

Prenex form.

A sentence is in *prenex form* if all its quantifiers come at the very start. i.e., no quantifiers are within the scope of a truth-functional connective.

Prenexing rules.

Let P be a sentence in which the variable x does not occur. (If x occurs in P , but P is not in the scope of (Qx) , then the sentence P' that results from replacing x throughout P with a different variable is equivalent to P .) Then the following pairs of sentences are interderivable.

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|------|-------------------------------|---------------------------------|
| (1) | $\neg(x)Fx$ | $(\exists x)\neg Fx$ |
| (2) | $\neg(\exists x)Fx$ | $(x)\neg Fx$ |
| (3) | $P \& (x)Fx$ | $(x)(P \& Fx)$ |
| (4) | $P \vee (x)Fx$ | $(x)(P \vee Fx)$ |
| (5) | $P \& (\exists x)Fx$ | $(\exists x)(P \& Fx)$ |
| (6) | $P \vee (\exists x)Fx$ | $(\exists x)(P \vee Fx)$ |
| (7) | $P \rightarrow (\exists x)Fx$ | $(\exists x)(P \rightarrow Fx)$ |
| (8) | $P \rightarrow (x)Fx$ | $(x)(P \rightarrow Fx)$ |
| (9) | $(\exists x)Fx \rightarrow P$ | $(x)(Fx \rightarrow P)$ |
| (10) | $(x)Fx \rightarrow P$ | $(\exists x)(Fx \rightarrow P)$ |