Superconductivity-Induced Anomalies in the Spin Excitation Spectra of Underdoped YBa$_2$Cu$_3$O$_{6+x}$

H. F. Fong and B. Keimer
Department of Physics, Princeton University, Princeton, New Jersey 08544
and Brookhaven National Laboratory, Upton, New York 11973

D. L. Milius and I. A. Aksay
Department of Chemical Engineering, Princeton University, Princeton, New Jersey 08544
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Polarized and unpolarized neutron scattering have been used to determine the effect of superconductivity on the magnetic excitation spectra of YBa$_2$Cu$_3$O$_{6.5}$ ($T_c = 52$ K) and YBa$_2$Cu$_3$O$_{6.7}$ ($T_c = 67$ K). Pronounced enhancements of the spectral weight centered around 25 and 33 meV, respectively, are observed below $T_c$ in both crystals, compensated predominantly by a loss of spectral weight at higher energies. The data provide important clues to the origin of the 40 meV magnetic resonance peak in YBa$_2$Cu$_3$O$_7$.

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Recently a new magnetic resonance mode has been found in the superconducting state of YBa$_2$Cu$_3$O$_7$ by inelastic neutron scattering. The mode occurs at an energy of 40 meV and wave vector $q = (\pi/a, \pi/a)$, and disappears in the normal state [1–3]. Since this mode is a novel signature of the superconducting state in the cuprates and has not been observed in any other material, much theoretical effort has gone into its interpretation. Qualitative considerations on the basis of a BCS pairing model show that quasiparticle pair production across the superconducting energy gap can give rise to enhanced spin-flip neutron scattering below the superconducting transition, provided that the order parameter changes phase on the Fermi surface [1,4]. More elaborate theories are required to explain the experimental features of the mode in detail, especially its sharpness in both energy and momentum. Final-state interactions between the quasiparticles [5] as well as band structure anomalies [6] have been suggested to account for the experimental data in the framework of a $d$-wave BCS model. Predictions derived from the interlayer pair tunneling theory of high temperature superconductivity explain most features of the neutron data without invoking such effects [7]. A more complicated order parameter with a sign change between different bands [8] and a collective mode in the particle-particle (rather than particle-hole) channel [9] have also been proposed. Clearly, more experimental information is required in order to discriminate between these divergent interpretations of the 40 meV mode. Open questions include the dependence of the energy, width, and spectral weight of the resonance peak on the doping level, and the relation between the resonance peak and the magnetic excitations spectrum in the normal state.

These issues are addressed in this Letter by systematically studying the influence of superconductivity on the magnetic excitation spectra of underdoped YBa$_2$Cu$_3$O$_{6+x}$. The doping dependence of the magnetic excitation spectrum of this system has already been characterized extensively in prior work. Briefly, the spin excitations in the antiferromagnetic regime ($x \approx 0.4$) are well described by the spin wave theory [10–12]. For $x \approx 0.4$, the magnetic response is broadened in $q$ and the spectral weight is depressed at low energies [12,13]. We have observed similar features in our samples. However, in these second-generation experiments we have taken data with very high counting statistics and found that the onset of superconductivity leads to a pronounced redistribution of the spectral weight. The energy of maximal spectral weight enhancement increases monotonically with the superconducting transition temperature.

The samples used for the present study were two YBa$_2$Cu$_3$O$_{6+x}$ single crystals of volumes ~3 cm$^3$ and mosaic spreads 0.8° and 1.4° (full width at half maximum), respectively. The samples were oxygen depleted in their as-grown state and were annealed in air at 640 °C for different lengths of time. The average oxygen content during the anneal was monitored by thermogravimetric analysis. After the average oxygen content was adjusted by this procedure, the samples were sealed in quartz tubes and kept at 740 °C for about two weeks is order to achieve a homogeneous distribution of the oxygen content. The uniform susceptibility measured on a piece cut from the first sample, shown in the inset of Fig. 2, demonstrates that the oxygen content is indeed highly homogeneous: The width of the superconducting transition ($T_c = 52$ K midpoint) is very similar to the ones reported for very high quality small crystals in this doping regime [14]. Susceptibility measurements on the second crystal revealed $T_c = 67$ K (midpoint) with a somewhat larger width. A comparison with previously reported calibrations of the lattice constants and transition

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temperatures [14,15] shows that the oxygenation states of the two crystals are $x \sim 0.5 \pm 0.05$ and $x \sim 0.7 \pm 0.05$, respectively.

