\text{s}^{-1}$), four times higher than water. This is well within the range of viscosities reported in other systems (15, 16). We also observe a constant, radius-independent contribution to the diffusion constant (the parameter b in the legend to Fig. 1*C*), as noted previously (10). This is consistent with a random “stirring” of the cytoplasm and is $\approx 25\%$ of the total at molecular masses of 55 kDa, the molecular mass of Bcd. This would represent an active, and hence biologically controllable, contribution to the dynamics of molecular motion. Although this enhances the effective diffusion constant, our experiments show that it does not invalidate the description of the dynamics by the diffusion equation.

Scaling of Gene Expression Profiles. The above results make plausible that spreading of Bcd from its localized source, and hence the generation of the primary anteroposterior gradient, will be described by the diffusion equation. However, diffusion-based models provide no natural mechanism for generating spatial patterns that scale with the size of the egg. Specifically, in systems where patterns emerge through a combination of diffusion and biochemical reactions, the diffusion constant and reaction rates determine an absolute length scale. Thus, when the size of the system changes, the spacing of the pattern elements would remain fixed (4). Although Bcd is conserved across >100 million years of dipteran evolution (17), the eggs of closely related species vary over at least a factor of five in length (Table 2). Despite these changes in size, the stripe-like patterns of gap and pair-rule genes scale with egg length, as is clear qualitatively in Fig. 2. As a quantitative example of this scaling, the point of half maximal *hunchback* expression is at $45 \pm 6\%$ egg length in *L. sericata* and at $48 \pm 3\%$ in *D. melanogaster*, so that the absolute positions of this boundary are changing in proportion to egg length over a nearly threefold range.

Table 2. Effective diffusion constants of 40-kDa dextran molecules in dipteran species

Species (mean egg length)	N	D , $\mu\text{m}^2/\text{s}$
<i>D. busckii</i> (344 μm)	8	14.5 ± 3.8
<i>D. melanogaster</i> (485 μm)	20	17.6 ± 1.8
<i>L. sericata</i> (1,170 μm)	6	22.8 ± 1.5
<i>C. vicina</i> (1,420 μm)	4	20.3 ± 1.3

In *D. melanogaster*, the expression patterns illustrated in Fig. 2 reflect and depend on the underlying distribution of Bcd (17). We can envision two very different mechanisms for generating scaled versions of these profiles in the species with larger embryos. First, the Bcd gradient could stay the same, and the cis-acting control sites of downstream genes could have adapted over evolution so that specific genes are activated by lower concentrations of Bcd in species with larger eggs. Alternatively, the Bcd gradient itself could scale, while the readout mechanisms encoded in the control sites of downstream genes are conserved across species.

To distinguish between these possibilities, we examined Bcd protein profiles from images of immunofluorescently stained embryos in *L. sericata*, *D. melanogaster*, and *D. busckii* embryos (Fig. 3*A*; see *Methods*). In Fig. 3*B Upper*, we show Bcd profiles from multiple embryos of each species, and in Fig. 3*B Lower*, we show the same data but with the x axis normalized by embryo length for each individual. Bcd protein extends farther in the larger eggs; however, when scaled to egg size, the Bcd gradients for the different species overlay one another.

For each embryo in all species studied, the apparent concentration of Bcd vs. position has an exponential form, $c(x) \propto \exp(-x/\lambda)$, which is consistent with the simplest model of diffusion and degradation (see *Methods*). Here, λ is a characteristic length; rapidly (slowly) decaying gradients have a short (long) λ . In a scatter plot of λ vs. egg length (Fig. 3*C*), we see that the large variations of egg length across species are associated with changes in absolute values of λ . Within each species, we observe significant embryo-to-embryo variability, as reported previously for *D. melanogaster* (14), indicating that individual egg

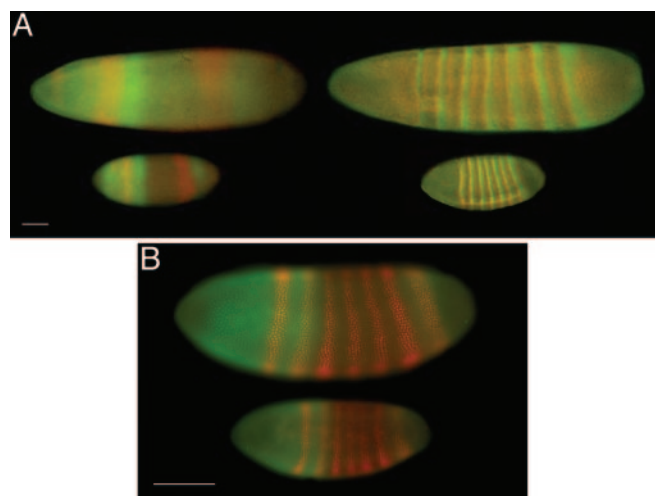


Fig. 2. Immunofluorescence stainings for products of the gap and pair-rule genes in higher diptera. (A) Immunofluorescence staining of *L. sericata* (upper embryos) and *D. melanogaster* (lower embryos) for Hunchback (green) and Giant (red) in the left column, and for Paired (green) and Runt (red) in the right column. (B) Anti-Hunchback (green) and anti-Runt (red) immunofluorescence staining of *D. melanogaster* (upper embryo) and *D. busckii* (lower embryo). (Scale bars: 100 μm .)

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