

## HOMEWORK #1 SOLUTIONS

- 1.
- a) It's just not true that if Jane Austen wrote a book (W) then it has a happy ending (H).  
 $\neg(W \rightarrow H)$
  - b) Hegel was neither a great philosopher (P) nor a great historian (H).  
 $\neg P \ \& \ \neg H$
  - c) Sieglinde will survive (S), and either her son will gain the Ring (G) and Wotan's plan will be fulfilled (F) or else Valhalla will be destroyed (D).  
 $S \ \& \ ((G \ \& \ F) \ \vee \ D)$
  - d) Wotan (W) and Alberic (A) will not both be satisfied  
 $\neg(W \ \& \ A)$

2.

- a)
- |     |                                   |          |
|-----|-----------------------------------|----------|
| (1) | $P \rightarrow (Q \rightarrow R)$ | A        |
| (2) | $P \rightarrow Q$                 | A        |
| (3) | $P$                               | A // R   |
| (4) | $Q \rightarrow R$                 | 1, 3 MPP |
| (5) | $Q$                               | 2, 3 MPP |
| (6) | $R$                               | 4, 5 MPP |
- b)
- |     |                            |               |
|-----|----------------------------|---------------|
| (1) | $\neg\neg Q \rightarrow P$ | A             |
| (2) | $\neg P$                   | A // $\neg Q$ |
| (3) | $\neg\neg\neg Q$           | 1, 2 MTT      |
| (4) | $\neg Q$                   | 3 DN          |
- c)
- |     |                            |          |
|-----|----------------------------|----------|
| (1) | $(A \vee B) \rightarrow T$ | A        |
| (2) | $Z \rightarrow A$          | A        |
| (3) | $T \rightarrow W$          | A        |
| (4) | $Z$                        | A // W   |
| (5) | $A$                        | 2, 4 MPP |
| (6) | $A \vee B$                 | 5 VI     |
| (7) | $T$                        | 1, 6 MPP |
| (8) | $W$                        | 3, 7 MPP |

d)

(1)	$(A \rightarrow B) \& (C \rightarrow A)$	A
(2)	$(C \& (W \rightarrow Z)) \& W$	A // $(B \vee D) \& (Z \vee E)$
(3)	$A \rightarrow B$	1 &E
(4)	$C \rightarrow A$	1 &E
(5)	$W$	2 &E
(6)	$C \& (W \rightarrow Z)$	2 &E
(7)	$C$	6 &E
(8)	$W \rightarrow Z$	6 &E
(9)	$A$	4, 7 MPP
(10)	$B$	3, 9 MPP
(11)	$B \vee D$	10 VI
(12)	$Z$	8, 5 MPP
(13)	$Z \vee E$	12 VI
(14)	$(B \vee D) \& (Z \vee E)$	11, 13 &I