The neutron scattering measurements were performed at the H4M, H7, and H8 triple axis spectrometers at the High Flux Beam Reactor at the Brookhaven National Laboratory. The beam collimations were 40'-40'-80'-80' and the final energy was 30.5 meV for the unpolarized-beam measurements. The (002) reflection of pyrolytic graphite was used as both monochromator and analyzer. For the polarized-beam measurements we used Heusler alloy crystals as monochromator and analyzer, beam collimations 40'-60'-80'-80' and 28 meV final energy. The flipping ratio was 33 (corresponding to $\sim 95\%$ beam polarization) for both horizontal and vertical guide fields at the sample. The energy resolutions were $\sim 7$ meV (full width at half maximum) in both cases.

Figure 1 shows typical constant-energy scans for YBa$_2$Cu$_3$O$_{6.5}$ taken with both unpolarized and polarized beams. As previously reported [12,13], the intensity is peaked at an in-plane wave vector of $q = \left( \frac{1}{2}, \frac{1}{2}, 0 \right)$. [The reciprocal space coordinates ($H, K, L$) are quoted in units of the reciprocal lattice vectors $2\pi/a \sim 2\pi/b \sim 1.63 \, \text{Å}^{-1}$ and $2\pi/c \sim 0.53 \, \text{Å}^{-1}$]. At all temperatures the magnetic intensity is sinusoidally modulated as a function of the wave vector perpendicular to the CuO$_2$ planes, a behavior which is also characteristic of both acoustic spin waves in antiferromagnetic YBa$_2$Cu$_3$O$_{6+x}$ [10–12] and of the 40 meV resonance peak in YBa$_2$Cu$_3$O$_7$ [1–3]. Our data were taken at momentum transfers for which this intensity modulation is maximum.

Constant-energy scans with similar counting statistics were taken at a series of temperatures and fitted to Gaussians in order to extract the amplitude and width of the magnetic signal. The fitted $q$ width does not change with temperature outside of the experimental error. By contrast, the amplitude displays a dramatic temperature dependence (Fig. 2): As previously observed [12,13], the intensity increases gradually as $T_c$ is approached from above. The ensuing abrupt increase by $\sim 30\%$ upon cooling through $T_c$ is only clearly discernible due to the high counting statistics of our data and has thus far not been reported. (A sharp magnetic feature at $h\omega = 27$ meV was previously observed by Tranquada et al. [13] at this doping level but its temperature dependence was not measured.)

In principle, the observed enhancement of the neutron cross section below $T_c$ could also arise from a superconductivity-induced phonon shift and/or linewidth change. We used two independent methods to rule out this possibility. First, we used an unpolarized beam to monitor the phonon intensity in this energy range at high momentum transfers where lattice dynamical models [1] predict strong phonon scattering. No difference of the

FIG. 1. (a) Unpolarized-beam scans at $h\omega = 25$ meV and (b) polarized-beam scans at $h\omega = 21$ meV for YBa$_2$Cu$_3$O$_{6.5}$, with $Q = (H, H, -5.4)$. In (a) the lines are fits to Gaussians as discussed in the text. In (b) the open (closed) symbols are data taken for horizontal (vertical) field at the sample position. The upper profile in (b) shows magnetic scattering in the spin-flip (SF) channel, while the lower profile is phonon scattering in the non-spin-flip (NSF) channel. The curves are guides to the eye.

FIG. 2. The open circles are the amplitudes of the magnetic cross section at $h\omega = 25$ meV, extracted from Gaussian fits to unpolarized-beam constant-energy scans. The closed circles are the spin-flip peak intensities measured at $Q = (\frac{3}{2}, \frac{1}{2}, -1.7)$ with a polarized beam, corrected for the background and scaled to the unpolarized-beam data. The inset shows the field-cooled dc susceptibility at $H = 10 \, \text{G}$ measured by SQUID magnetometry on a small piece cut from the inside (not the surface) of the sample. Because of demagnetization effects the Meissner fraction was nominally $>100\%$. The data were therefore normalized to the maximum susceptibility.
intensities above and below $T_c$ was observed outside the statistical error. Second, we used spin polarization analysis to separate the non-spin-flip (phonon) and spin-flip (magnetic) cross sections. Depending on the energy transfer, the data were taken in two scattering geometries in which momentum transfers of the forms either $(H,H,L)$ or $(3H,H,L)$ were accessible. Use of both configurations was necessary to avoid accidental elastic scattering which can give rise to spurious signals at certain energy transfers [1]. Typical raw data are shown in Fig. 1(b). The phonon cross section does not depend strongly on the in-plane momentum transfer at energies around 25 meV, as shown in the figure. The spin-flip scattering is peaked at $Q = (\frac{1}{2}, \frac{1}{2}, 0)$ and shows the characteristic factor-of-two polarization dependence when the neutron spin at the sample position is rotated from $Q$ parallel (horizontal field) to $Q$ perpendicular (vertical field) [16]. The peak in the unpolarized-beam data of Fig. 1(a) thus arises exclusively from magnetic scattering. The filled circles in Fig. 2 are the spin-flip peak intensity at 25 meV, corrected for the non-spin-flip scattering measured with counting statistics comparable to those of the unpolarized-beam data. The non-spin-flip scattering was measured with similar statistics and showed no change upon cooling through $T_c$. The excellent agreement with the unpolarized-beam data again confirms the magnetic origin of the enhanced cross section below $T_c$.

Figure 3 shows the difference between spectra measured above and below $T_c$ for both YBa$_2$Cu$_3$O$_{6.5}$ and YBa$_2$Cu$_3$O$_{6.7}$. In addition to these scans, $Q$ scans were performed at several energies above and below $T_c$ in order to obtain the energy and temperature dependence of the background throughout the Brillouin zone. For most of the data in Fig. 3 the background (originating mostly from single-phonon and multiphonon scattering events) was found to be temperature independent in the temperature range of interest. For the measurements taken below 18 meV in YBa$_2$Cu$_3$O$_{6.7}$ the background increases uniformly throughout the Brillouin zone by about 10% upon heating from 10 to 80 K. The origin of this increase is unknown (though it could arise from multiphonon scattering), but it is unlikely to be related to magnetic excitations. The subtractions below 18 meV in the lower panel of Fig. 3 were corrected for this overall effect and thus show only differences centered at $Q = (\frac{1}{2}, \frac{1}{2}, 0)$. The data were further corrected for the Bose population factor $[1 - \exp(-\frac{\hbar \omega}{k_B T})]^{-1}$ in order to convert the magnetic cross section to the dynamical spin susceptibility $\chi''(\mathbf{q}, \omega)$. Following the same procedure as discussed above for YBa$_2$Cu$_3$O$_{6.5}$, we found that the 33 meV spectral weight enhancement for YBa$_2$Cu$_3$O$_{6.7}$ again sets in below $T_c$. The difference plots of Fig. 3 therefore directly reveal the effect of superconductivity on $\chi''(\mathbf{q}, \omega)$.

Several interesting features are apparent in the difference spectra. First, the YBa$_2$Cu$_3$O$_{6.5}$ data show that most (but not all) of the spectral weight enhancement around 25 meV is drawn from higher energies in the 30–40 meV range. Work with tighter energy resolution [12,17] shows that the spectral weight is suppressed at energies below ~5 meV in the superconducting state, thus accounting for the remaining spectral weight. Though the evidence is weaker, presumably because the 33 meV resonance is drawn from a wider energy range, this scenario is also consistent with the data on YBa$_2$Cu$_3$O$_{6.7}$. The conservation of spectral weight is expected on the basis of the total moment sum rule, but the fact that the resonance spectral weight is drawn from normal-state excitations of both higher and lower energies is surprising and inconsistent with the simplest picture in which the resonance is exclusively built up from states below the superconducting energy gap.

The data of Fig. 3 also demonstrate that the 40 meV resonance peak observed in the optimally doped compound evolves continuously with the carrier concentration. A synopsis of the data at all three doping levels is given in Fig. 4. The resonance is broadened in the deeply underdoped regime but already resolution limited for YBa$_2$Cu$_3$O$_{6.7}$. Although the data are of course too sparse to establish a functional dependence of the resonance energy on $T_c$ or doping level, the resonance energy increases monotonically with $T_c$, and the presently available data are consistent with a simple proportionality. Note that a very recent photoemission study of
underdoped $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ [18] demonstrates that the superconducting energy gap in the single-particle density of states is independent of doping.

The data of Fig. 4 also dispel possible speculations about an essential relationship between the 40 meV resonance and a phonon of slightly higher energy (42.5 meV) [11] obtained on underdoped $\text{YBa}_2\text{Cu}_3\text{O}_7$ [1]. Details will be given in a forthcoming full publication [17]. Note that the normal state magnetic intensity in the range $10 \text{ meV} \leq \hbar\omega \leq 40 \text{ meV}$ decreases dramatically (at least by a factor of 5) in the same doping interval.

In summary, our data are consistent with previous work on underdoped $\text{YBa}_2\text{Cu}_3\text{O}_{6.7}$ in the normal state [12,13], but additional spectral enhancements, undoubtedly analogs of the 40 meV resonance in $\text{YBa}_2\text{Cu}_3\text{O}_7$, are observed in the superconducting state. Some new and surprising aspects of the resonance are elucidated, including in particular its doping dependence and its relation to the magnetic spectrum in the normal state. Obviously, the theoretical models proposed to explain the 40 meV mode should now be tested against this more extensive data set.

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